

Flow Visualization with Integral Surfaces

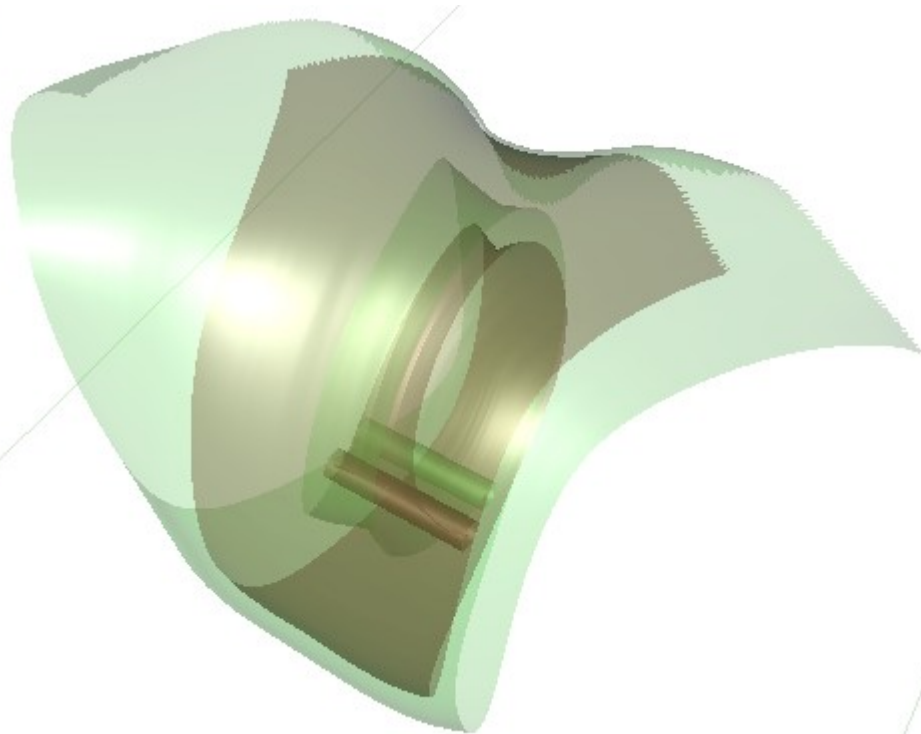
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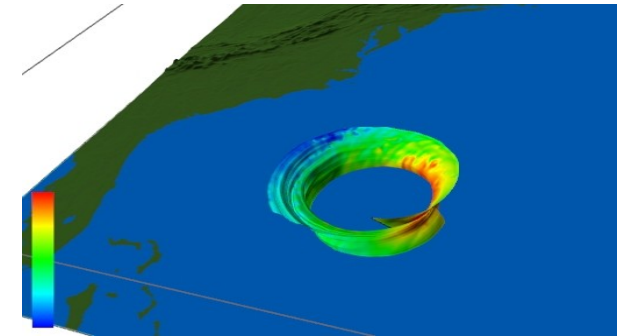


Swansea University
Prifysgol Abertawe

Overview

Flow Visualization with Integral Surfaces:

- Introduction to flow visualization
- Flow data and applications
- Stream, path, and streaklines
- Integral surface-based flow visualization
- Advantages of surfaces over curves
- Stream and path surfaces
- Stream and path surface construction
- Stream and path surface demo
- Streak surfaces and construction
- Streak surface demo
- Conclusions and Acknowledgments



What is Flow Visualization?

- A classic topic within scientific visualization
- The depiction of vector quantities (as opposed to scalar quantities)
- Applications include: aerodynamics, astronomy, automotive simulation, chemistry, computational fluid dynamics (CFD), engineering, medicine, meteorology, oceanography, **physics**, turbo-machinery design

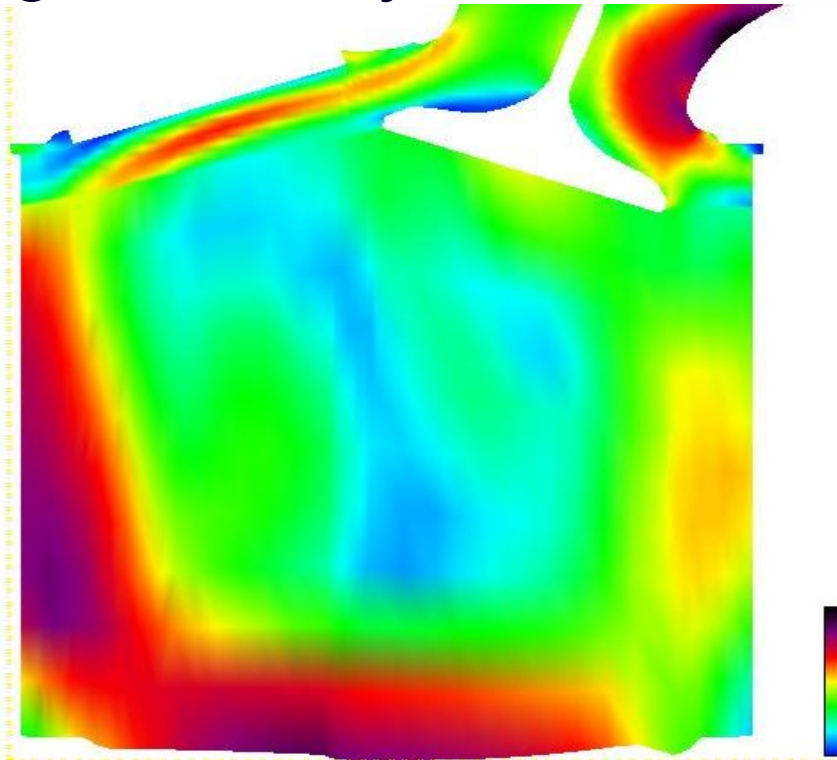
Challenges:

- to effectively visualize both *magnitude* + *direction*, often simultaneously
- large data sets
- time-dependent data
- What should be visualized? (data filtering/feature extraction)

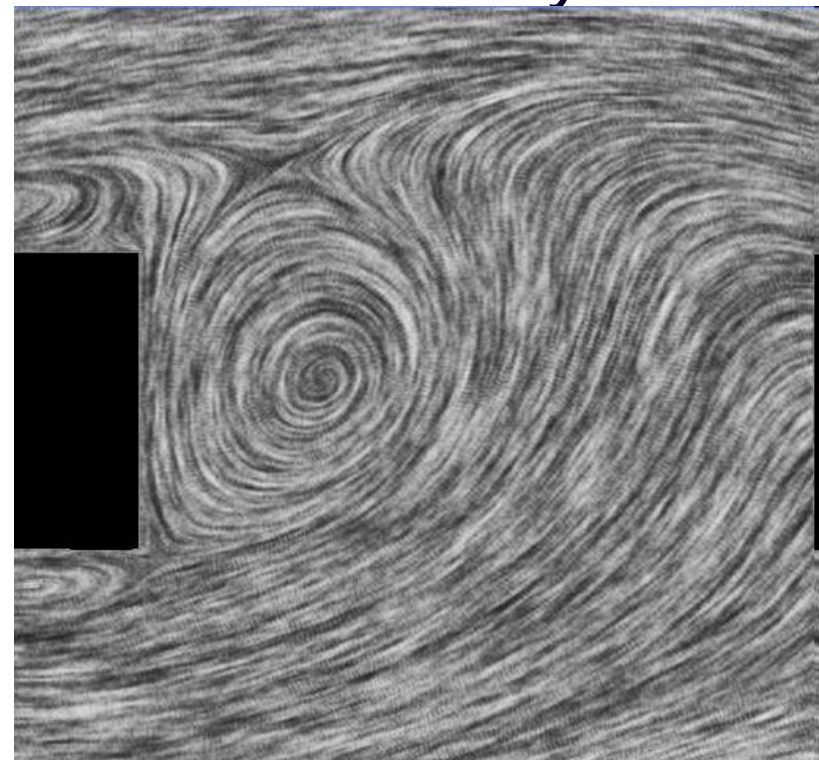
What is Flow Visualization?

Challenge: to effectively visualize both *magnitude* + *direction* often simultaneously

