#### MGS 2005 Functional Reactive Programming

Lecture 1: Introduction to FRP, Yampa, and Arrows

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## **Reactive programming**

#### **Reactive systems**:

- Input arrives *incrementally* while system is running.
- Output is generated in response to input in an interleaved and *timely* fashion.

#### Contrast transformational systems.

The notions of

- time
- time-varying values, or signals

are inherent and central for reactive systems.

## Outline

- Brief introduction to FRP and Yampa
- Signal functions
- Arrows

## **Functional Reactive Programming**

What is Functional Reactive Programming (FRP)?

- Paradigm for reactive programming in a functional setting.
- Originated from Functional Reactive Animation (Fran) (Elliott & Hudak).
- Has evolved in a number of directions and into different concrete implementations.

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## **FRP** applications

Some domains where FRP has been used:

- Graphical Animation (Fran: Elliott, Hudak)
- Robotics (Frob: Peterson, Hager, Hudak, Elliott, Pembeci, Nilsson)
- Vision (FVision: Peterson, Hudak, Reid, Hager)
- GUIs (Fruit: Courtney)
- Hybrid modeling (Nilsson, Hudak, Peterson)

## **Related languages and paradigms**

FRP related to:

- Synchronous languages, like Esterel, Lucid Synchrone.
- Modeling languages, like Simulink, Modelica.

## **Key FRP features**

- First class reactive components.
- Synchronous: all system parts operate in synchrony.
- Support for hybrid (mixed continuous and discrete time) systems.
- Allows dynamic system structure.

# Yampa

#### What is Yampa?

- The most recent Yale FRP implementation. People:
  - Antony Courtney
  - Paul Hudak
  - Henrik Nilsson
  - John Peterson
- A Haskell combinator library, a.k.a.
   Domain-Specific Embedded Language (DSEL).

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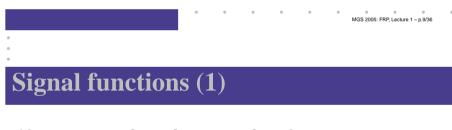
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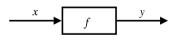
#### Yampa

What is Yampa?

- Structured using *arrows*.
- Continuous-time signals (conceptually)
- Option type *Event* to handle discrete-time signals.
- Advanced *switching constructs* to describe systems with dynamic structure.



Key concept: functions on signals.



Intuition:

Signal  $\alpha \approx \text{Time} \rightarrow \alpha$  x :: Signal T1 y :: Signal T2 $f :: \text{Signal T1} \rightarrow \text{Signal T2}$ 

## Yampa?

Yampa is a river with long calmly flowing sections and abrupt whitewater transitions in between.



#### A good metaphor for hybrid systems!

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## **Signal functions (2)**

Additionally, *causality* required: output at time t must be determined by input on interval [0, t].

Signal functions are said to be

- pure or stateless if output at time t only depends on input at time t
- *impure* or *stateful* if output at time *t* depends on input over the interval [0, *t*].

## **Signal functions in Yampa**

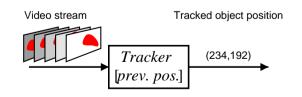
- Signal functions are first class entities. Intuition: SF  $\alpha \beta \approx$  Signal  $\alpha \rightarrow$  Signal  $\beta$
- *Signals* are *not* first class entities: they only exist indirectly through signal functions.

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## **Example: Video tracker**

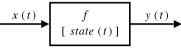
Video trackers are typically stateful signal functions:



## Signal functions and state

Alternative view:

Signal functions can encapsulate state.



state(t) summarizes input history x(t'),  $t' \in [0, t]$ . Thus, really a kind of **process**.

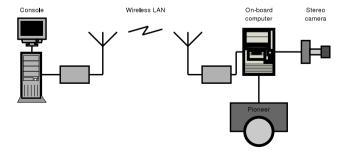
From this perspective, signal functions are:

- *stateful* if y(t) depends on x(t) and state(t)
- *stateless* if y(t) depends only on x(t)

## **Example: Robotics (1)**

[PPDP'02, with Izzet Pembeci and Greg Hager, Johns Hopkins University]

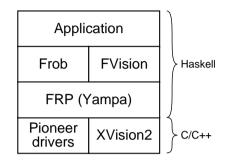
Hardware setup:



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## **Example: Robotics (2)**

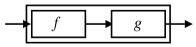
#### Software architecture:



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Yampa and Arrows (1)										

In Yampa, systems are described by combining signal functions (forming new signal functions).

For example, serial composition:



A *combinator* can be defined that captures this idea:

```
(>>>) :: SF a b -> SF b c -> SF a c
```

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### **Example: Robotics (3)**

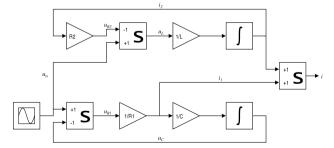


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## Yampa and Arrows (2)

But systems can be complex:



How many and what combinators do we need to be able to describe arbitrary systems?

