

# G53CMP: Lecture 12 & 13

## *Code Generation II*

Henrik Nilsson

University of Nottingham, UK

# Code Generation: Demo I

Let us generate code for:

```
let
  var f: Integer := 1;
  var i: Integer := 1
in
  while i <= 10 do begin
    f := f * i;
    putint(f);
    i := i + 1
  end
```

# Code Generation: Demo II (1)

And for this program using arrays and a procedure:

```
let
  proc swap(var x: Integer, var y: Integer)
    let
      var t: Integer
    in begin
      t := x; x := y; y := t
    end;
  var a: Integer[5] := [7, 3, 1, 9, 2];
  var i: Integer;
  var j: Integer
```

# Code Generation: Demo II (2)

```
in begin
  i := 0;
  while i < 4 do begin
    j := i + 1;
    while j < 5 do begin
      if a[i] > a[j] then
        swap(a[i], a[j])
      else skip();
      j := j + 1
    end;
    i := i + 1
  end;
end;
```

# Code Generation: Demo II (3)

```
i := 0;
while i <= 4 do begin
    putint(a[i]);
    i := i + 1
end
end
```

# Specifying Code Selection (1)

- Code selection is specified *inductively* over the phrases of the source language:

$$\begin{array}{l} \textit{Command} \quad \rightarrow \quad \underline{\textit{Identifier}} := \textit{Expression} \\ \quad \quad \quad | \quad \textit{Command} ; \textit{Command} \\ \quad \quad \quad \dots \end{array}$$

# Specifying Code Selection (1)

- Code selection is specified **inductively** over the phrases of the source language:

$$\begin{array}{l} \textit{Command} \rightarrow \underline{\textit{Identifier}} := \textit{Expression} \\ \quad \quad \quad | \quad \textit{Command} ; \textit{Command} \\ \quad \quad \quad \dots \end{array}$$

- Code Function**: maps a source phrase to an instruction sequence. For example:

$$\begin{array}{l} \textit{execute} : \textit{Command} \rightarrow \textit{Instruction}^* \\ \textit{evaluate} : \textit{Expression} \rightarrow \textit{Instruction}^* \\ \textit{elaborate} : \textit{Declaration} \rightarrow \textit{Instruction}^* \end{array}$$

# Specifying Code Selection (2)

Note:



# Specifying Code Selection (2)

Note:

- *execute* **generates code** for executing a command (it does not execute a command directly);

# Specifying Code Selection (2)

Note:

- *execute* **generates code** for executing a command (it does not execute a command directly);
- *evaluate* **generates code** for evaluating an expression, leaving the result on the top of the stack.

# Specifying Code Selection (2)

Note:

- *execute* **generates code** for executing a command (it does not execute a command directly);
- *evaluate* **generates code** for evaluating an expression, leaving the result on the top of the stack.
- *elaborate* **generates code** for reserving storage for declared constants and variables, evaluating any initialisation expressions, and for declared procedures and functions.

# Specifying Code Selection (3)

- Code functions are specified by means of **code templates**:

$$\text{execute } [ C_1 \ ; \ C_2 ] =$$
$$\text{execute } C_1$$
$$\text{execute } C_2$$

# Specifying Code Selection (3)

- Code functions are specified by means of **code templates**:

*execute*  $\llbracket C_1 ; C_2 \rrbracket =$   
*execute*  $C_1$   
*execute*  $C_2$

- The brackets  $\llbracket$  and  $\rrbracket$  enclose pieces of **concrete syntax** and **meta variables**.

# Specifying Code Selection (3)

- Code functions are specified by means of **code templates**:

$execute \llbracket C_1 ; C_2 \rrbracket =$

$execute C_1$

$execute C_2$

- The brackets  $\llbracket$  and  $\rrbracket$  enclose pieces of **concrete syntax** and **meta variables**.
- Note the **recursion**; i.e. inductive definition over the underlying phrase structure.

# Specifying Code Selection (3)

- Code functions are specified by means of **code templates**:

$execute \llbracket C_1 ; C_2 \rrbracket =$

$execute C_1$

$execute C_2$

- The brackets  $\llbracket$  and  $\rrbracket$  enclose pieces of **concrete syntax** and **meta variables**.
- Note the **recursion**; i.e. inductive definition over the underlying phrase structure.