magnitude only

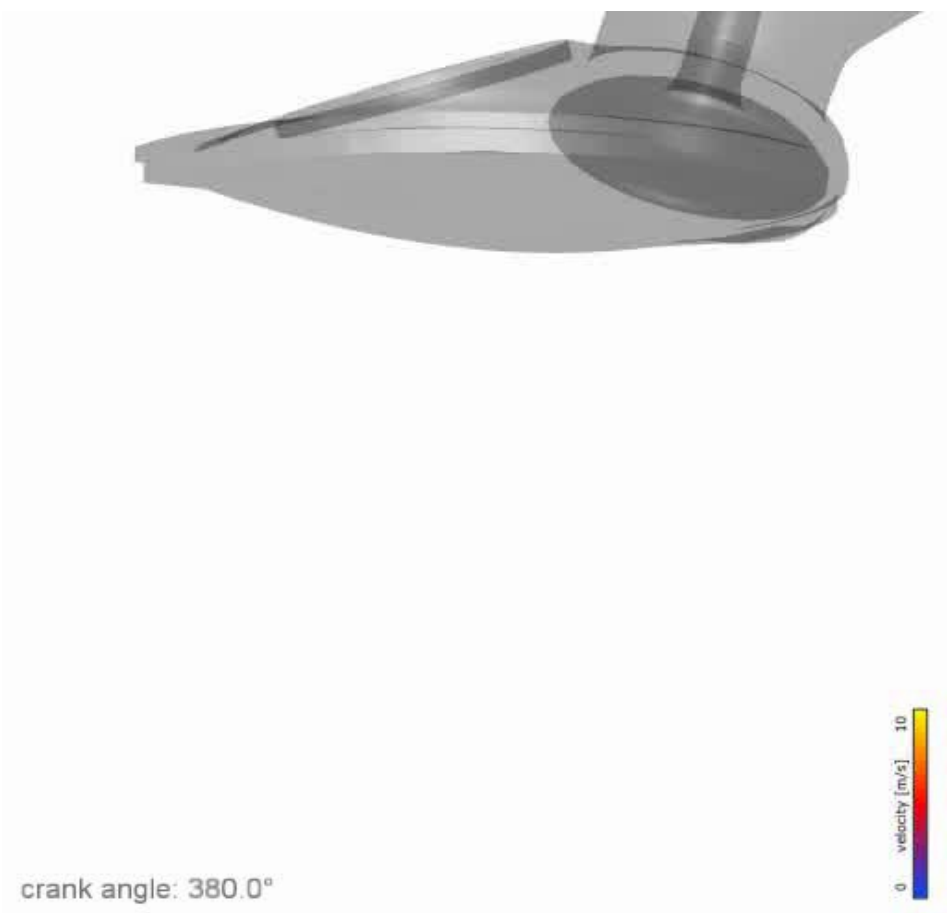


orientation only



Note on Computational Fluid Dynamics

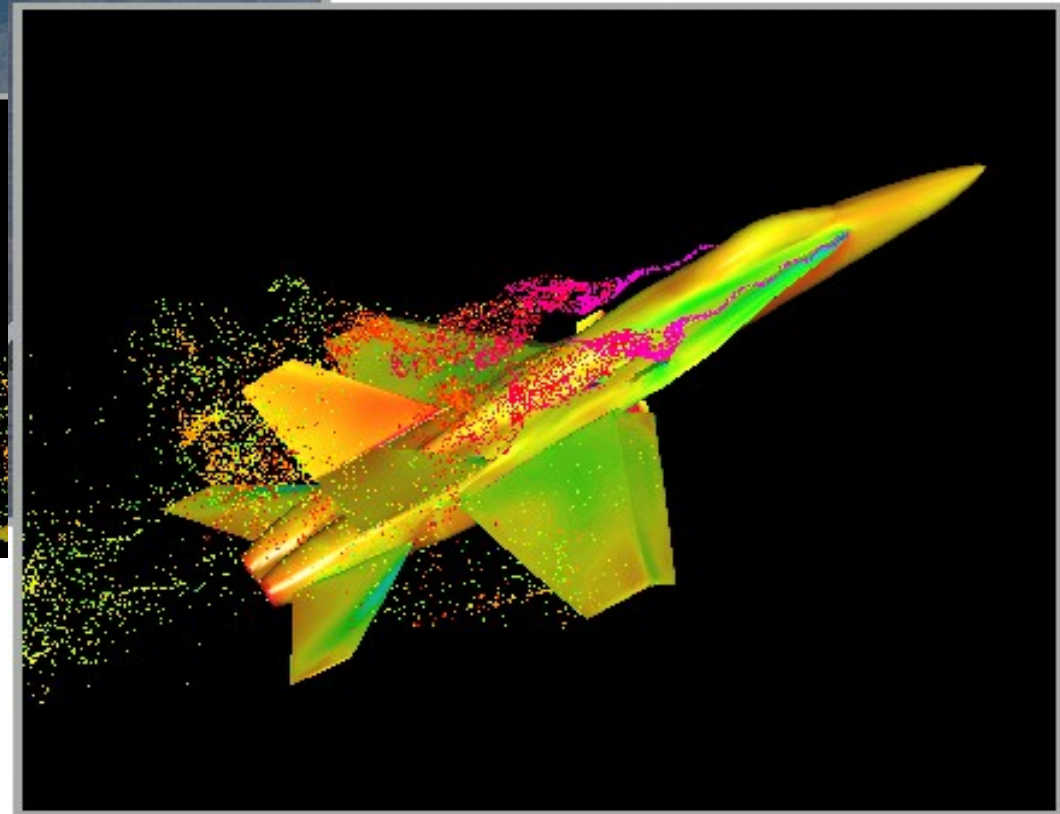
- We often visualize Computational Fluid Dynamics (CFD) simulation data
- CFD: discipline of predicting flow behavior, quantitatively
- data is (often) result of a simulation of flow through or around an object of interest
- some characteristics of CFD data:
 - large, often gigabytes
 - unsteady, time-dependent
 - unstructured, adaptive resolution grids
 - smooth



Comparison with Reality



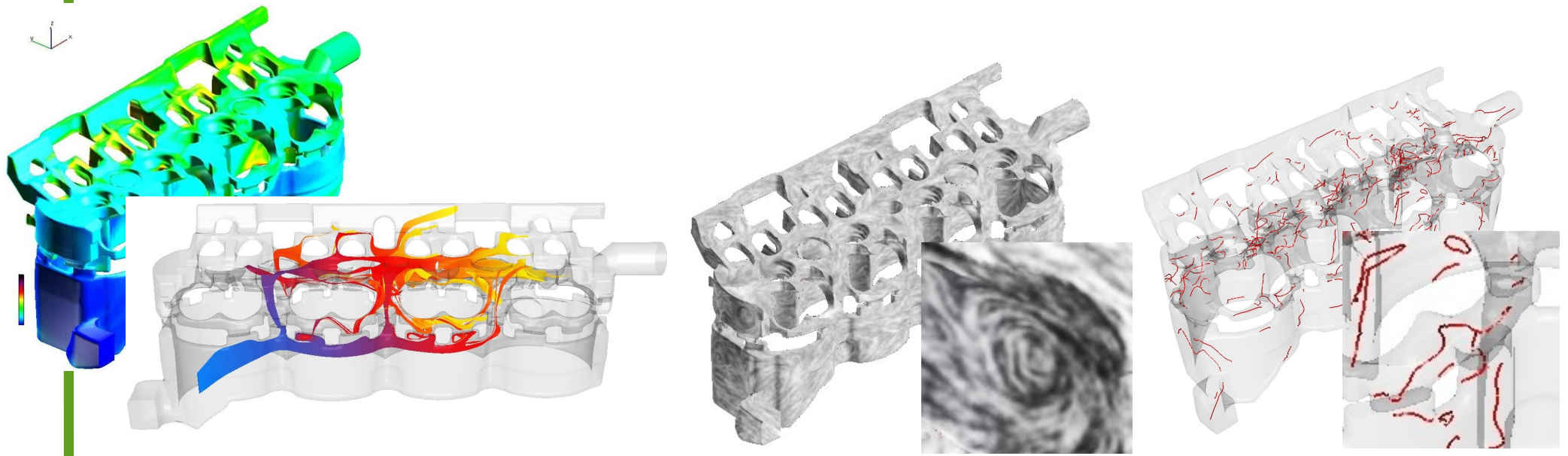
Experiment



Simulation

Flow Visualization Classification

1. **direct:** overview of vector field, minimal computation, e.g. glyphs, color mapping
2. **texture-based:** covers domain with a convolved texture, e.g., Spot Noise, LIC, ISA, IBFV(S)
3. **geometric:** a discrete object(s) whose geometry reflects flow characteristics, e.g. streamlines
4. **feature-based:** both automatic and interactive feature-based techniques, e.g. flow topology



Steady vs. Time-dependent

Steady (time-independent) flows:

- flow itself constant over time
- $\mathbf{v}(\mathbf{x})$, e.g., laminar flows
- simpler case for visualization

Time-dependent (unsteady) flows:

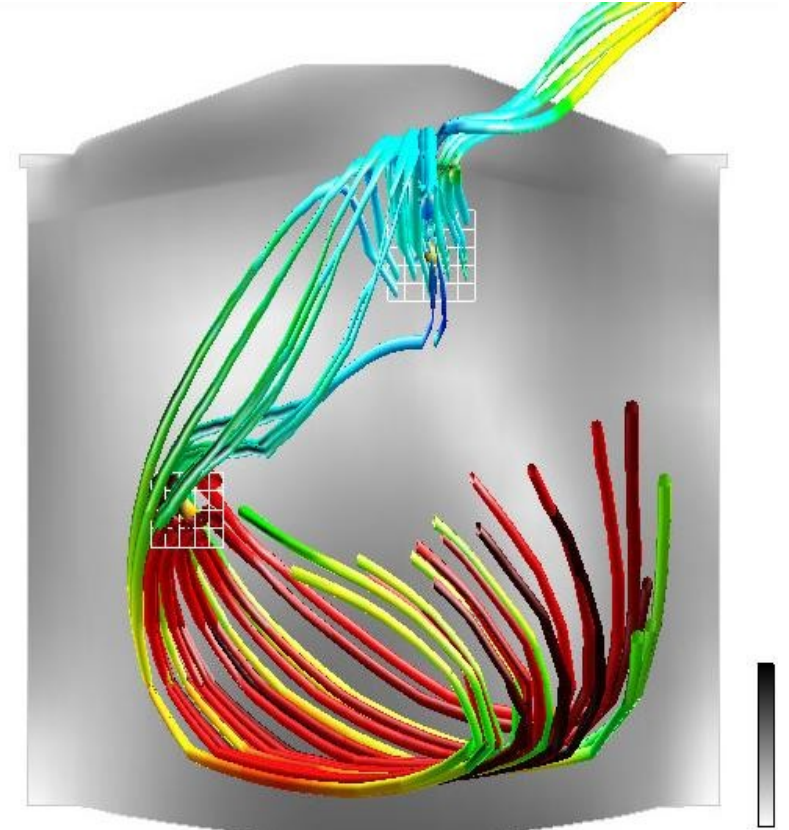
- flow itself changes over time
- $\mathbf{v}(\mathbf{x},t)$, e.g., turbulent flow
- more complex case

Stream, Path, and Streaklines

Terminology:

- **Streamline:** a curve that is everywhere tangent to the flow (release 1 massless particle)
- **Pathline:** a curve that is everywhere tangent to an unsteady flow field (release 1 massless particle)
- **Streakline:** a curve traced by the continues release of particles in unsteady flow from the same position in space (release infinitely many massless particles)

Each is equivalent in steady-state flow



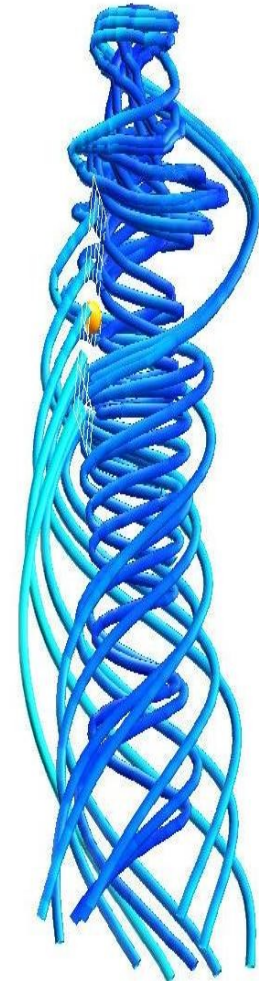
Characteristics of Integral Lines

Advantages:

- **Implementation:** various easy-to-implement streamline tracing algorithms (integration)
- **Intuitive:** interpretation is not difficult
- **Applicability:** generally applicable to all vector fields, also in three-dimensions

Disadvantages:

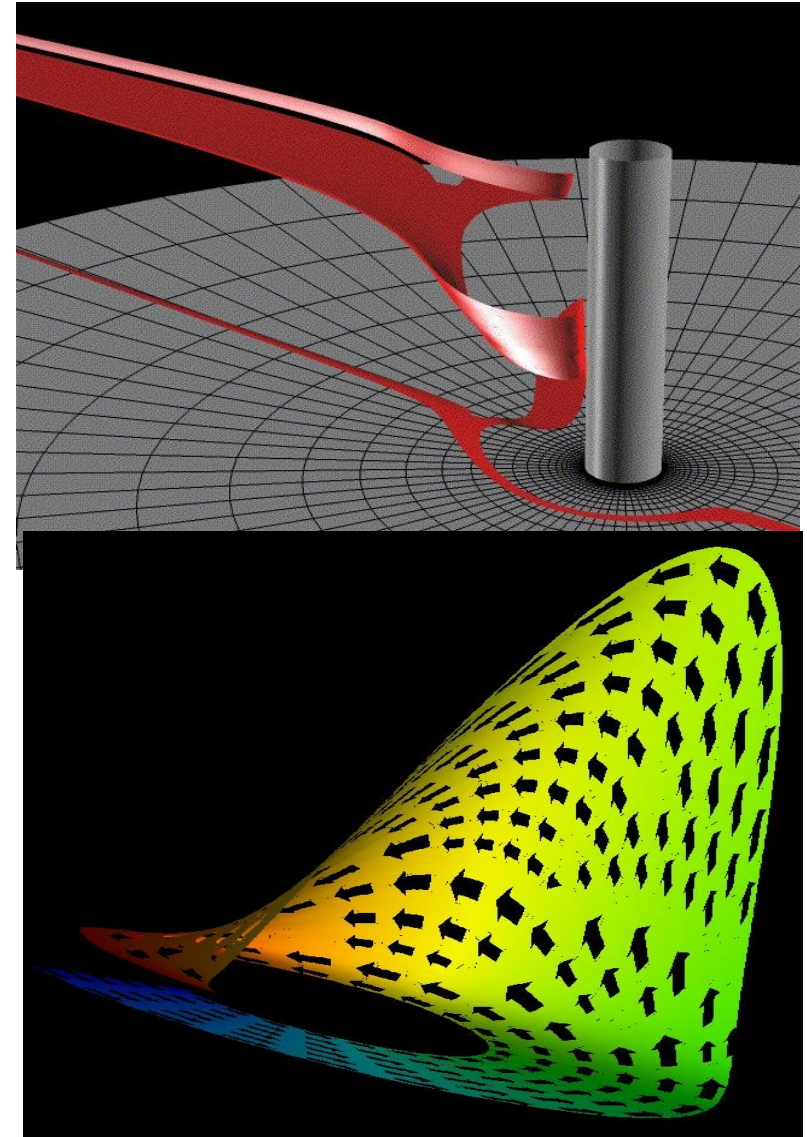
- **Perception:** too many lines can lead to clutter and visual complexity
- **Perception:** depth is difficult to perceive, no well-defined normal vector
- **Seeding:** optimal placement is very challenging (unsolved problem)



Stream Surfaces

Terminology:

- **Stream surface:** a surface that is everywhere tangent to flow
- **Stream surface:** the union of stream lines seeded at all points of a curve (the seed curve)
- Next higher dimensional equivalent to a streamline
- Unsteady flow can be visualized with a **path surface** or **streak surface**



Stream Surfaces

First stream surface computation

- Introduced before SciVis existed
- Early use in flow visualization (Helman and Hesselink 1990) for flow separation

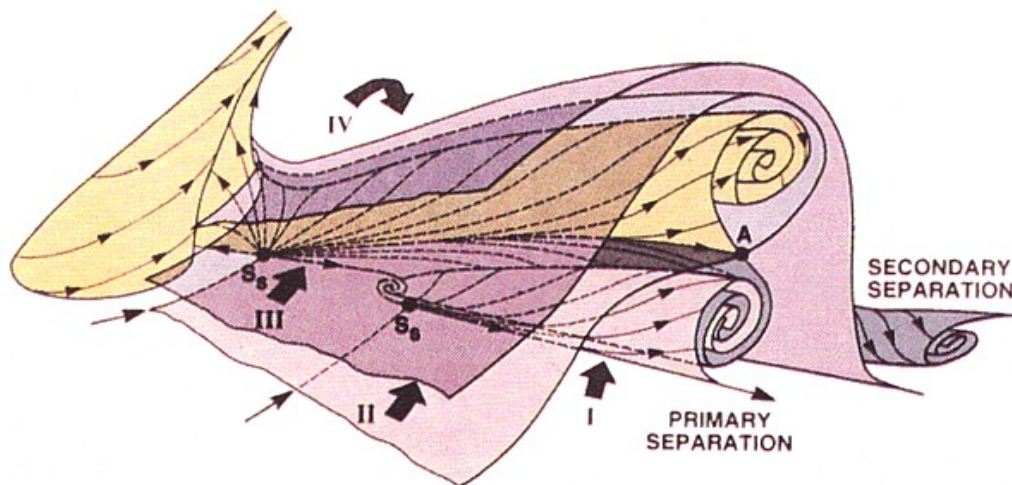


Image: Ying et al.



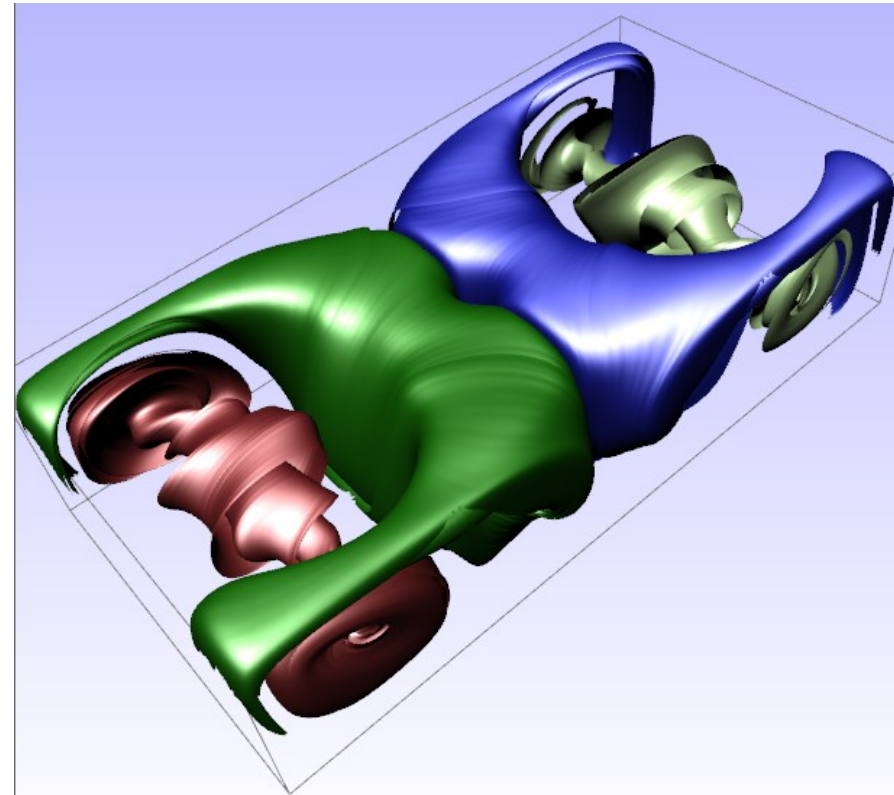
Stream Surfaces: Advantages

Motivation:

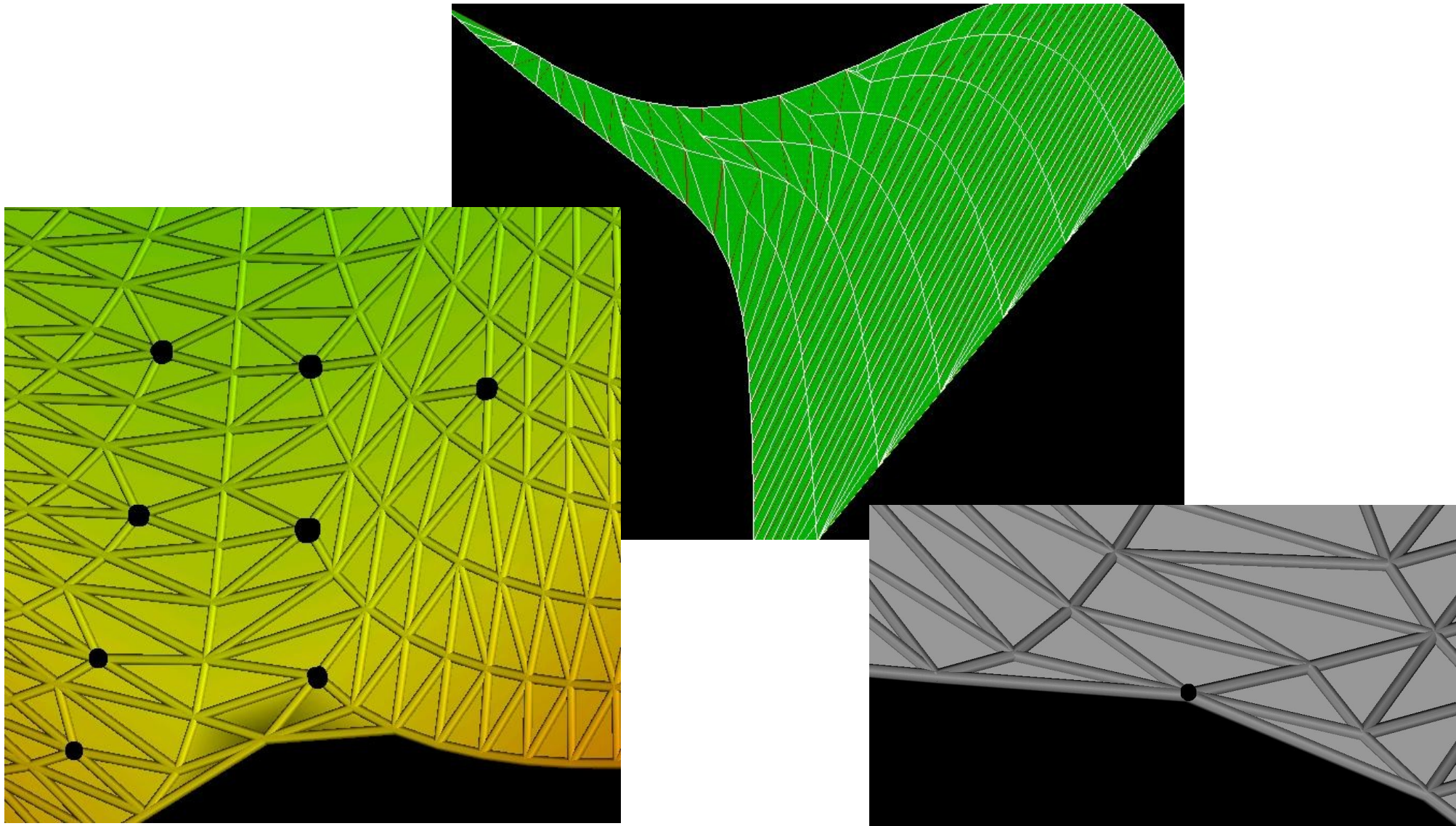
- **Separates (steady) flow:** flow cannot cross surface (stream surfaces only)
- **Perception:** Less visual clutter and complexity than many lines/curves
- **Perception:** well-defined normal vectors make shading easy, improving depth perception
- **Rendering:** surfaces provide more rendering options than lines: e.g., shading and texture-mapping etc.

