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The Arpeggigon: A Functional Reactive Musical Automaton

London Haskell Meetup, 2017-06-28

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The Arpeggigon (1)

- Software realisation of the reacTogon:



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- Interactive cellular automaton:
 - Configuration
 - Performance parameters

The Arpeggigon (2)

- Implemented in Haskell using:
 - The Functional Reactive Programming (FRP) system Yampa
 - Reactive Values and Relations

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- Based on the *Harmonic Table*

The Arpeggigon (2)

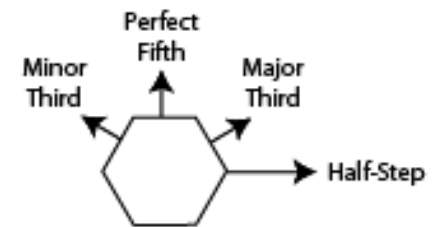
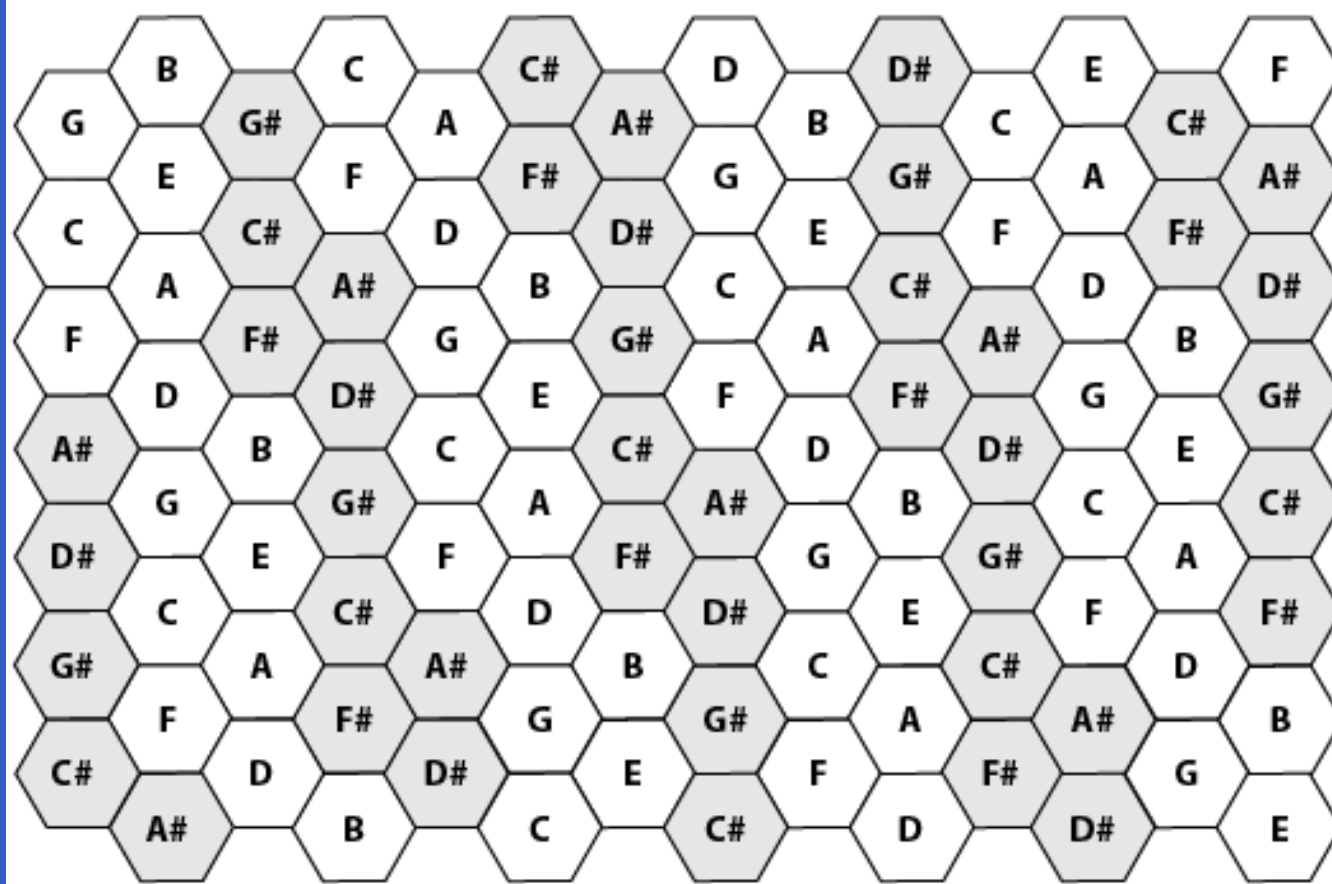
- Implemented in Haskell using:
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 - Reactive Values and Relations
- Based on the *Harmonic Table*