(Think of  $\llbracket \cdot \rrbracket$  as a map from concrete to abstract syntax as specified by the abstract syntax grammars.)

# Specifying Code Selection (4)

In a simple language, the code template for assignment might be:

$$\begin{aligned} \text{execute } \llbracket I := E \rrbracket = \\ \text{evaluate } E \\ \text{STORE } \text{addr}(I) \end{aligned}$$

where

$$\text{addr} : \text{Identifier} \rightarrow \text{Address}$$



# Specifying Code Selection (4)

In a simple language, the code template for assignment might be:

$$\begin{aligned} \text{execute } \llbracket I := E \rrbracket = \\ \text{evaluate } E \\ \text{STORE } \text{addr}(I) \end{aligned}$$

where

$$\text{addr} : \text{Identifier} \rightarrow \text{Address}$$

Note that the instruction sequences and individual instructions in the RHS of the defining equation are implicitly **concatenated**.

# Specifying Code Selection (4)

In a simple language, the code template for assignment might be:

$$\begin{aligned} \text{execute } \llbracket I := E \rrbracket = \\ \text{evaluate } E \\ \text{STORE } \text{addr}(I) \end{aligned}$$

where

$$\text{addr} : \text{Identifier} \rightarrow \text{Address}$$

Note that the instruction sequences and individual instructions in the RHS of the defining equation are implicitly **concatenated**.

Note: meta variables range over **abstract syntax**.

# Exercise: Code Templates

Generate code for the fragment

```
f := f * n;  
n := n - 1
```

using the following two templates:

$$\begin{array}{l} \textit{execute} \llbracket C_1 ; C_2 \rrbracket = \\ \textit{execute} C_1 \\ \textit{execute} C_2 \end{array} = \begin{array}{l} \textit{execute} \llbracket I := E \rrbracket = \\ \textit{evaluate} E \\ \text{STORE } \textit{addr}(I) \end{array}$$

and  $\textit{addr}(f) = [\text{SB} + 11]$ ,  $\textit{addr}(n) = [\text{SB} + 17]$ .

Expand as far as the above templates allow.

# Not Quite that Simple ...

However, something is clearly missing! Recall:

*execute* : *Command*  $\rightarrow$  *Instruction*\*

*evaluate* : *Expression*  $\rightarrow$  *Instruction*\*

*elaborate* : *Declaration*  $\rightarrow$  *Instruction*\*

*addr* : *Identifier*  $\rightarrow$  *Address*

and consider again:

*execute*  $\llbracket I := E \rrbracket =$

*evaluate* *E*

STORE *addr*(*I*)

# Not Quite that Simple ...

However, something is clearly missing! Recall:

*execute* : *Command*  $\rightarrow$  *Instruction*\*

*evaluate* : *Expression*  $\rightarrow$  *Instruction*\*

*elaborate* : *Declaration*  $\rightarrow$  *Instruction*\*

*addr* : *Identifier*  $\rightarrow$  *Address*

and consider again:

*execute*  $\llbracket I := E \rrbracket =$

*evaluate* *E*

STORE *addr*(*I*)

**How can the function *addr* possibly map an identifier (a name) to an address?**

- 
- 
- 

# Not Quite that Simple ... (2)

In more detail:

# Not Quite that Simple ... (2)

In more detail:

- *elaborate* is responsible for **assigning** addresses to variables

# Not Quite that Simple ... (2)

In more detail:

- *elaborate* is responsible for **assigning** addresses to variables
- a function like *addr* needs **access** to the addresses assigned by *elaborate*



# Not Quite that Simple ... (2)

In more detail:

- *elaborate* is responsible for **assigning** addresses to variables
- a function like *addr* needs **access** to the addresses assigned by *elaborate*
- but the given type signatures for the code functions do **not permit** this communication!

- 
- 
- 

# Not Quite that Simple ... (3)

Consequently:

# Not Quite that Simple ... (3)

Consequently:

- The code functions need an additional ***stack environment argument***, associating variables with addresses.