Disadvantages:

- **Construction/Implementation:** *more complicated algorithms are required to construct integral surfaces*
- **Occlusion:** multiple surfaces hide one another
- **Placement:** placement of surfaces is still and unsolved problem

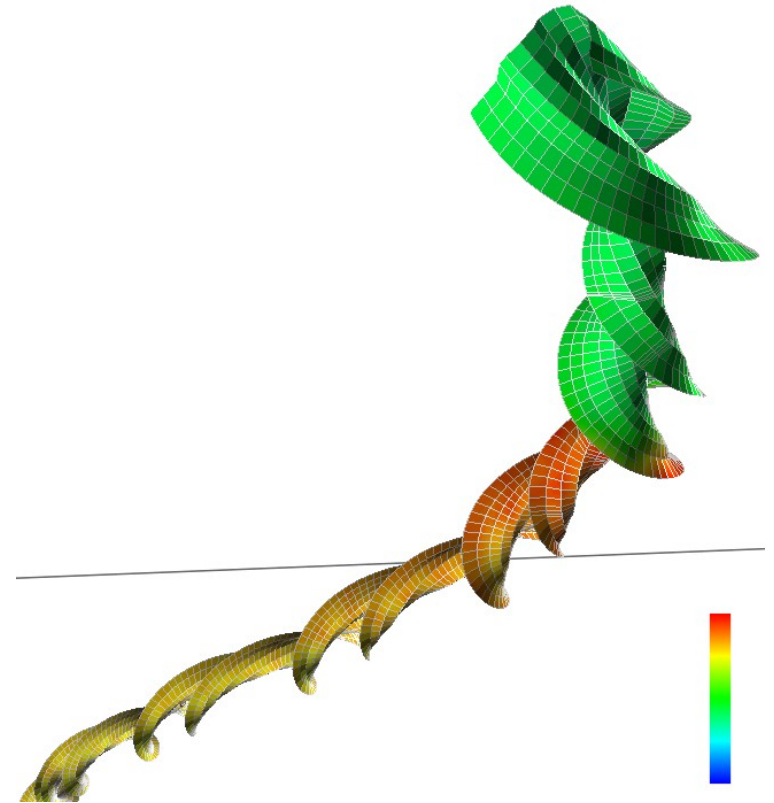


Stream Surfaces – Split / Merge



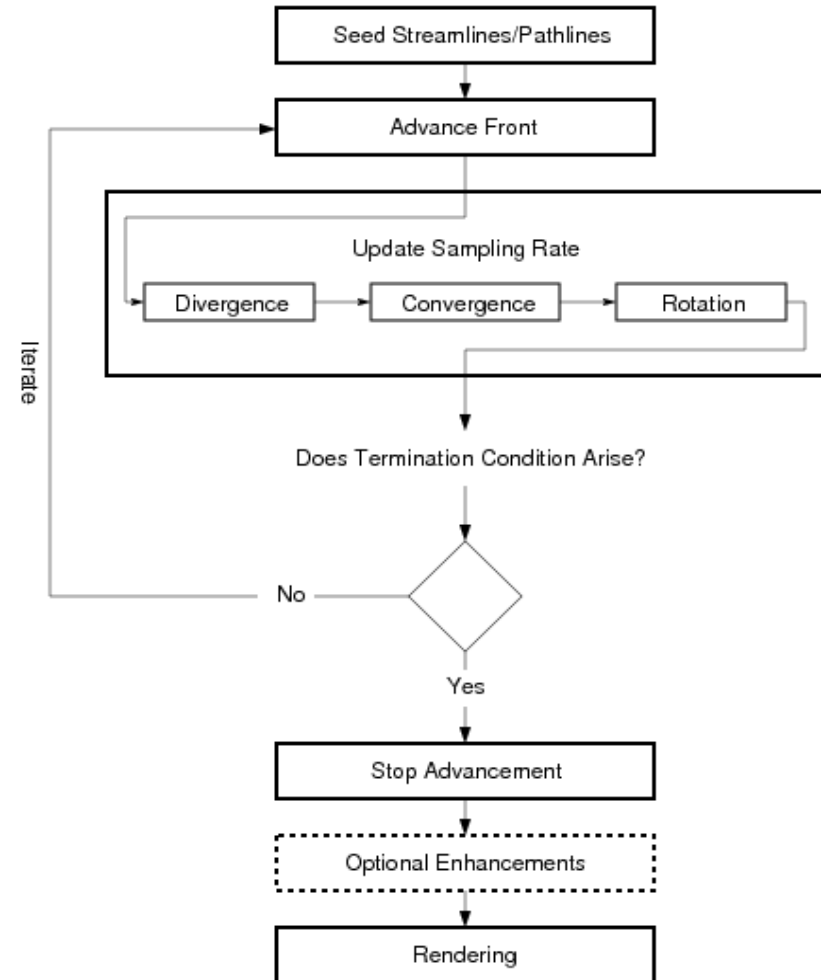
Easy Integral Surfaces

- Relies on use of quad primitives
- Use of local operations (per quad).
- Simple data structure
- Implicit parameterization
- Formulated as a reconstructive sampling of the vector field
 - `d_sample`
 - `d_advance`
 - `d_sep`



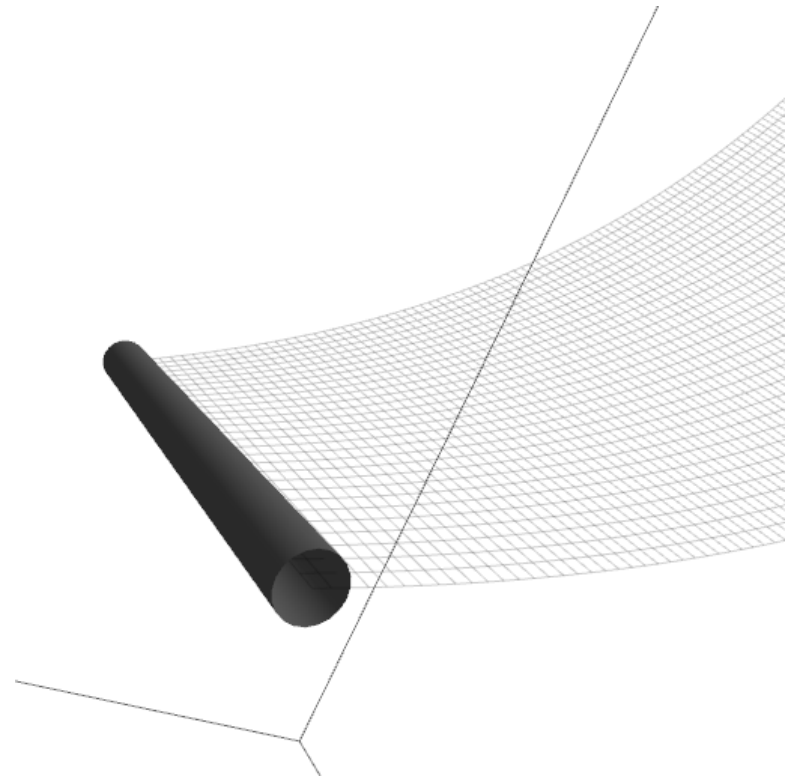
Algorithm Overview

```
Seed;  
While (not terminated)  
    Advance front;  
    Update Sampling Rate;  
End While  
Render;
```



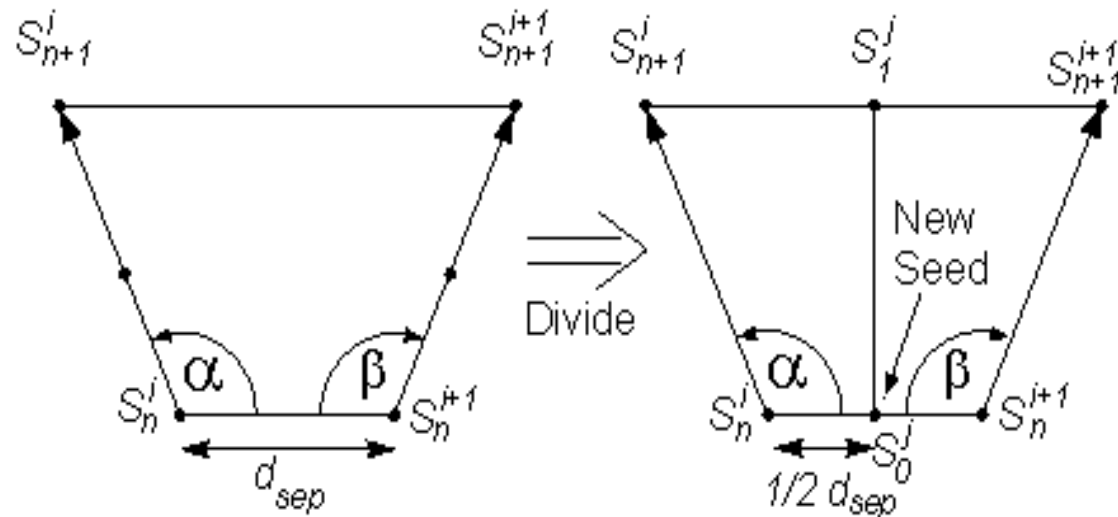
Seeding and Advancement

- Interactive seeding curve:
 - Position and orientation
 - Length
 - Prongs/number of seeds
- Integral surface front advance distance guided by
 - Nyquist rate
 - $0.5 d_{\text{sample}}$