Code: <https://gitlab.com/chupin/arpeggigon>

Video:

<https://www.youtube.com/watch?v=v0HIkFR1EN4>

The Harmonic Table



Running a Sample Configuration

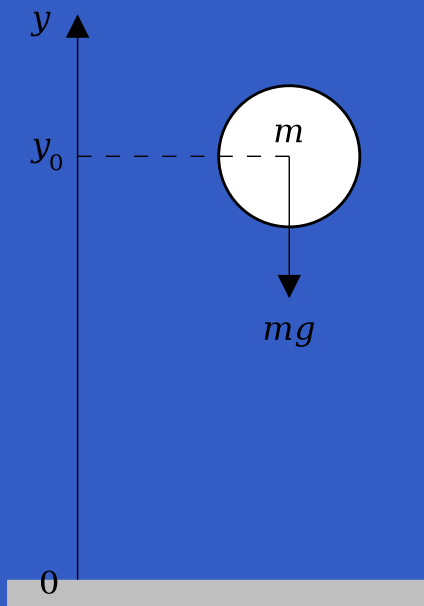
The screenshot displays the Arpeggigon software interface. On the left, a large hexagonal grid is shown with several notes placed on it. The notes are represented by green hexagons and black circles with white symbols. The grid is labeled "Layer" in the top-left corner. On the right, a control panel is visible, featuring a tempo slider set to 120. Below the tempo slider, there are controls for "Layer beat" (set to "Quarter note"), "Beats per bar" (set to 4), "Volume" (set to 99), and "Strength" (set to 1.0). There are also checkboxes for "Repeat count" (checked), "Enable repeat count", and "Keep heads on restart". The instrument is set to "Acoustic Grand Piano". Other settings include "NoAccent", "NoSlide", and "Quarter note" for the note type. At the bottom of the control panel, there are buttons for "Add layer", "Remove layer", "Save configuration", "Load configuration", "Restart", "Pause", "Stop", and "Record".

This Talk

- Demonstration
- Brief introduction to FRP and Yampa
- Time in music
- The Arpeggigon core
- Brief introduction to Reactive Values and Relations
- The Arpeggigon shell

Functional Reactive Programming (1)

- Key idea: Don't program one-time-step-at-a-time, but describe an evolving entity as whole.



$$y = y_0 + \int v dt$$

$$v = v_0 + \int -9.81$$

We are used to describing behaviours in totality over time in mathematics. Why not program in the same way?

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- FRP has evolved in a number of directions and into different concrete implementations.
- We will use Yampa: an FRP system embedded in Haskell.

Key FRP Features

Combines conceptual simplicity of the synchronous data flow approach with the flexibility and abstraction power of higher-order functional programming:

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Good conceptual fit for many applications, including games and, as we will see here, interactive musical applications.

