

G52MAL Machines and Their Languages Lecture 12

Disambiguating Context-Free Grammars

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Recap: Ambiguity (1)

A CFG $G = (N, T, P, S)$ is **ambiguous** if there is at least one word $w \in L(G)$ such that there are

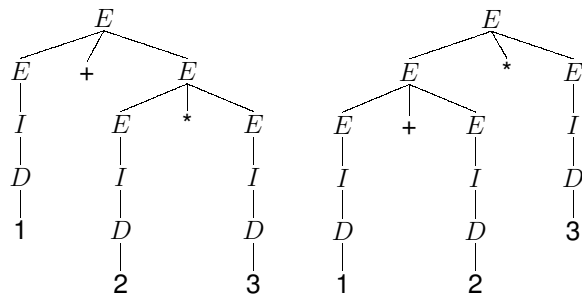
- two different **derivation trees**, or
- two different **left-most derivations**, or
- two different **right-most derivations**

for w .

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Recap: Ambiguity (4)

Consider: $1 + 2 * 3$. Two derivation trees:



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Recap: Derivation Trees (1)

A tree is a **derivation tree** for a CFG $G = (N, T, P, S)$ iff

1. Every node has a label from $N \cup T \cup \{\epsilon\}$.
2. The label of the root node is S .
3. Labels of interior nodes belong to N .
4. If a node n has label A and nodes n_1, n_2, \dots, n_k are children of n , from left to right, with labels X_1, X_2, \dots, X_k , respectively, then $A \rightarrow X_1X_2 \dots X_k$ is a production in P .
5. If a node n has label ϵ , then n is a leaf and the only child of its parent.

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Recap: Ambiguity (2)

Ambiguity can be problematic for a number of reasons, including that the structure of a derivation tree often is used to suggest a **meaning** for the word.

Example: Arithmetic Expressions

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Disambiguating Grammars

Given an ambiguous grammar G , it is often possible to construct an **equivalent** grammar G' (i.e., $L(G) = L(G')$), such that G' is **not** ambiguous.

Some languages are **inherently ambiguous** CFLs, meaning that every CFG generating the language necessarily is ambiguous.

We will consider exploiting

- Operator Precedence
- Associativity

to disambiguate expression grammars as an example.

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Recap: Derivation Trees (2)

- The string of **leaf labels** read from left to right, eliding any ϵ , constitute the **yield** of the tree.
- For a CFG $G = (N, T, P, S)$, a string $\alpha \in (N \cup T)^*$ is the yield of some derivation tree iff $S \xrightarrow{*}_G \alpha$.

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Recap: Ambiguity (3)

$SAE = (N = \{E, I, D\}, T = \{+, *, (,), 0, 1, \dots, 9\}, P, E)$ where P is given by:

$$\begin{aligned} E &\rightarrow E + E \\ &\quad | E * E \\ &\quad | (E) \\ &\quad | I \\ I &\rightarrow DI | D \\ D &\rightarrow 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 \end{aligned}$$

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