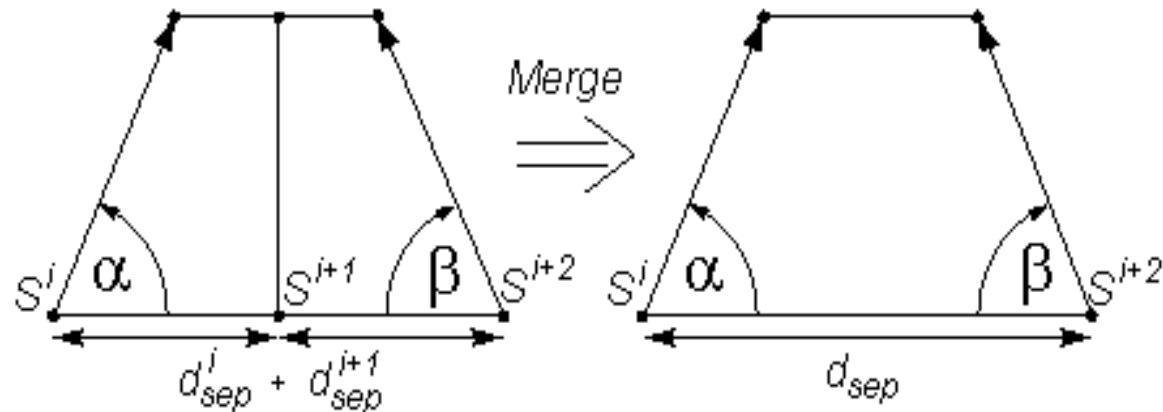
Divergence

- Leads to undersampling
- Depicted by surface widening
- **Detected:** ($\alpha > 90$ AND $\beta > 90$) AND $d_{sep} > d_{sample}$.
- **Solution:** Introduce new vertices into surface.
- Split quad in two



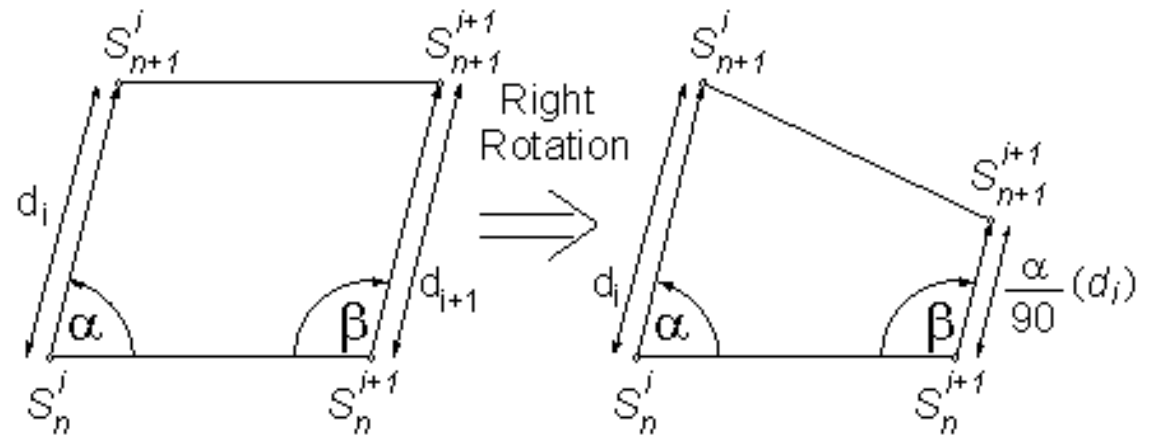
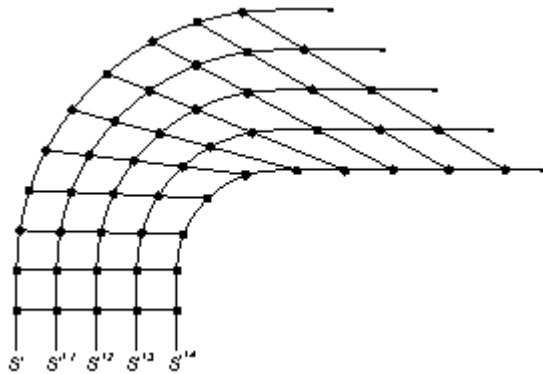
Convergence

- Results in oversampling.
- Surface narrows
- **Detected:** ($\alpha < 90$ AND $\beta < 90$) AND edge length < 0.5 d_{sample}
- **Solution:** Remove vertices from surface
- Merge two quads into a single one



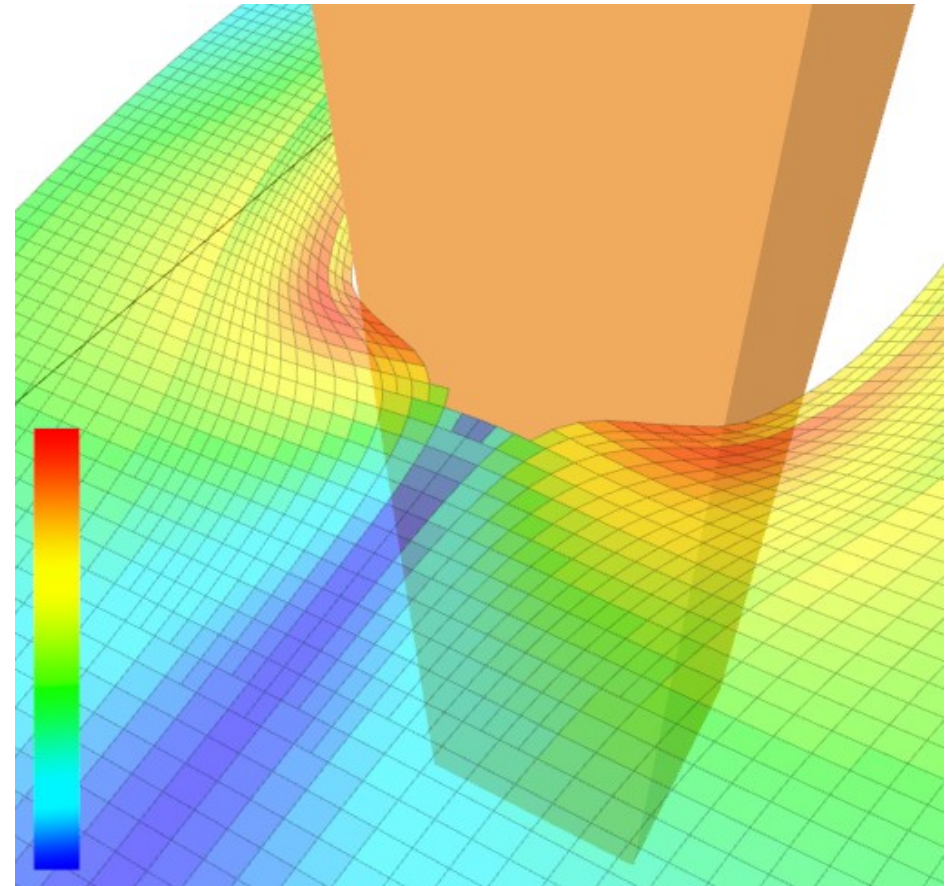
Curvature

- Produces irregular quads.
- **Detected:** ($\alpha < 90$ AND $\beta < 90$) OR ($\alpha > 90$ AND $\beta < 90$).
- **Solution:** Adjust step-size according to angle between segments
- Groups of quads may have to be processed together



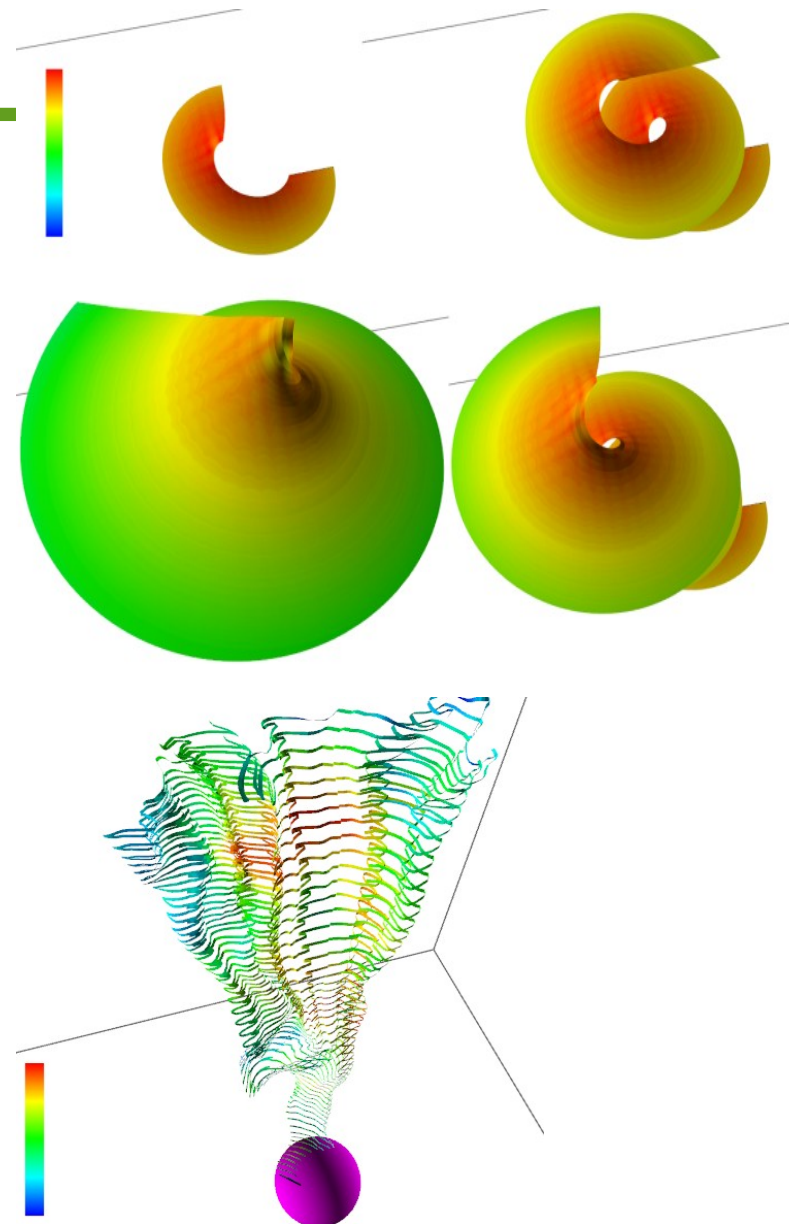
Splitting and Termination

- Surface may split when object boundary encountered
- Separate portions computed independently
- Terminating Conditions:
 - Critical Point (Zero Velocity)
 - Object Intersection
 - Leave Domain
 - Desired geodesic length reached