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Yampa

Yampa

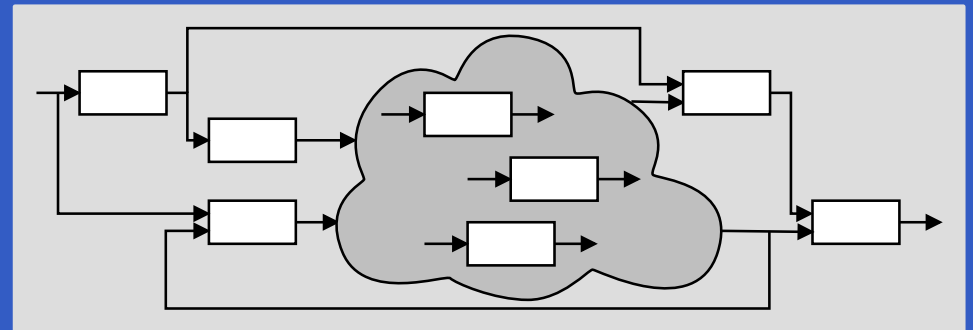
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Yampa

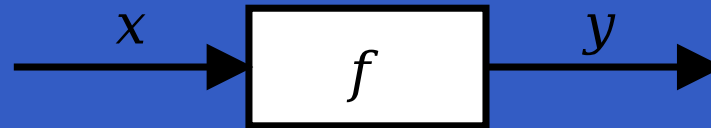
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- Key notions:
 - **Signals**: time-varying values
 - **Signal Functions**: pure functions on signals
 - **Switching**: temporal composition of signal functions

Yampa

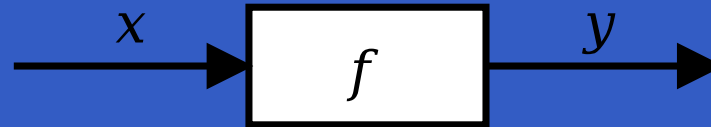
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 - **Signal Functions**: pure functions on signals
 - **Switching**: temporal composition of signal functions
- Programming model:



Signal Functions

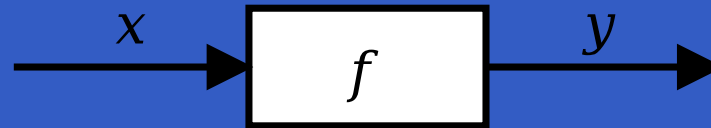


Signal Functions



Intuition:

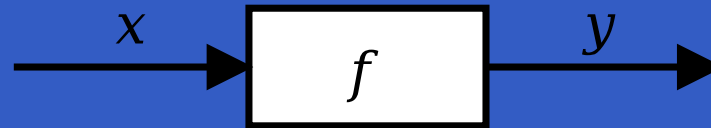
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Intuition:

$Time \approx \mathbb{R}$

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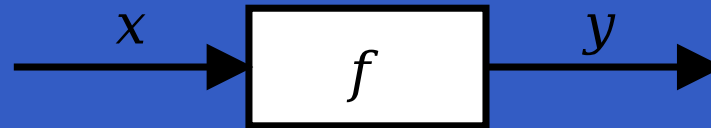
Time $\approx \mathbb{R}$

Signal $a \approx \text{Time} \rightarrow a$

$x :: \text{Signal } T1$

$y :: \text{Signal } T2$

Signal Functions



Intuition:

$Time \approx \mathbb{R}$

$Signal\ a \approx Time \rightarrow a$

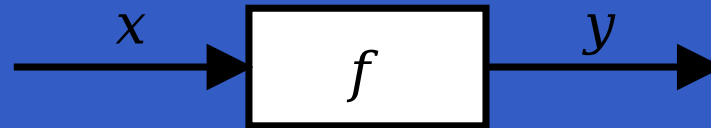
$x :: Signal\ T1$

$y :: Signal\ T2$

$SF\ a\ b \approx Signal\ a \rightarrow Signal\ b$

$f :: SF\ T1\ T2$

Signal Functions



Intuition:

$Time \approx \mathbb{R}$

$Signal\ a \approx Time \rightarrow a$

$x :: Signal\ T1$

$y :: Signal\ T2$

$SF\ a\ b \approx Signal\ a \rightarrow Signal\ b$

$f :: SF\ T1\ T2$

Additionally, **causality** required: output at time t must be determined by input on interval $[0, t]$.

