## LiU-FP2016: Lecture 10

Monad Transformers

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### Monad Transformers (1)

What if we need to support more than one type of effect?

For example: State and Error/Partiality?

We could implement a suitable monad from scratch:

newtype SE s a = SE (s  $\rightarrow$  Maybe (a, s))

### Monad Transformers (2)

#### However:

• Not always obvious how: e.g., should the combination of state and error have been

newtype SE s a = SE (s  $\rightarrow$  (Maybe a, s))

 Duplication of effort: similar patterns related to specific effects are going to be repeated over and over in the various combinations.

### Monad Transformers (3)

#### Monad Transformers can help:

- A monad transformer transforms a monad by adding support for an additional effect.
- A library of monad transformers can be developed, each adding a specific effect (state, error, ...), allowing the programmer to mix and match.
- A form of aspect-oriented programming.

Caveat: Will consider the idea of monad transformers, not any specific library like e.g. MTL.

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### Monad Transformers in Haskell (1)

 A monad transformer maps monads to monads. Represented by a type constructor T of the following kind:

T ::  $(* \rightarrow *) \rightarrow (* \rightarrow *)$ 

 Additionally, a monad transformer adds computational effects. A mapping lift from computations in the underlying monad to computations in the transformed monad is needed:

lift :: M a -> T M a

### Monad Transformers in Haskell (2)

# • These requirements are captured by the following (multi-parameter) type class:

class (Monad m, Monad (t m))
 => MonadTransformer t m where
 lift :: m a -> t m a

### **Classes for Specific Effects**

A monad transformer adds specific effects to *any* monad. Thus the effect-specific operations needs to be overloaded. For example:

```
class Monad m => E m where
    eFail :: m a
    eHandle :: m a -> m a -> m a
```

```
class Monad m => S m s | m -> s where
   sSet :: s -> m ()
   sGet :: m s
```

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### The Identity Monad

We are going to construct monads by successive transformations of the identity monad:

```
newtype I a = I a unI (I a) = a
```

instance Monad I where return a = I a m >>= f = f (unI m)

runI :: I a -> a runI = unI

### The Error Monad Transformer (1)

newtype ET m a = ET (m (Maybe a))
unET (ET m) = m

#### Any monad transformed by ET is a monad:

instance Monad m => Monad (ET m) where return a = ET (return (Just a))

m >>= f = ET \$ do ma <- unET m case ma of Nothing -> return Nothing Just a -> unET (f a)

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### **The Error Monad Transformer (2)**

#### We need the ability to run transformed monads:

runET :: Monad m => ET m a -> m a
runET etm = do
 ma <- unET etm
 case ma of
 Just a -> return a
 Nothing -> error "Should not happen"
ET is a monad transformer:
 instance Monad m =>
 MonadTransformer ET m where

lift m = ET (m >>= \a -> return (Just a))

### The Error Monad Transformer (3)

#### Any monad transformed by ET is an instance of E:

instance Monad m => E (ET m) where eFail = ET (return Nothing) ml 'eHandle' m2 = ET \$ do ma <- unET m1 case ma of Nothing -> unET m2 Just \_ -> return ma

### **The Error Monad Transformer (4)**

# A state monad transformed by ${\mathbb E}{\mathbb T}$ is a state monad:

instance S m s => S (ET m) s where sSet s = lift (sSet s) sGet = lift sGet

### **Exercise 2: Running Transf. Monads**

#### Let

ex2 = eFail 'eHandle' return 1

- 1. Suggest a possible type for ex2. (Assume 1 :: Int.)
- 2. Given your type, use the appropriate combination of "run functions" to run ex2.

### **Exercise 2: Solution**

ex2 :: ET I Int
ex2 = eFail 'eHandle' return 1

ex2result :: Int
ex2result = runI (runET ex2)

## The State Monad Transformer (1)

newtype ST s m a = ST (s  $\rightarrow$  m (a, s)) unST (ST m) = m

#### Any monad transformed by ST is a monad:

instance Monad m => Monad (ST s m) where return a = ST (\s -> return (a, s))

m >>= f = ST \$ \s -> do
 (a, s') <- unST m s
 unST (f a) s'</pre>

### The State Monad Transformer (2)

#### We need the ability to run transformed monads:

runST :: Monad m => ST s m a -> s -> m a
runST stf s0 = do
 (a, \_) <- unST stf s0
 return a</pre>

#### ST is a monad transformer:

instance Monad m =>
 MonadTransformer (ST s) m where
lift m = ST (\s -> m >>= \a ->
 return (a, s))

### The State Monad Transformer (3)

#### Any monad transformed by ST is an instance of S:

instance Monad m => S (ST s m) s where sSet s = ST ( $\ ->$  return ((), s)) sGet = ST ( $\ ->$  return (s, s))

## An error monad transformed by ST is an error monad:

instance E m => E (ST s m) where eFail = lift eFail m1 'eHandle' m2 = ST \$ \s -> unST m1 s 'eHandle' unST m2 s

### **Exercise 3: Effect Ordering**

#### Consider the code fragment

ex3a :: (ST Int (ET I)) Int ex3a = (sSet 42 >> eFail) 'eHandle' sGet

# Note that the exact same code fragment also can be typed as follows:

ex3b :: (ET (ST Int I)) Int ex3b = (sSet 42 >> eFail) 'eHandle' sGet

#### What is

runI (runET (runST ex3a 0)) runI (runST (runET ex3b) 0)

. . . .

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### **Exercise 3: Solution**

runI (runET (runST ex3a 0)) = 0 runI (runST (runET ex3b) 0) = 42

### Why? Because:

ST s (ET I) a  $\cong$  s -> (ET I) (a, s)  $\cong$  s -> I (Maybe (a, s))  $\cong$  s -> Maybe (a, s) ET (ST s I) a  $\cong$  (ST s I) (Maybe a)  $\cong$  s -> I (Maybe a, s)  $\cong$  s -> I (Maybe a, s)  $\cong$  s -> (Maybe a, s)

### **Exercise 4: Alternative ST?**

#### To think about.

Could  $\ensuremath{\mathtt{ST}}$  have been defined in some other way, e.g.

newtype ST s m a = ST (m (s  $\rightarrow$  (a, s)))

#### or perhaps

newtype ST s m a = ST (s -> (m a, s))

## Reading (1)

- Nick Benton, John Hughes, Eugenio Moggi. Monads and Effects. In *International Summer School on Applied Semantics 2000*, Caminha, Portugal, 2000.
- Sheng Liang, Paul Hudak, Mark Jones. Monad Transformers and Modular Interpreters. In Proceedings of the 22nd ACM Symposium on Principles of Programming Languages (POPL'95), January 1995, San Francisco, California

### Reading (2)

- Mauro Jaskelioff. Monatron: An Extensible Monad Transformer Library. In *Implementation of Functional* Languages (IFL'08), 2008.
- Mauro Jaskelioff. Modular Monad Transformers. In European Symposium on Programming (ESOP,09), 2009.

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### **Problems with Monad Transformers**

- With one transformer for each possible effect, we get a lot of combinations: the number grows quadratically; each has to be instantiated explicitly.
- Jaskelioff (2008,2009) has proposed a possible, more extensible alternative.