# Not Quite that Simple ... (3)

Consequently:

- The code functions need an additional **stack environment argument**, associating variables with addresses.
- The code function *elaborate* must **return an updated stack environment**.

# Not Quite that Simple ... (3)

Consequently:

- The code functions need an additional **stack environment argument**, associating variables with addresses.
- The code function *elaborate* must **return an updated stack environment**.
- Need to keep track of the **current stack depth** (with respect to `LB`) to allow *elaborate* to determine the address (within activation record) for a new variable.

# Not Quite that Simple ... (5)

- Need to keep track of the current scope level as the difference of current scope level and the scope level of a variable is needed in addition to its address to access it (see later lecture on run-time organisation and *static links*).

# Not Quite that Simple ... (5)

- Need to keep track of the current scope level as the difference of current scope level and the scope level of a variable is needed in addition to its address to access it (see later lecture on run-time organisation and *static links*).

Moreover, need to generate *fresh names* for jump targets (recall the demo).

# Not Quite that Simple ... (6)

To clearly convey the basic ideas first, we will:

- Use simplified MiniTriangle as main example:
  - No user-defined procedures or functions (only predefined, global ones).
  - Consequently, all variables are global (addressed with respect to  $SB$ ).
  - No arrays (only simple variables, all of size 1 word) .
- Gloss over the bookkeeping details for the most part.



# Not Quite that Simple ... (7)

However:

- Additional details will be given occasionally.
- Will revisit at appropriate points in lectures on run-time organisation.
- Refer to the HMTC (coursework compiler) source code for full details.

# Code Functions for MiniTriangle

In the simplified exposition, we can consider the code functions to have the following types:

$run : Program \rightarrow Instruction^*$

$execute : Command \rightarrow Instruction^*$

$execute^* : Command^* \rightarrow Instruction^*$

$evaluate : Expression \rightarrow Instruction^*$

$evaluate^* : Expression^* \rightarrow Instruction^*$

$fetch : Identifier \rightarrow Instruction^*$

$assign : Identifier \rightarrow Instruction^*$

$elaborate : Declaration \rightarrow Instruction^*$

$elaborate^* : Declaration^* \rightarrow Instruction^*$

# A Code Generation Monad

HMTC uses a *Code Generation monad* to facilitate some of the bookkeeping:

```
instance Monad (CG instr)
```

# A Code Generation Monad

HMTC uses a *Code Generation monad* to facilitate some of the bookkeeping:

```
instance Monad (CG instr)
```

Takes care of:

- Collation of generated instructions
- Generation of fresh names

# A Code Generation Monad

HMTC uses a *Code Generation monad* to facilitate some of the bookkeeping:

```
instance Monad (CG instr)
```

Takes care of:

- Collation of generated instructions
- Generation of fresh names

Typical operations:

- `emit :: instr -> CG instr ()`
- `newName :: CG instr Name`

# Some HMTC Code Functions

```
execute :: Level -> CGEnv -> Depth -> Command  
        -> CG TAMInst ()
```

```
evaluate :: Level -> CGEnv -> Expression  
        -> CG TAMInst ()
```

```
elaborateDecls :: Level -> CGEnv -> Depth  
              -> [Declaration]  
              -> CG TAMInst (CGEnv, Depth)
```

(In essence: actual signatures differ in minor ways.)

# MiniTriangle Abstract Syntax Part I

(Simplified: no procedures, functions, arrays)

<i>Program</i>	→	<i>Command</i>	Program
<i>Command</i>	→	<u><i>Identifier</i></u> := <i>Expression</i>	CmdAssign
		<u><i>Identifier</i></u> ( <i>Expression</i> * )	CmdCall
		<b>begin</b> <i>Command</i> * <b>end</b>	CmdSeq
		<b>if</b> <i>Expression</i> <b>then</b> <i>Command</i>	CmdIf
		<b>else</b> <i>Command</i>	
		<b>while</b> <i>Expression</i> <b>do</b> <i>Command</i>	CmdWhile
		<b>let</b> <i>Declaration</i> * <b>in</b> <i>Command</i>	CmdLet

