Functional Reactivity: Eschewing the Imperative

An Overview of Functional Reactive Programming in the Context of Yampa

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while system is

Reactive programming (1)

Input arrives running.

Output is generated in response to input in an interleaved and fashion.

Contrast

The notions of

- time
- time-varying values, or

are inherent and central to reactive systems.

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Reactive Programming (2)

Reactive systems are

- generally concurrent
- often parallel
- often distributed

Thus, besides timeliness, difficulties related to development of concurrent, parallel, and distributed programming are also inherent.

The Synchronous Approach (1)

The "synchronous realisation" (France, 1980s):

If we heed the observation that time-varying values are central to reactive programming and

- express systems directly as of such entities
- adopt system-wide time, abstracting away processing delays (hence)

The Synchronous Approach (2)

...then:

- systems can be described declaratively at a very high level of abstraction
- simple, deterministic semantics, facilitates reasoning
- many problems related to imperative idioms for concurrency and synchronisation simply vanishes.

Contrast programming with values at isolated points in time in a fundamentally temporally agnostic setting.

The Synchronous Approach (3)

The synchronous languages were invented in France in the 1980s. The first ones were:

- Esterel
- Lustre
- Signal

Have been very successful; e.g. lots of industrial applications.

Many new languages and variations since then.

Functional Reactive Programming

Functional Reactive Programming (FRP):

- Paradigm for reactive, concurrent programming in purely declarative (functional) setting.
- Originated from Functional Reactive Animation (Fran) (Elliott & Hudak).
- Has evolved in a number of directions and into different concrete implementations.
- (Usually) continuous notion of time and additional support for discrete events.

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FRP applications

Some domains where FRP or FRP-like ideas have been used:

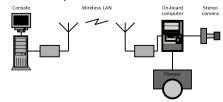
- Graphical Animation
- Robotics
- Vision
- GUIs
- Hybrid modeling
- Video games
- Sensor networks
- · Audio processing and generation
- Financial, event-based systems

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Example: Robotics (1)

[PPDP'02, with Izzet Pembeci and Greg Hager, Johns Hopkins University]

Hardware setup:



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Example: Robotics (2)



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Related approaches

FRP related to:

- Synchronous languages, like Esterel, Lucid Synchrone.
- Modeling languages, like Simulink, Modelica.

Distinguishing features of FRP:

- · First class reactive components.
- · Allows highly dynamic system structure.
- Supports hybrid (mixed continuous and discrete) systems.

Yampa

- An FRP system originating at Yale
- in Haskell (a Haskell library).
- used as the basic structuring framework.
- Notionally
- Discrete-time signals modelled by continuous-time signals and an option type, allowing for systems.
- Advanced allows for highly dynamic system structure.

Yampa?

Yampa is a river with long calmly flowing sections and abrupt whitewater transitions in between.

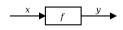


A good metaphor for hybrid systems!

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Signal functions

Key concept:



Intuition:

 $\begin{array}{ll} \operatorname{Signal} \ \alpha \ \approx \ \operatorname{Time} \rightarrow \alpha \\ x \ \colon \quad \operatorname{Signal} \ \operatorname{T1} \\ y \ \colon \quad \operatorname{Signal} \ \operatorname{T2} \end{array}$

f:: Signal T1 \rightarrow Signal T2

Additionally:

requirement.

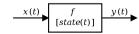
are first class entities in Yampa:

SF $\alpha \beta \approx \text{Signal } \alpha \rightarrow \text{Signal } \beta$

Signal functions and state

Alternative view:

Signal functions can encapsulate state.



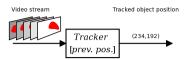
state(t) summarizes input history x(t'), $t' \in [0, t]$.

Functions on signals are either:

- : y(t) depends on x(t) and state(t)
- y(t) depends only on x(t)

Example: Video tracker

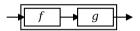
Video trackers are typically stateful signal functions:



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Building systems (1)

How to build systems? Think of a signal function as a . Blocks have inputs and outputs and can be combined into larger blocks. For example, serial composition:

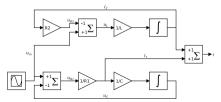


A *combinator* can be defined that captures this idea:

(>>>) :: SF a b -> SF b c -> SF a c

Building systems (2)

But systems can be complex:



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Arrows

Yampa uses John Hughes' framework:

- Abstract data type interface for function-like types (or "blocks", if you prefer).
- Particularly suitable for types representing process-like computations.
- Provides a minimal set of "wiring" combinators.

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What is an arrow? (1)

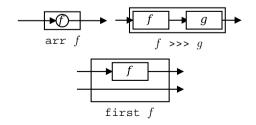
- A a of arity two.
- Three operators:

```
- :
arr :: (b->c) -> a b c
- :
(>>>) :: a b c -> a c d -> a b d
- :
first :: a b c -> a (b,d) (c,d)
```

A set of that must hold.

What is an arrow? (2)

These diagrams convey the general idea:



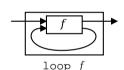
Some arrow laws

Being able to use simple algebraic laws like these greatly facilitates reasoning about programs.