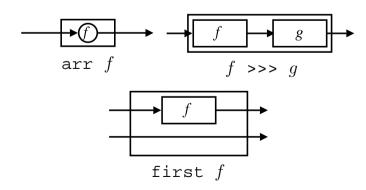
## Yampa and Arrows (3)

John Hughes' arrow framework:

- Abstract data type interface for function-like types.
- Particularly suitable for types representing process-like computations.
- Related to *monads*, since arrows are computations, but more general.
- Provides a minimal set of "wiring" combinators.

## What is an arrow? (2)

These diagrams convey the general idea:



## What is an arrow? (1)

- A type constructor a of arity two.
- Three operators:
  - lifting:
    - arr ::  $(b \rightarrow c) \rightarrow a b c$
  - composition:
    - (>>>) :: a b c -> a c d -> a b d
  - widening:

first ::  $a b c \rightarrow a (b,d) (c,d)$ 

• A set of *algebraic laws* that must hold.

#### The Arrow class

In Haskell, a *type class* is used to capture these ideas (except for the laws):

class Arrow a where

arr :: (b -> c) -> a b c
(>>>) :: a b c -> a c d -> a b d
first :: a b c -> a (b,d) (c,d)

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## Functions are arrows (1)

Functions are a simple example of arrows. The arrow type constructor is just (->) in that case.

Exercise 1: Suggest suitable definitions of

- arr
- (>>>)
- first

for this case!

(We have not looked at what the laws are yet, but they are "natural".)

## **Functions are arrows (3)**

- f >>> g = \a -> g (f a) **Or**
- f >>> g = g . f **or even**
- (>>>) = flip (.)
- first  $f = \langle (b,d) \rightarrow (f b,d)$

### **Functions are arrows (2)**

#### Solution:

• arr = id To see this, recall id :: t -> t arr :: (b->c) -> a b c Instantiate with

> a = (->) t = b->c = (->) b c

### **Functions are arrows (4)**

Arrow instance declaration for functions:

instance Arrow (->) where arr = id (>>>) = flip (.) first f = \(b,d) -> (f b,d)

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#### **Arrow laws**

```
(f >>> g) >>> h = f >>> (g >>> h)
arr (f >>> g) = arr f >>> arr g
arr id >>> f = f
f = f >>> arr id
first (arr f) = arr (first f)
first (f >>> g) = first f >>> first g
```

*Exercise 2:* Draw diagrams illustrating the first and last law!

## The loop combinator (2)

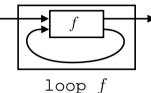
Not all arrow instances support loop. It is thus a method of a separate class:

class Arrow a => ArrowLoop a where loop :: a (b, d) (c, d) -> a b c

Remarkably, the four combinators arr, >>>, first, and loop are sufficient to express any conceivable wiring!

### The loop combinator (1)

Another important operator is loop: a fixed-point operator used to express recursive arrows or *feedback*:



### Some more arrow combinators (1)

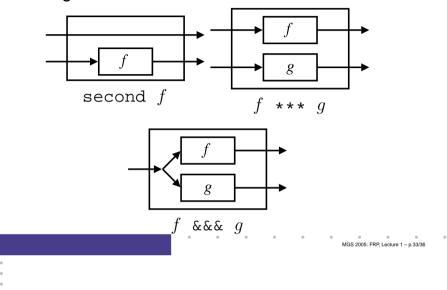
```
second :: Arrow a =>
    a b c -> a (d,b) (d,c)
(***) :: Arrow a =>
    a b c -> a d e -> a (b,d) (c,e)
(&&&) :: Arrow a =>
    a b c -> a b d -> a b (c,d)
```

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#### Some more arrow combinators (2)

As diagrams:



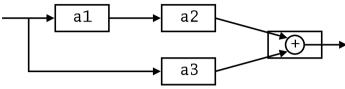
## Reading (1)

- John Hughes. Generalising monads to arrows. Science of Computer Programming, 37:67–111, May 2000
- John Hughes. Programming with arrows. In Advanced Functional Programming, 2004. To be published by Springer Verlag.
- Henrik Nilsson, Antony Courtney, and John Peterson. Functional reactive programming, continued. In *Proceedings of the 2002 Haskell Workshop*, pp. 51–64, October 2002.

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## Some more arrow combinators (3)

*Exercise 3:* Describe the following circuit using arrow combinators:



a1, a2, a3 :: A Double Double

**Exercise 4:** The combinators second, (\*\*\*), and (&&&) are not primitive, but defined in terms of arr, (>>>), and first. Suggest suitable definitions!

## Reading (2)

 Paul Hudak, Antony Courtney, Henrik Nilsson, and John Peterson. Arrows, robots, and functional reactive programming. In Advanced Functional Programming, 2002. LNCS 2638, pp. 159–187.

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