Some Basic Signal Functions

identity :: SF a a

Some Basic Signal Functions

identity :: $SF\ a\ a$

constant :: $b \rightarrow SF\ a\ b$

Some Basic Signal Functions

$identity :: SF\ a\ a$

$constant :: b \rightarrow SF\ a\ b$

$iPre :: a \rightarrow SF\ a\ a$

Some Basic Signal Functions

identity :: $SF\ a\ a$

constant :: $b \rightarrow SF\ a\ b$

iPre :: $a \rightarrow SF\ a\ a$

integral :: $VectorSpace\ a\ s \Rightarrow SF\ a\ a$

$$y(t) = \int_0^t x(\tau) d\tau$$

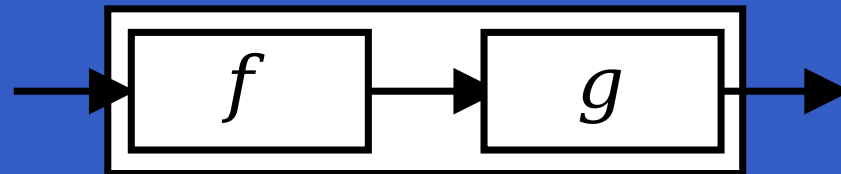
Composition

In Yampa, systems are described by combining signal functions (forming new signal functions).

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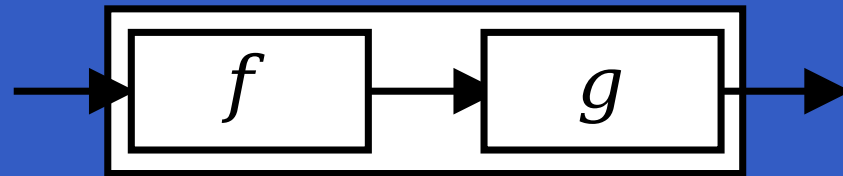
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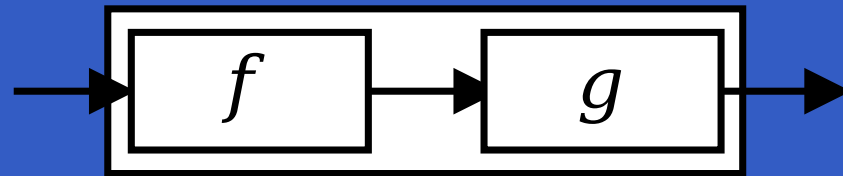
A **combinator** that captures this idea:

$$(\gg) :: SF\ a\ b \rightarrow SF\ b\ c \rightarrow SF\ a\ c$$

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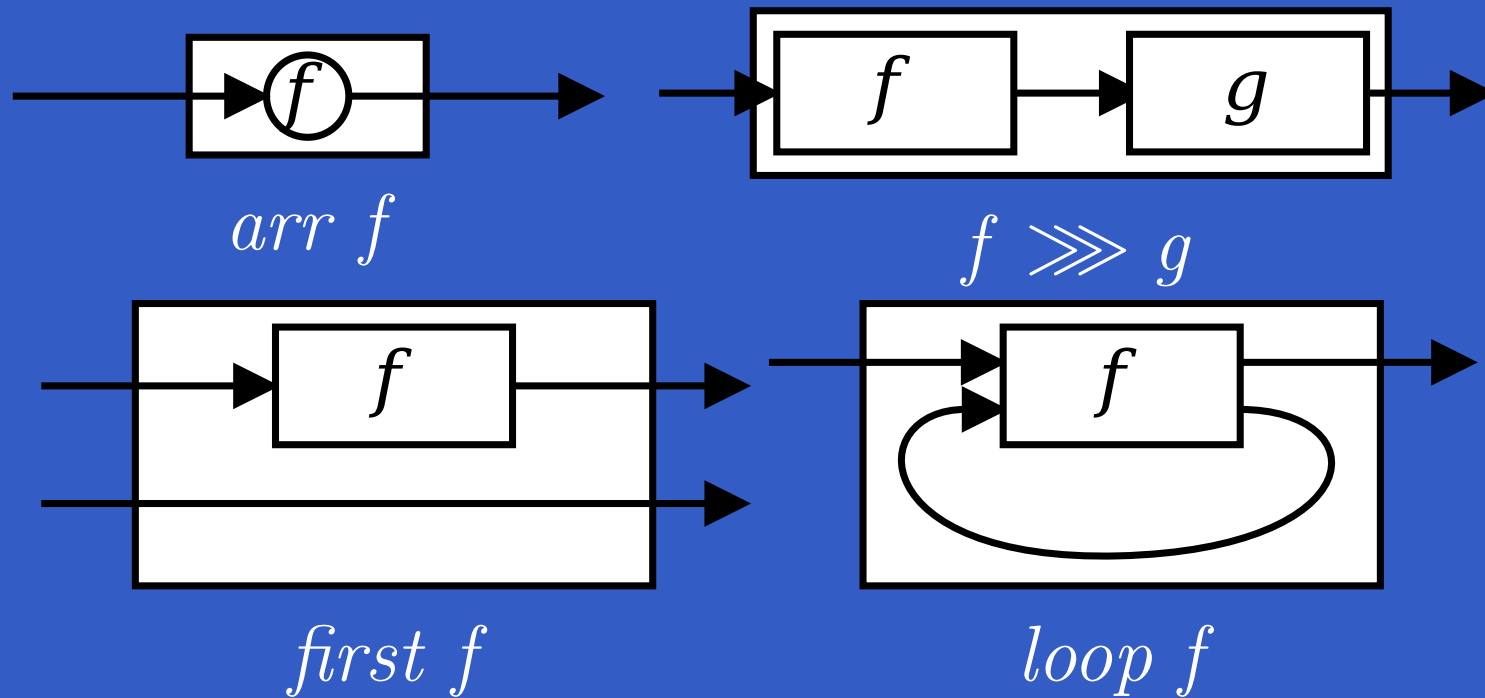


A **combinator** that captures this idea:

$$(\gg) :: SF\ a\ b \rightarrow SF\ b\ c \rightarrow SF\ a\ c$$

Signal functions are the primary notion; signals a secondary one, only existing indirectly.

The Arrow Combinators



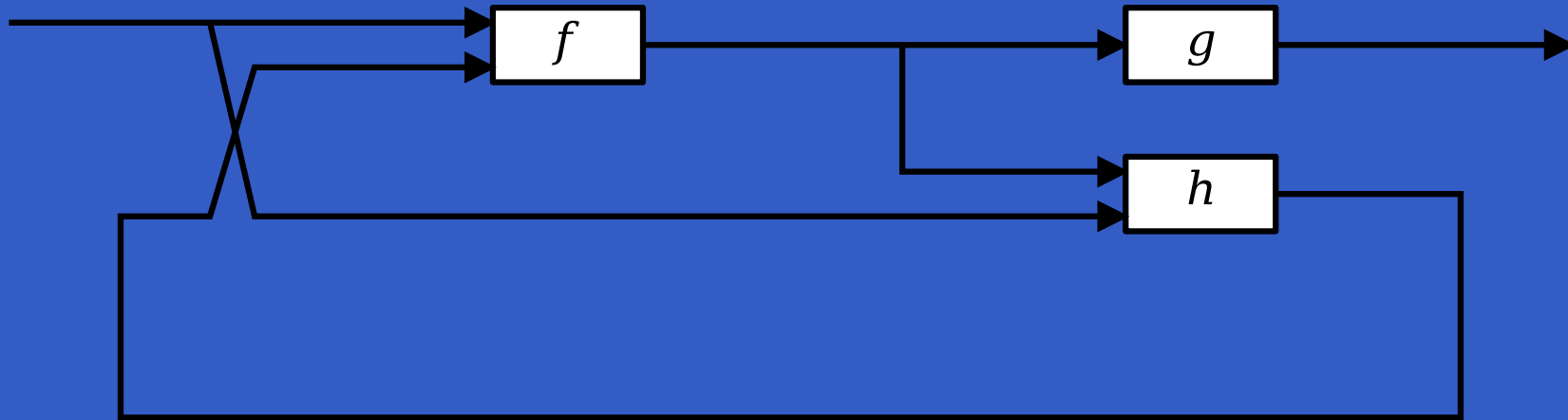
$arr \quad :: (a \rightarrow b) \rightarrow SF\ a\ b$