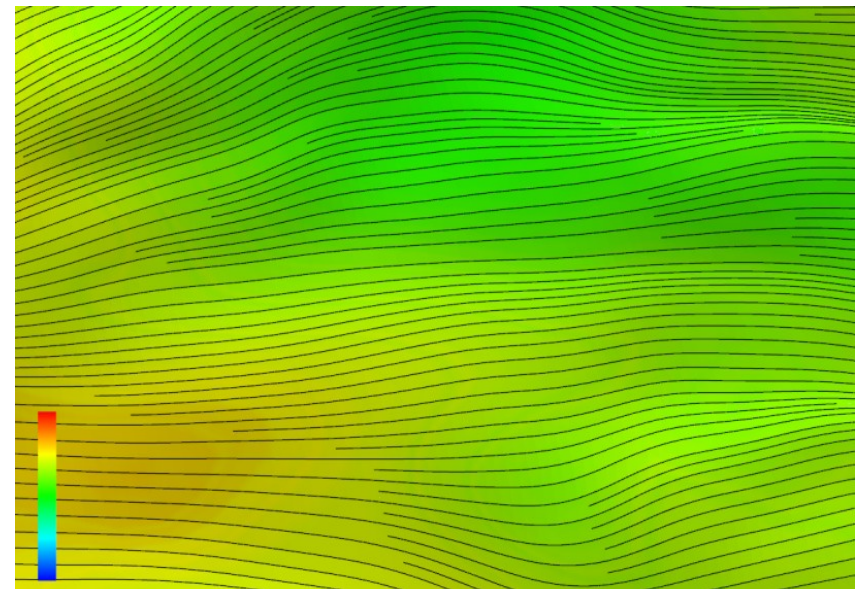
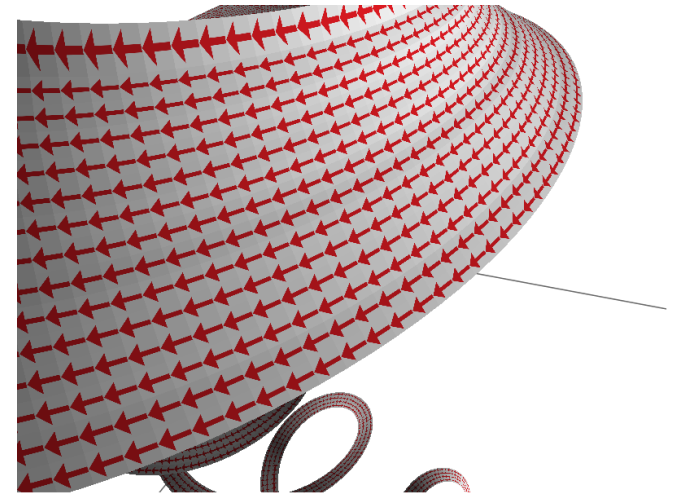
Enhancements

- Surface Painter
 - Helps reduce occlusion
 - User controls the length of surface
- Timelines and Timeribbons
 - Formed from the surface front
 - Turn off the shear operation
 - Velocity magnitude is required



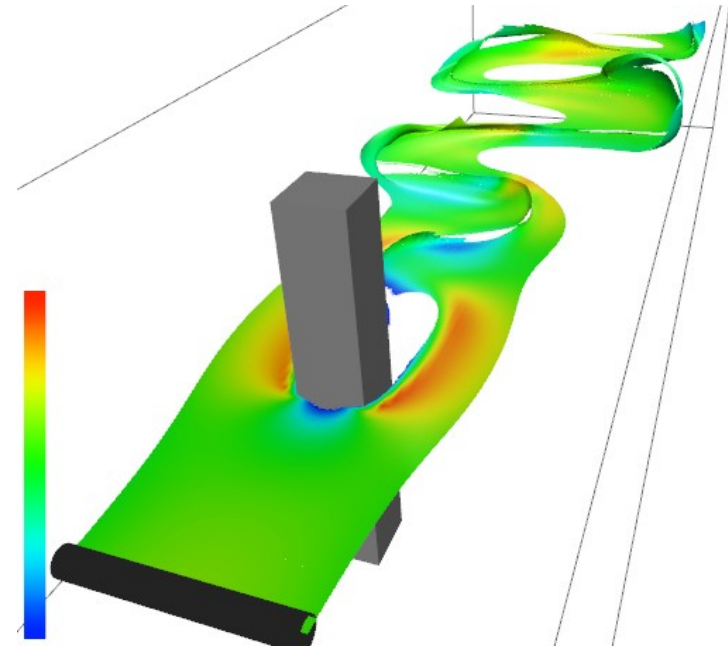
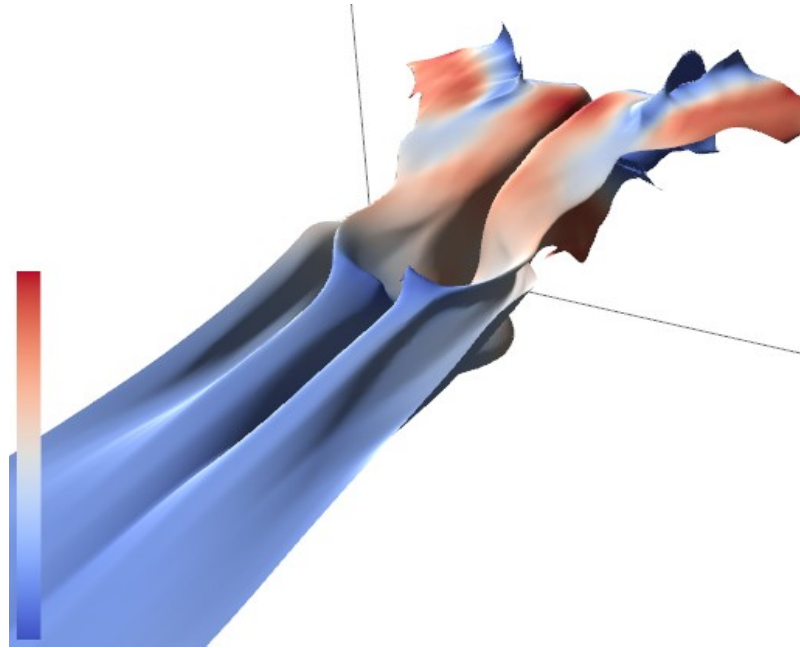
Enhancements

- Stream and Path Arrows
 - Provide information on internal surface structure.
 - Clearly show downstream direction.
- Evenly-spaced flow lines.
 - Stems naturally from convergence and divergence operations.
 - Render flow lines on top of surface.



Stream and Path Surface Results: Video(s)

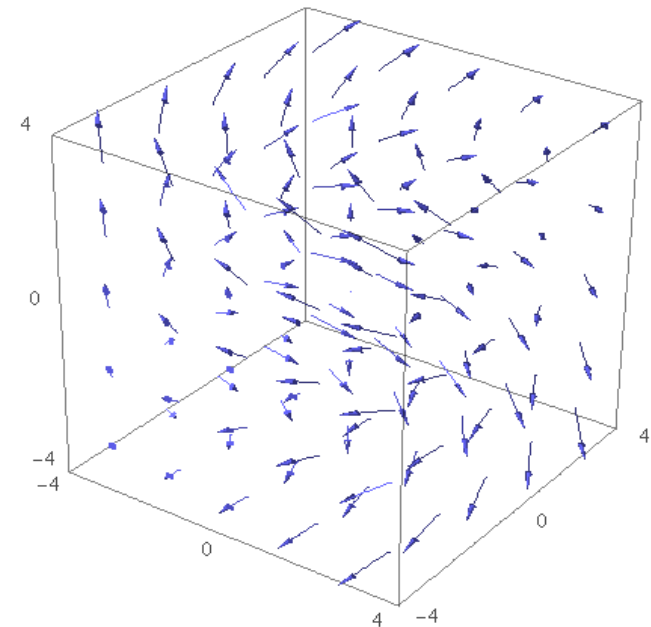
Constructing Streak Surfaces in 3D Unsteady Vector Fields



3D, Unsteady Vector Fields

Discrete locations in 3D space

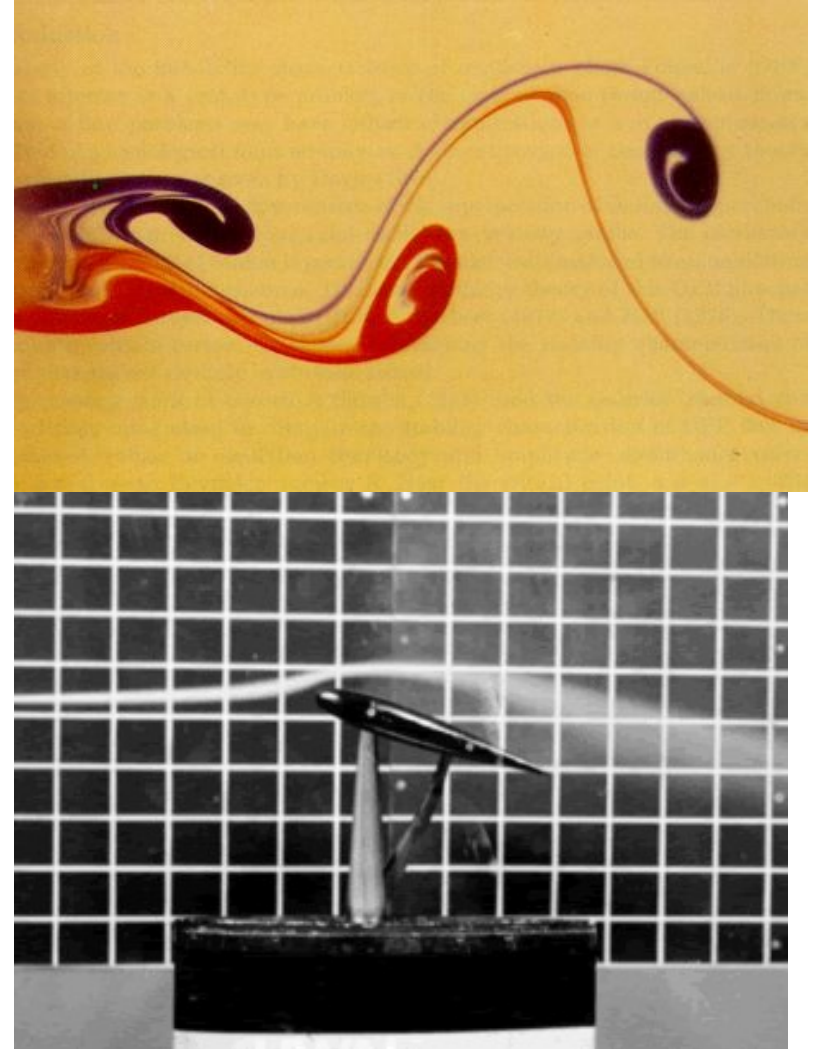
- 4-tuple (4D vector) for each sample
- x-, y-, z-, t- components
- Direction
- Magnitude
- Velocity field when describing the motion of a fluid
- Obtained from CFD simulations or constructed from empirical data
- Unsteady vector fields vary over time



