LiU-FP2016: Lecture 10 Monad Transformers

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We could implement a suitable monad from scratch:

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 Duplication of effort: similar patterns related to specific effects are going to be repeated over and over in the various combinations.

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- A library of monad transformers can be developed, each adding a specific effect (state, error, ...), allowing the programmer to mix and match.
- A form of aspect-oriented programming.

Caveat: Will consider the idea of monad transformers, not any specific library like e.g. MTL.

Monad Transformers in Haskell (1)

 A monad transformer maps monads to monads. Represented by a type constructor T of the following kind:

T:
$$(* \rightarrow *) \rightarrow (* \rightarrow *)$$

LiU-FP2016: Lecture 10 – p.5/23

Monad Transformers in Haskell (1)

 A monad transformer maps monads to monads. Represented by a type constructor T of the following kind:

T :: (* -> *) -> (* -> *)

 Additionally, a monad transformer adds computational effects. A mapping lift from computations in the underlying monad to computations in the transformed monad is needed:

lift :: M a -> T M a

Monad Transformers in Haskell (2)

These requirements are captured by the following (multi-parameter) type class:

class (Monad m, Monad (t m))

=> MonadTransformer t m where

lift :: m a -> t m a

Classes for Specific Effects

A monad transformer adds specific effects to any monad. Thus the effect-specific operations needs to be overloaded. For example:

class Monad m => E m where eFail :: m a eHandle :: m a -> m a -> m a

class Monad m => S m s | m -> s where
 sSet :: s -> m ()
 sGet :: m s

The Identity Monad

We are going to construct monads by successive transformations of the identity monad:

newtype I a = I aunI (I a) = a

instance Monad I where
 return a = I a
 m >>= f = f (unI m)

runI :: I a -> a runI = unI

The Error Monad Transformer (1)

newtype ET m a = ET (m (Maybe a))
unET (ET m) = m

Any monad transformed by ET is a monad:

instance Monad m => Monad (ET m) where return a = ET (return (Just a))

m >>= f = ET \$ do
 ma <- unET m
 case ma of
 Nothing -> return Nothing
 Just a -> unET (f a)

The Error Monad Transformer (2)

We need the ability to run transformed monads:

runET :: Monad m => ET m a -> m a
runET etm = do
ma <- unET etm
case ma of
Just a -> return a
Nothing -> error "Should not happen"
ET is a monad transformer:

instance Monad m =>
 MonadTransformer ET m where
 lift m = ET (m >>= \a -> return (Just a))

The Error Monad Transformer (3)

Any monad transformed by ET is an instance of E:

instance Monad m => E (ET m) where eFail = ET (return Nothing) m1 'eHandle' m2 = ET \$ do ma <- unET m1 case ma of Nothing -> unET m2 Just _ -> return ma

The Error Monad Transformer (4)

A state monad transformed by ET is a state monad:

instance S m s => S (ET m) s where
 sSet s = lift (sSet s)
 sGet = lift sGet

Exercise 2: Running Transf. Monads

Let

ex2 = eFail 'eHandle' return 1

1. Suggest a possible type for ex2.
 (Assume 1 :: Int.)

2. Given your type, use the appropriate combination of "run functions" to run ex2.

Exercise 2: Solution

ex2 :: ET I Int
ex2 = eFail `eHandle` return 1

ex2result :: Int
ex2result = runI (runET ex2)

The State Monad Transformer (1)

newtype ST s m a = ST (s -> m (a, s))
unST (ST m) = m

Any monad transformed by ST is a monad:

instance Monad m => Monad (ST s m) where
 return a = ST (\s -> return (a, s))

The State Monad Transformer (2)

We need the ability to run transformed monads:

runST :: Monad m => ST s m a -> s -> m a runST stf s0 = do (a, _) <- unST stf s0 return a ST is a monad transformer: instance Monad m => MonadTransformer (ST s) m where lift m = ST ($\s -> m >>= \a ->$ return (a, s))

The State Monad Transformer (3)

Any monad transformed by ST is an instance of S:

instance Monad m => S (ST s m) s where

sSet s = ST ($\ ->$ return ((), s))

 $sGet = ST (\langle s - \rangle return (s, s))$

An error monad transformed by ST is an error monad:

instance E m => E (ST s m) where
eFail = lift eFail
m1 'eHandle' m2 = ST \$ \s ->
unST m1 s 'eHandle' unST m2 s

Exercise 3: Effect Ordering

Consider the code fragment

ex3a :: (ST Int (ET I)) Int

ex3a = (sSet 42 >> eFail) 'eHandle' sGet

Note that the exact same code fragment also can be typed as follows:

ex3b :: (ET (ST Int I)) Int

ex3b = (sSet 42 >> eFail) 'eHandle' sGet

What is

runI (runET (runST ex3a 0))
runI (runST (runET ex3b) 0)

Exercise 3: Solution

runI (runET (runST ex3a 0)) = 0runI (runST (runET ex3b) 0) = 42Why? Because: <u>ST s (ET I) a \cong s -> (ET I) (a, s)</u> \cong s -> I (Maybe (a, s)) \cong s -> Maybe (a, s) ET (ST s I) a \cong (ST s I) (Maybe a) \cong s -> I (Maybe a, s) \cong s -> (Maybe a, s) LiU-FP2016: Lecture 10 - p.19/23

Exercise 4: Alternative ST?

To think about.

Could ST have been defined in some other way, e.g.

newtype ST s m a = ST (m (s -> (a, s)))
or perhaps

newtype ST s m a = ST $(s \rightarrow (m a, s))$

Problems with Monad Transformers

- With one transformer for each possible effect, we get a lot of combinations: the number grows quadratically; each has to be instantiated explicitly.
- Jaskelioff (2008,2009) has proposed a possible, more extensible alternative.

Reading (1)

- Nick Benton, John Hughes, Eugenio Moggi. Monads and Effects. In *International Summer School on Applied Semantics 2000*, Caminha, Portugal, 2000.
- Sheng Liang, Paul Hudak, Mark Jones. Monad Transformers and Modular Interpreters. In *Proceedings* of the 22nd ACM Symposium on Principles of Programming Languages (POPL'95), January 1995, San Francisco, California

Reading (2)

- Mauro Jaskelioff. Monatron: An Extensible Monad
 Transformer Library. In *Implementation of Functional Languages (IFL'08)*, 2008.
- Mauro Jaskelioff. Modular Monad Transformers. In European Symposium on Programming (ESOP,09), 2009.