$(\ggg) \quad :: SF\ a\ b \rightarrow SF\ b\ c \rightarrow SF\ a\ c$

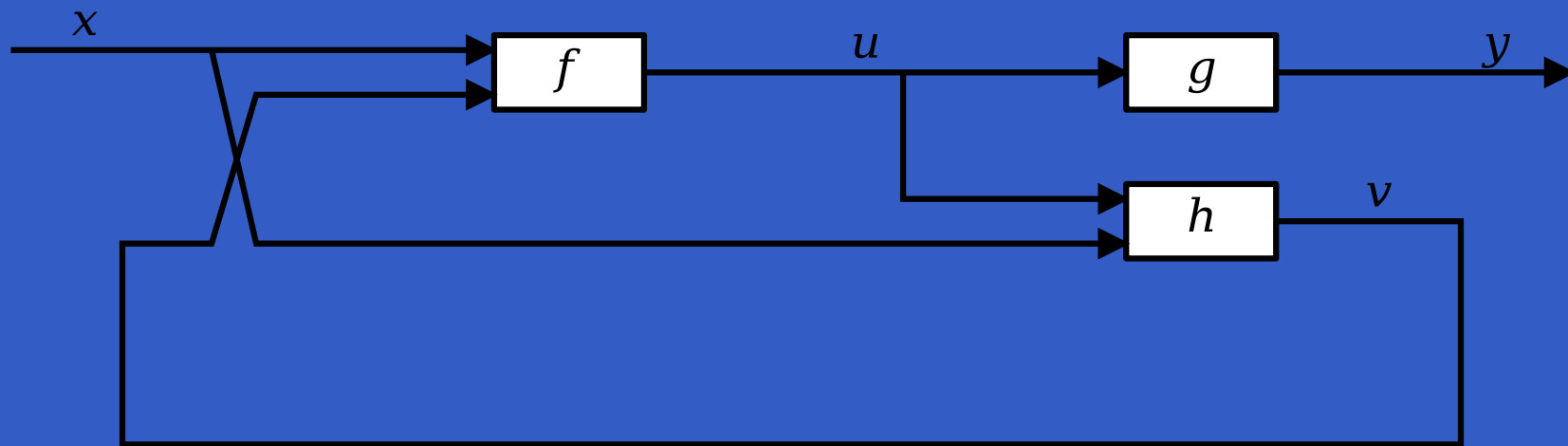
$first \quad :: SF\ a\ b \rightarrow SF\ (a, c)\ (b, c)$