# Meta Variable Conventions

$C \in \textit{Command}$

$Cs \in \textit{Command}^*$

$E \in \textit{Expression}$

$Es \in \textit{Expression}^*$

$D \in \textit{Declaration}$

$Ds \in \textit{Declaration}^*$

$I \in \textit{Identifier}$

$O \in \textit{Operator}$

$IL \in \textit{IntegerLiteral}$

$TD \in \textit{TypeDenoter}$



# Code Function *execute* (1)

$run : \text{Program} \rightarrow \text{Instruction}^*$

$execute : \text{Command} \rightarrow \text{Instruction}^*$

$run \llbracket C \rrbracket =$   
 $execute\ C$   
 $\text{HALT}$

$execute \llbracket I := E \rrbracket =$   
 $evaluate\ E$   
 $assign\ I$

# Code Function *execute* (2)

$$\begin{aligned} \text{execute } \llbracket I ( Es ) \rrbracket &= \\ &\text{evaluate}^* Es \\ &\text{CALL } \text{addr}(I) \end{aligned}$$
$$\begin{aligned} \text{execute } \llbracket \text{begin } Cs \text{ end} \rrbracket &= \\ &\text{execute}^* Cs \end{aligned}$$

# Code Function *execute* (3)

$$\begin{aligned} \text{execute } \llbracket \text{if } E \text{ then } C_1 \text{ else } C_2 \rrbracket = & \\ & \text{evaluate } E \\ & \text{JUMP IFZ } g \\ & \text{execute } C_1 \\ & \text{JUMP } h \\ & g : \text{execute } C_2 \\ & h : \end{aligned}$$

where  $g$  and  $h$  are **fresh** names.

# Exercise: Code Function *execute*

Given

<i>evaluate</i> $\llbracket I \rrbracket =$	<i>addr</i> (a) = [SB + 11]
LOAD <i>addr</i> (I)	<i>addr</i> (b) = [SB + 12]
<i>execute</i> $\llbracket I := IL \rrbracket =$	<i>addr</i> (c) = [SB + 13]
LOADL <i>IL</i>	
STORE <i>addr</i> (I)	

generate code for:

```
if b then
    if c then a := 1 else a := 2
else
    a := 3
```

# Code Function *execute* (5)

In detail (pseudo Haskell, code generation monad):

```
execute l env n [if E then C1 else C2] = do  
  g ← newName  
  h ← newName  
  evaluate l env E  
  emit (JUMPIFZ g)  
  execute l env n C1  
  emit (JUMP h)  
  emit (Label g)  
  execute l env n C2  
  emit (Label h)
```

# Code Function *execute* (6)

$$\begin{aligned} \text{execute } \llbracket \text{while } E \text{ do } C \rrbracket &= \\ &\text{JUMP } h \\ &g : \text{execute } C \\ &h : \text{evaluate } E \\ &\text{JUMPIFNZ } g \end{aligned}$$

where  $g$  and  $h$  are **fresh** names.

# Code Function *execute* (7)

$$\begin{aligned} \text{execute } \llbracket \text{let } Ds \text{ in } C \rrbracket = \\ \text{elaborate}^* Ds \\ \text{execute } C \\ \text{POP } 0 \ s \end{aligned}$$

where  $s$  is the amount of storage allocated by  $\text{elaborate}^* Ds$ .

# Code Function *execute* (8)

In detail (pseudo Haskell, code generation monad):

```
execute l env n [[let Ds in C] = do  
    (env', n') ← elaborate* l env n Ds  
    execute l env' n' C  
    emit (POP 0 (n' - n))
```

where:

```
elaborate* : Level → CGEnv → Depth  
            → Declaration*  
            → CG TAMInst (Env, Depth)
```