The loop combinator

Another important operator is loop: a fixed-point operator used to express recursive arrows or

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Remarkably, the four combinators arr, >>>, first, and loop suffice for expressing

Some more arrow combinators (1)

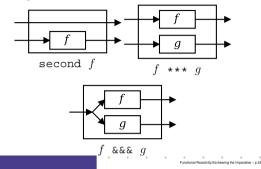
```
second :: Arrow a =>
    a b c -> a (d,b) (d,c)

(***) :: Arrow a =>
    a b c -> a d e -> a (b,d) (c,e)

(&&&) :: Arrow a =>
    a b c -> a b d -> a b (c,d)
```

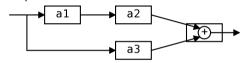
Some more arrow combinators (2)

As diagrams:



Example: A Simple Network

A simple network:



a1, a2, a3 :: A Double Double

One way to express it using arrow combinators:

The arrow do notation (1)

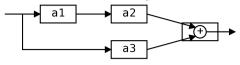
Using the basic combinators directly can be cumbersome. Ross Paterson's **do**-notation for arrows provides a convenient alternative. Only

```
\begin{array}{c} \operatorname{proc}\ pat\ ->\operatorname{do}\left[\ \operatorname{rec}\ \right]\\ pat_1 <-\operatorname{sfexp}_1 -<\operatorname{exp}_1\\ pat_2 <-\operatorname{sfexp}_2 -<\operatorname{exp}_2\\ \dots\\ pat_n <-\operatorname{sfexp}_n -<\operatorname{exp}_n\\ \operatorname{returnA} -<\operatorname{exp} \end{array}
```

Also: let $pat = exp \equiv pat <- arr id -< exp$

The arrow do notation (2)

Let us redo the example using this notation:



```
circuit_v4 :: A Double Double
circuit_v4 = proc x -> do
    y1 <- a1 -< x
    y2 <- a2 -< y1
    y3 <- a3 -< x
    returnA -< y2 + y3</pre>
```

Yampa and Arrows

The Yampa signal function type is an arrow.

Signal function instances of the core combinators:

```
arr :: (a -> b) -> SF a b
>>> :: SF a b -> SF b c -> SF a c
first :: SF a b -> SF (a,c) (b,c)
loop :: SF (a,c) (b,c) -> SF a b
```

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Some further basic signal functions

```
• identity :: SF a a
  identity = arr id

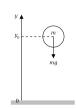
• constant :: b -> SF a b
  constant b = arr (const b)

• integral :: VectorSpace a s=>SF a a

• time :: SF a Time
  time = constant 1.0 >>> integral

• (^<<) :: (b->c) -> SF a b -> SF a c
  f (^<<) sf = sf >>> arr f
```

A bouncing ball



$$y = y_0 + \int v \, \mathrm{d}t$$
$$v = v_0 + \int -9.81$$

On impact:

$$v = -v(t-)$$

(fully elastic collision)

Modelling the bouncing ball: part 1

Free-falling ball:

```
type Pos = Double

type Vel = Double

fallingBall ::
    Pos -> Vel -> SF () (Pos, Vel)

fallingBall y0 v0 = proc () -> do
    v <- (v0 +) ^<< integral -< -9.81
    y <- (y0 +) ^<< integral -< v
    returnA -< (y, v)</pre>
```

Events

Conceptually, signals are only defined at discrete points in time, often associated with the occurrence of some **event**.

Yampa models discrete-time signals by lifting the of continuous-time signals:

Associating information with an event occurrence:

```
tag :: Event a -> b -> Event b
```

Modelling the bouncing ball: part 2

Detecting when the ball goes through the floor:

Switching

Q: How and when do signal functions "start"?

- A: "apply" a signal functions to its input signal at some point in time.
 - This creates a "running" signal function
 - The new signal function instance often replaces the previously running instance.

Switchers thus allow systems with to be described.

The basic switch

Idea:

- Allows one signal function to be replaced by another.
- Switching takes place on the first occurrence of the switching event source.

```
switch ::
    SF a (b, Event c)
    -> (c -> SF a b)
    -> SF a b
```

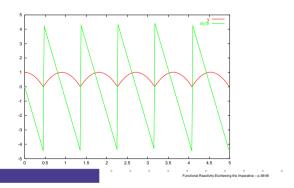
Modelling the bouncing ball: part 3

Making the ball bounce:

```
bouncingBall :: Pos -> SF () (Pos, Vel)
bouncingBall y0 = bbAux y0 0.0
  where
    bbAux y0 v0 =
    switch (fallingBall' y0 v0) $ \((y,v) -> bbAux y (-y))
```

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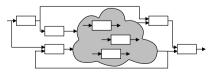
Simulation of bouncing ball



Highly dynamic system structure?

Basic switch allows one signal function to be replaced by another.

· What about more general structural changes?



What about state?

Dynamic signal function collections

Idea:

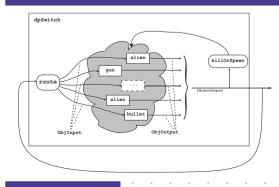
- Switch over of signal functions.
- On event, "freeze" running signal functions into collection of signal function preserving encapsulated
- · Modify collection as needed and switch back in.

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Example: Space Invaders



Overall game structure



Describing the alien behavior (1)

Describing the alien behavior (2)

Describing the alien behavior (3)

Describing the alien behavior (4)

```
sl <- shield -< oiHit oi
 die <- edge -< sl <= 0
returnA -< ObjOutput {
            ooObsObjState = oosAlien p h v,
            ooKillReq
                        = die,
            ooSpawnReg = noEvent
where
 v0 = zeroVector
```

State in alien

Each of the following signal functions used in alien encapsulate state:

- noiseR
- impulseIntegral
- occasionally integral
- hold
- shield
- iPre
- edge
- forceField

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Why not imperative, then?

If state is so important, why not stick to imperative/object-oriented programming where we have "state for free"?

- · Advantages of declarative programming retained:
 - High abstraction level.
 - Referential transparency, algebraic laws: formal reasoning is simpler.
- Synchronous approach avoids "event-call-back soup", meaning robust, easy-to-understand semantics.