$loop \quad :: SF\ (a, c)\ (b, c) \rightarrow SF\ a\ b$

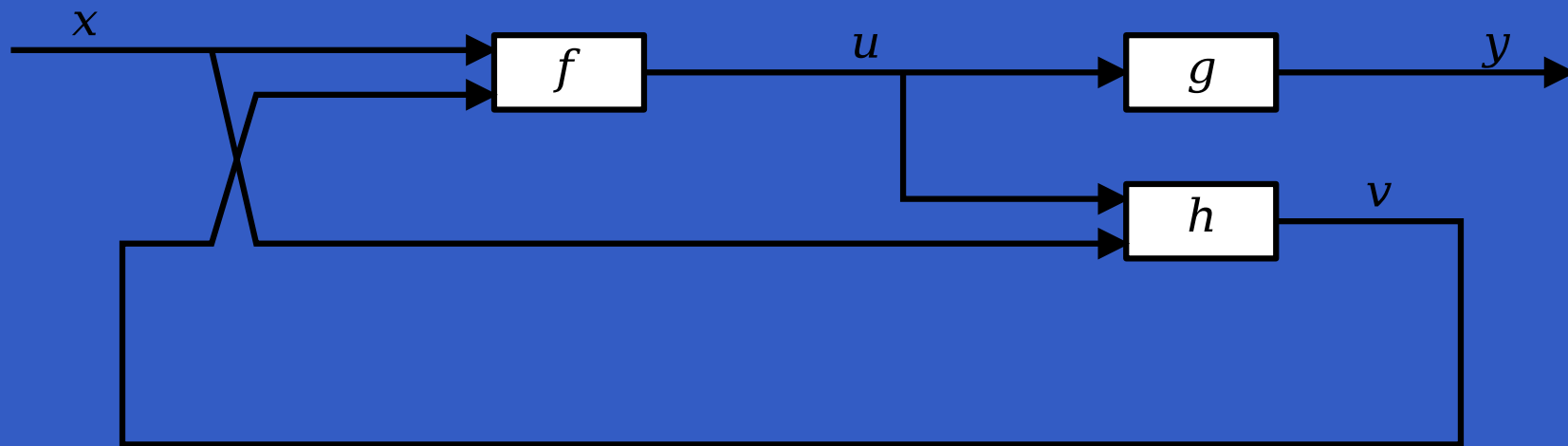
Paterson's Arrow Notation



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`proc x → do`

`rec`

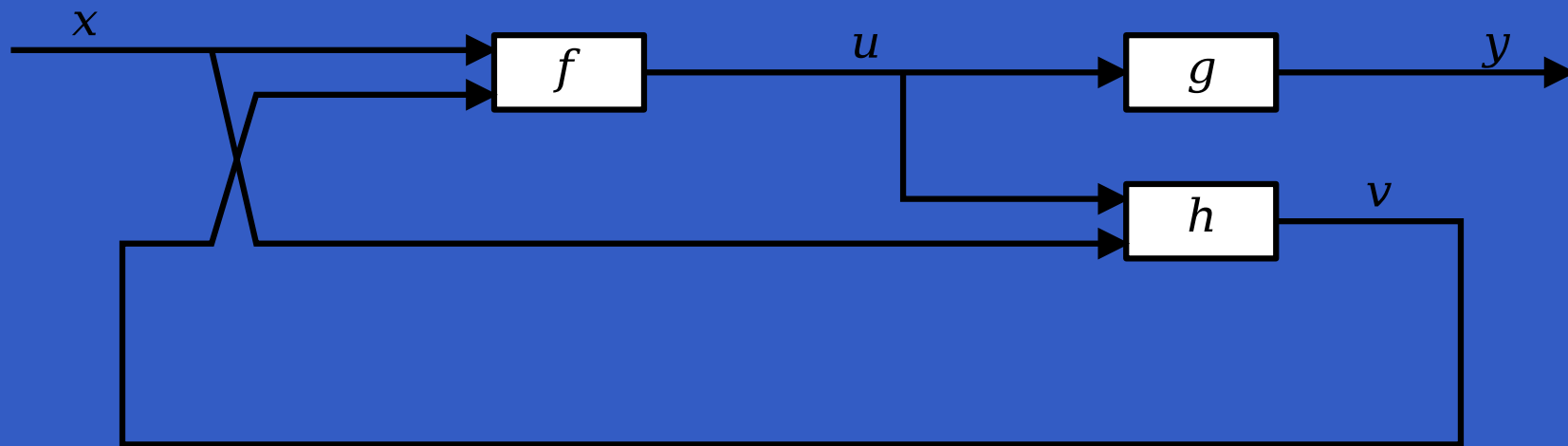
`u ← f ↯ (x, v)`

`y ← g ↯ u`

`v ← h ↯ (u, x)`

`return A ↯ y`

Paterson's Arrow Notation



```
proc  $x \rightarrow$  do
```

```
  rec
```

```
     $u \leftarrow f \multimap (x, v)$ 
```

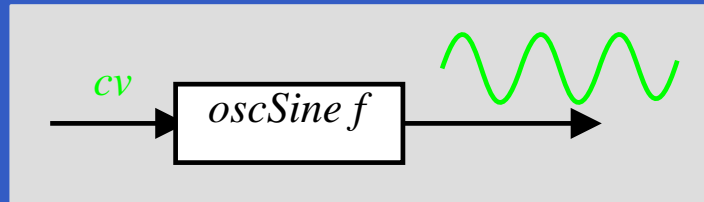
```
     $y \leftarrow g \multimap u$ 
```

```
     $v \leftarrow h \multimap (u, x)$ 
```

```
  return  $A \multimap y$ 
```

Only syntactic sugar:
everything translated into a
combinator expression.