What are Streak Surfaces? Recall:

Terminology

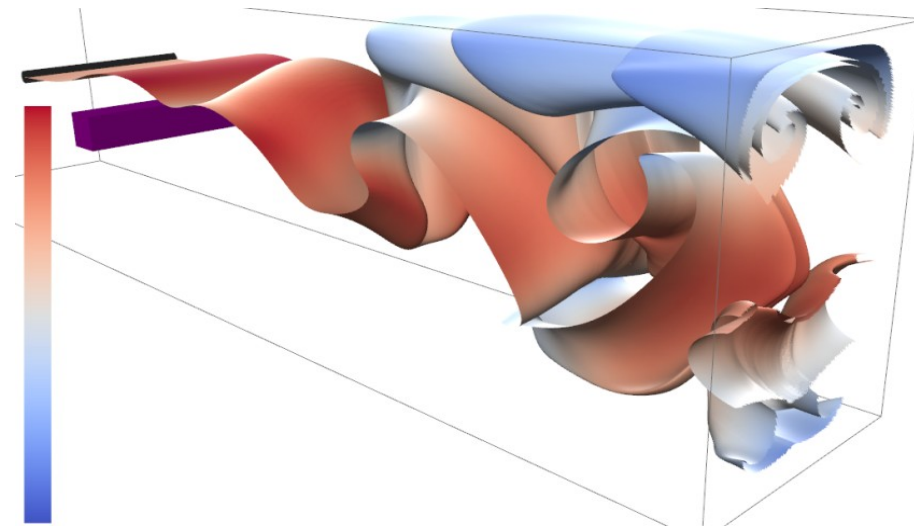
- **Streaklines:** curved formed by joining all particles passing through same point in space (at different times)
- Strong relation to smoke/dye injection from experimental flow visualization.
- **Streak surfaces** are an extension of streak lines (next higher dimension)



Streak Surfaces: Challenges

Challenges:

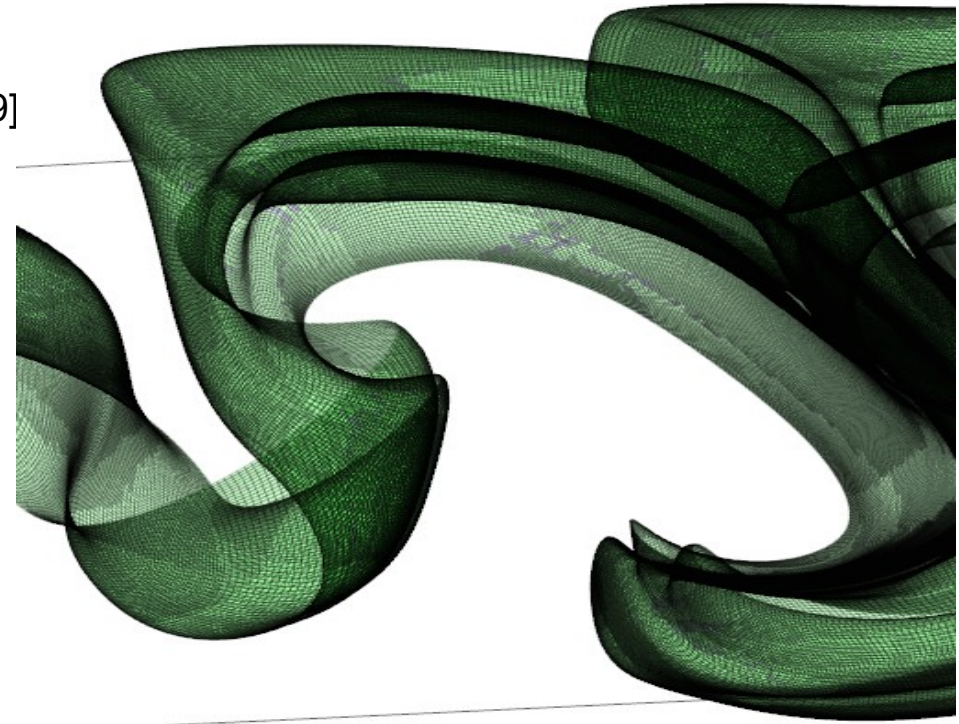
- Computational cost: surface advection is **very** expensive
- Surface completely dynamic: entire surface (all vertices) advect at each time-step
- Mesh quality and maintaining an adequate sampling of the field.
 - Divergence
 - Convergence
 - Shear
- Objects in domain and critical points
- Large size of time-dependent (unsteady) vector field data, out-of-core techniques



Our Method

Properties:

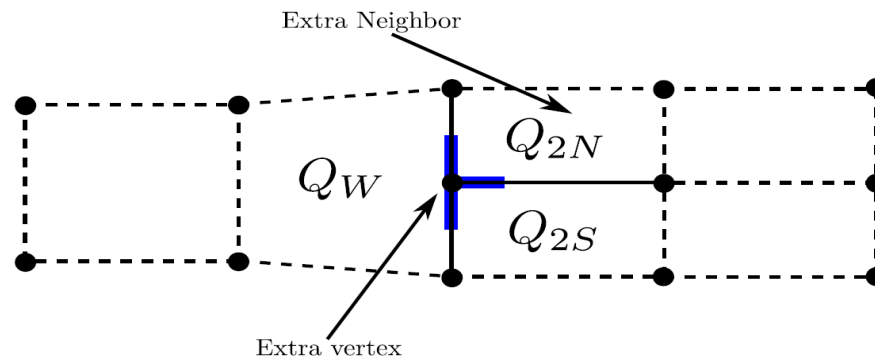
- Surface constructed using quad primitives (as opposed to triangles)
- Local operations for surface refinement performed on a quad-by-quad basis
- No global optimization required
- Allows the construction of large surfaces
- CPU-based for easier implementation
- Fills the gap between methods of Burger et al. [2009] and Krishnan et al. [2009]
 - Not as fast as GPU but interactive
 - Less constraints than GPU implementation – does not need to fit into GPU memory
- Good quality surfaces



Algorithm Data Structures

Data Structures:

- Maintain list of particles
- Particles form vertices that create mesh
- Maintain list of quads
 - Store pointers to vertices
 - Store pointers to all (Quad) neighbors
 - Store T-Junction objects
- Test edge lengths after each integration
- T-junction objects store extra vertex and neighbor information
- Only one T-junction allowed per edge

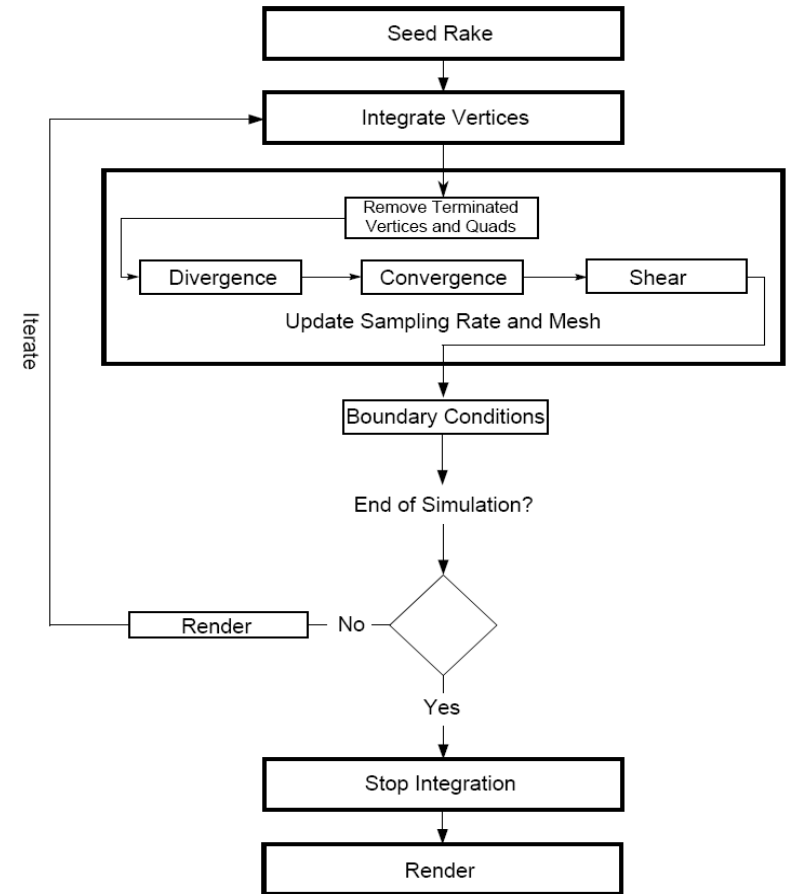


Streak Surface Algorithm Overview

Do:

Position seed with interactive rake

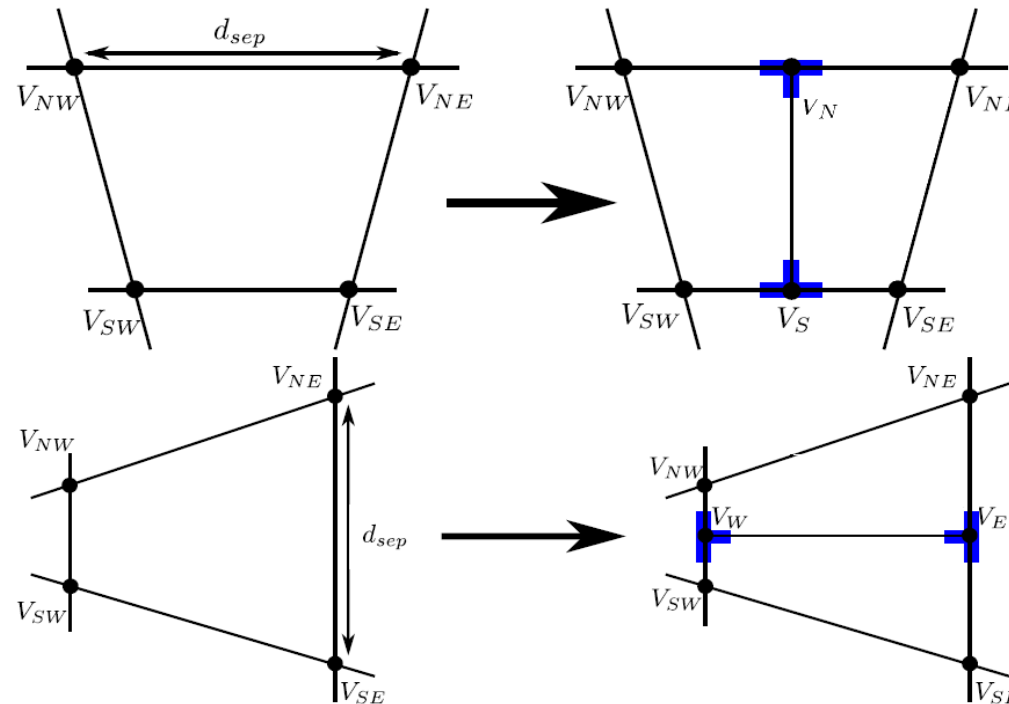
- Iteratively construct surface:
 - Advect surface
 - Refine Surface
 - Test for boundary conditions
 - Update
 - Test for termination criteria
- Final rendering