# Code Function $execute^*$

The code function  $execute^*$  has the obvious definition:

$$execute^* \llbracket \epsilon \rrbracket = \epsilon$$

$$execute^* \llbracket C ; Cs \rrbracket = \\ execute\ C \\ execute^* Cs$$

# MiniTriangle Abstract Syntax Part II

<i>Expression</i>	→	<u><i>IntegerLiteral</i></u>	ExpLitInt
		<u><i>Identifier</i></u>	ExpVar
		<u><i>Operator</i></u> <i>Expression</i>	ExpUnOpApp
		<i>Expression</i> <u><i>Operator</i></u>	ExpBinOpApp
		<i>Expression</i>	
<i>Declaration</i>	→	<b>const</b> <u><i>Identifier</i></u> :	DeclConst
		<i>TypeDenoter</i> = <i>Expression</i>	
		<b>var</b> <u><i>Identifier</i></u> : <i>TypeDenoter</i>	DeclVar
		( := <i>Expression</i>   $\epsilon$ )	
<i>TypeDenoter</i>	→	<u><i>Identifier</i></u>	TDBaseType

# Code Function *evaluate* (1)

*evaluate* : *Expression*  $\rightarrow$  *Instruction*\*

Fundamental invariant: all operations take arguments from the stack and writes result back onto the stack.

## Code Function *evaluate* (2)

Consider evaluating  $2 + 4 * 3 - 5$ . Plausible instruction sequence:

LOADL 2	Stack: 2
LOADL 4	Stack: 4, 2
LOADL 3	Stack: 3, 4, 2
CALL mul	Stack: 12, 2
CALL add	Stack: 14
LOADL 5	Stack: 5, 14
CALL sub	Stack: 9

(mul, add, sub are routines in the MiniTriangle standard library.)

# Code Function *evaluate* (3)

$$\textit{evaluate} \llbracket IL \rrbracket = \text{LOADL } c$$

where  $c$  is the value of  $IL$ .

$$\textit{evaluate} \llbracket I \rrbracket = \textit{fetch } I$$

# Code Function *evaluate* (4)

*evaluate*  $\llbracket \ominus E \rrbracket =$   
*evaluate*  $E$   
CALL *addr*( $\ominus$ )

*evaluate*  $\llbracket E_1 \otimes E_2 \rrbracket =$   
*evaluate*  $E_1$   
*evaluate*  $E_2$   
CALL *addr*( $\otimes$ )

(A call to a known function that can be replaced by a short code sequence can be optimised away at a later stage; e.g. CALL *add*  $\Rightarrow$  ADD.)

# Code Functions *fetch* and *assign* (1)

In simplified MiniTriangle, all constants and variables are **global**. Hence addressing relative to SB.

$$\text{fetch } \llbracket I \rrbracket = \text{LOAD } [\text{SB} + d]$$

where  $d$  is offset (or *displacement*) of  $I$  relative to SB.

$$\text{assign } \llbracket I \rrbracket = \text{STORE } [\text{SB} + d]$$

where  $d$  is offset of  $I$  relative to SB.

# Code Functions *fetch* and *assign* (2)

In a more realistic language, *fetch* and *assign* would take the current scope level and the scope level of the variable into account:



## Code Functions *fetch* and *assign* (2)

In a more realistic language, *fetch* and *assign* would take the current scope level and the scope level of the variable into account:

- Global variables addressed relative to SB.

# Code Functions *fetch* and *assign* (2)

In a more realistic language, *fetch* and *assign* would take the current scope level and the scope level of the variable into account:

- Global variables addressed relative to  $SB$ .
- Local variables addressed relative to  $LB$ .

## Code Functions *fetch* and *assign* (2)

In a more realistic language, *fetch* and *assign* would take the current scope level and the scope level of the variable into account:

- Global variables addressed relative to  $SB$ .
- Local variables addressed relative to  $LB$ .
- Non-global variables in enclosing scopes would be reached by following the ***static links*** (see later lecture) in one or more steps, and *fetch* and *assign* would have to generate the appropriate code.

# Assignment revisited

In detail (pseudo Haskell, code generation monad) the code for assignment looks more like this.

Note that the variable actually is represented by an **expression** that gets evaluated to an **address**:

```
execute l env n [  $E_v := E$  ] = do  
  evaluate l env E  
  evaluate l env E_v  
  case sizeof(E) of  
    1  $\rightarrow$  emit (STOREI 0)  
    s  $\rightarrow$  emit (STOREIB s)
```

(Reasons include: array references ( $a[i]$ ), call by reference parameters.)

# Exercise: Code Function *evaluate*

Given

$$\text{addr}(a) = [\text{SB} + 11]$$

$$\text{addr}(b) = [\text{SB} + 12]$$

$$\text{addr}(+) = \text{add}$$

$$\text{addr}(*) = \text{mult}$$

generate code for:

$$a + (b * 2)$$

# Code Function *elaborate* (1)

Elaboration must deposit value/reserve space for value on stack. Also, address (offset) of elaborated entity must be recorded (to be used by *fetch* and *assign*).

# Code Function *elaborate* (1)

Elaboration must deposit value/reserve space for value on stack. Also, address (offset) of elaborated entity must be recorded (to be used by *fetch* and *assign*).

*elaborate* : Declaration  $\rightarrow$  Instruction<sup>\*</sup>  
*elaborate*  $\llbracket$  const  $I : TD = E \rrbracket =$   
*evaluate*  $E$

# Code Function *elaborate* (1)

Elaboration must deposit value/reserve space for value on stack. Also, address (offset) of elaborated entity must be recorded (to be used by *fetch* and *assign*).

$$\begin{aligned} \textit{elaborate} & : \text{Declaration} \rightarrow \text{Instruction}^* \\ \textit{elaborate} \llbracket \text{const } I : TD = E \rrbracket & = \\ & \textit{evaluate } E \end{aligned}$$

(Additionally, the offset (w.r.t. SB) has to be recorded for the identifier denoted by *I*.)



## Code Function *elaborate* (2)

$$\textit{elaborate} \llbracket \text{var } I : TD \rrbracket =$$
$$\text{LOADL } 0$$
$$\textit{elaborate} \llbracket \text{var } I : TD := E \rrbracket =$$
$$\textit{evaluate } E$$

(Additionally, the offset (w.r.t. SB) has to be recorded for the identifier denoted by  $I$ .)

LOADL 0 is just used to reserve space on the stack; the value of the literal does not matter. More space must be reserved if the values of the type are big (e.g. record, array).

# Code Function *elaborate* (3)

For procedures and functions:

- Generate a fresh name for the entry point.
- Extend the environment according to formal argument declarations (the caller will push actual arguments onto stack prior to call).
- Generate code for the body at a scope level incremented by 1 and in the extended environment.

# Identifiers vs. Symbols (1)

- The coursework compiler HMTC uses **symbols** instead of identifiers in the latter stages.
- Symbols are introduced in the type checker (responsible for identification in HMTC) in place of identifiers (rep. changed from AST to MTIR).
- Symbols carry **semantic information** (e.g., type, scope level) to make that information readily available to e.g. the code generator.

(Cf. the lectures on identification where applied identifier occurrences were annotated with semantic information.)

# Identifiers vs. Symbols (2)

- Two kinds of (term-level) symbols:
  - External: defined outside the current compilation unit (e.g., in a library).
  - Internal: defined in the current compilation unit (in a `let`).

```
type TermSym = Either ExtTermSym IntTermSym
```

```
data ExtTermSym = ExtTermSym { ... }
```

```
data IntTermSym = IntTermSym { ... }
```

# External Symbols

- External symbols are known entities.
- Can thus be looked up once and for all (during identification).
- Have a value, such as a (symbolic) address.

```
data ExtTermSym = ExtTermSym {  
    etmsName  :: Name,  
    etmsType  :: Type,  
    etmsVal   :: ExtSymVal  
}
```

```
data ExtSymVal = ESVLbl Name | ESVInt MTInt | ...
```

# Internal Symbols

- Internal symbols do *not* carry any value such as stack displacement because this is not computed until the time of code generation.
- Such “late” information about an entity referred to by an internal symbol thus has to be looked up in the code generation environment.

```
data IntTermSym = IntTermSym {  
    itmsLvl      :: ScopeLvl,  
    itmsName    :: Name,  
    itmsType    :: Type,  
    itmsSrcPos  :: SrcPos  
}
```