Divergence

Quad Splitting:

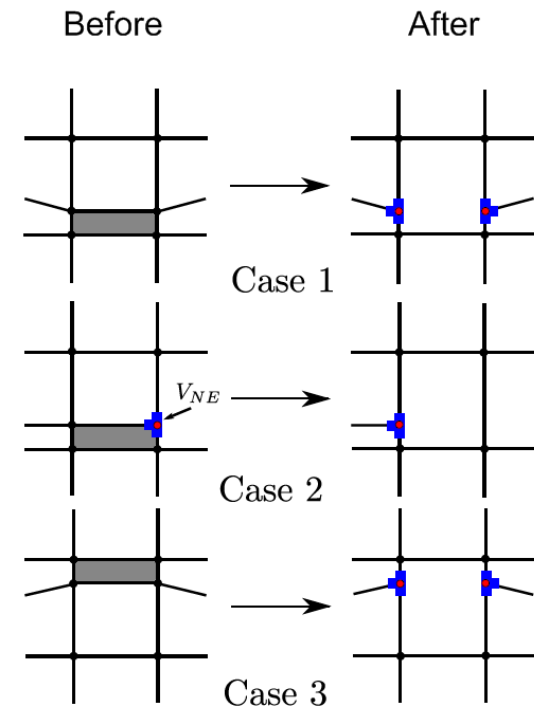
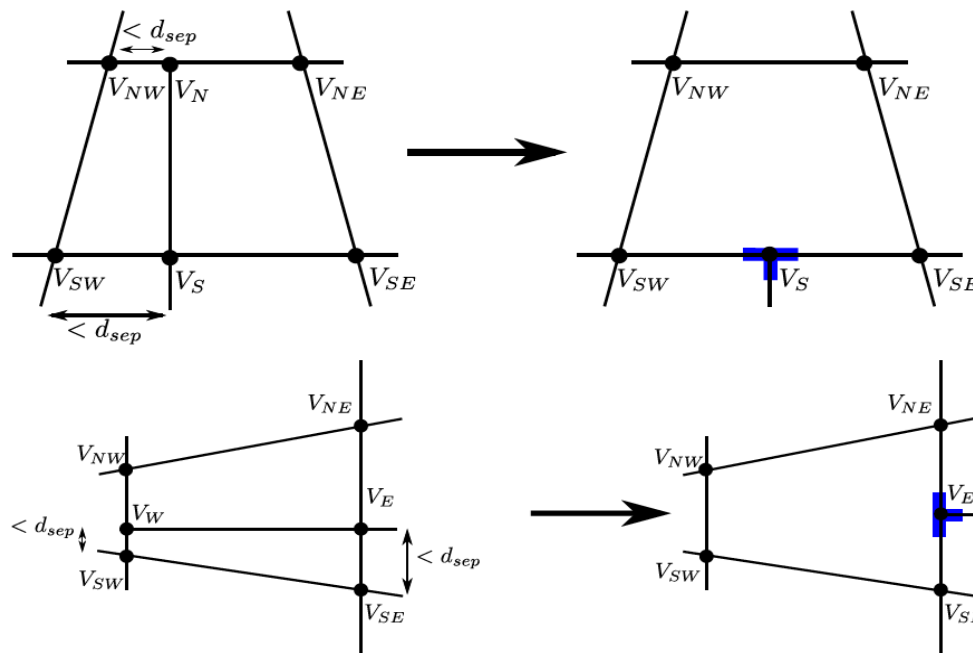
- Occurs when distance between neighbouring particles increases.
- Reduces the sampling of the vector field – may miss features.
- **Introduce new particles – divide the quad.**



Convergence

Quad Collapse:

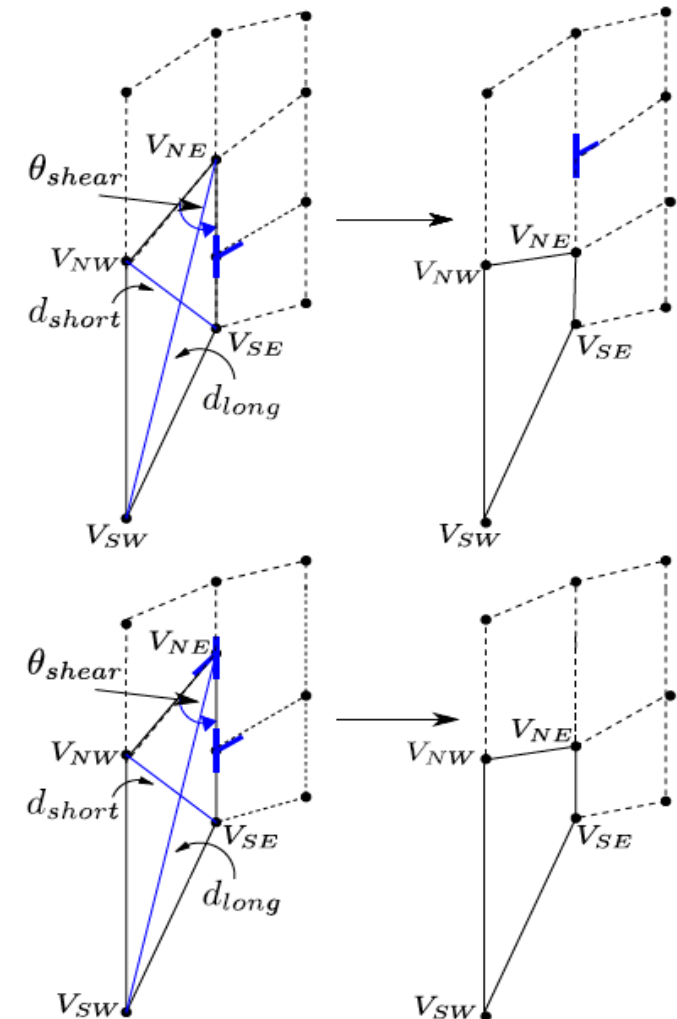
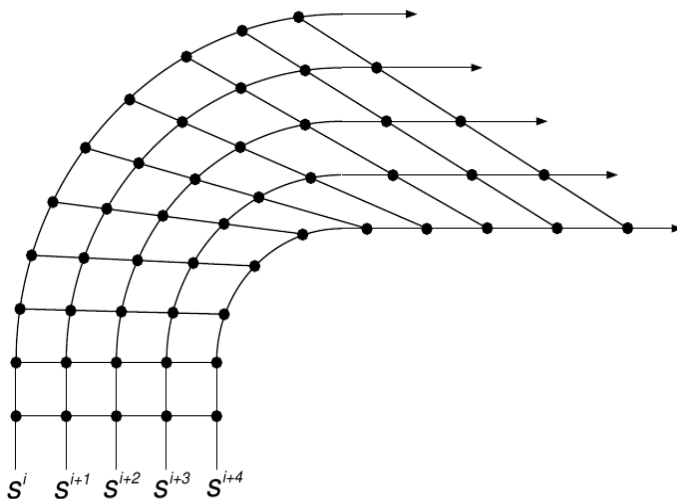
- Occurs when neighbouring particles move closer together.
- Leads to over-sampling, redundant particles and extra computation.
- Test distance between neighboring particles
- **Remove particles from the surface – merge the quad with neighbor.**



Shear

Shear Update:

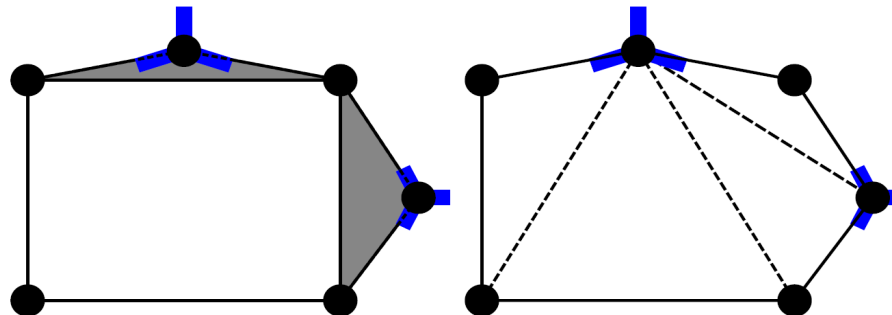
- Can lead to heavily deformed quads
- May lead to errors in checking sampling frequency
- Test the ratio between the quad diagonals
- **Update the mesh connectivity**



T-Junctions and Surface Discontinuities

Create Temporary Triangle Fan:

- Store T-Junction object explicitly
- T-junction vertices may not necessarily lie on neighboring quads edge
- If ignored cracks can form in the surface
- **Render the quad using a triangle fan**
 - Ensures whole surface is tessellated



Streak Surface Results: Video

Summary and Conclusions

- We claim surfaces offer advantages over traditional curves when visualizing 3D and 4D flow
- We present interactive algorithms for construction of stream, path and streak surfaces
- Algorithms are based on local operations performed on quads for mesh refinement
- Technique handles divergence, convergence and shear flow
- Splitting of surface to adapt to flow around object boundaries
- Demonstrated on a variety of data sets

Acknowledgements

Thank you for your attention! Any questions?

We thank the following for material used in this lecture:

- Christoph Garth
- Helwig Hauser
- **Tony McLoughlin**
- Ronny Peikert
- Juergen Schneider
- Eugene Zhang



This work was partially funded by EPSRC Grant EP/F002335/1