Example 1: Sine oscillator



$oscSine :: Frequency \rightarrow SF \ CV \ Sample$

$oscSine\ f0 = \mathbf{proc}\ cv \rightarrow \mathbf{do}$

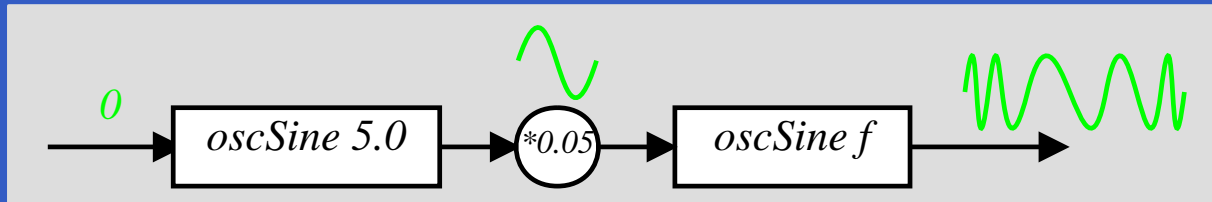
$\mathbf{let}\ f = f0 * (2 ** cv)$

$\phi \leftarrow \mathit{integral} \prec 2 * \pi * f$

$\mathbf{return}\ A \prec \sin\ \phi$

$\mathit{constant}\ 0 \gg \gg oscSine\ 440$

Example 2: Vibrato



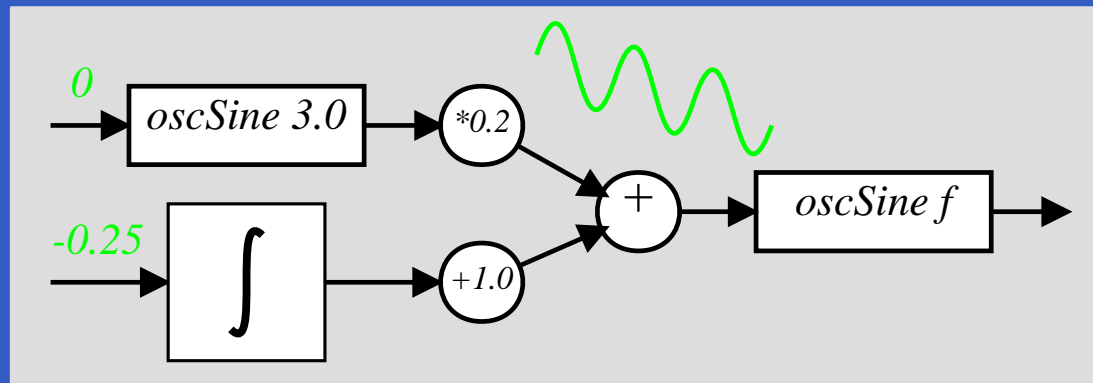
constant 0

≫≫ *oscSine 5.0*

≫≫ *arr (*0.05)*

≫≫ *oscSine 440*

Example 3: 50's Sci Fi



sciFi :: SF () Sample

sciFi = **proc** () → **do**

und ← arr (*0.2) <<< oscSine 3.0 — 0

swp ← arr (+1.0) <<< integral — -0.25

audio ← oscSine 440 — *und* + *swp*

returnA — *audio*

Events

Yampa models discrete-time signals by lifting the *co-domain* of signals using an option-type:

```
data Event a = NoEvent | Event a
```

Discrete-time signal = Signal (Event α).

Events

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$$\text{data } \textit{Event } a = \textit{NoEvent} \mid \textit{Event } a$$

Discrete-time signal = `Signal (Event a)`.

Some functions and event sources:

$$\textit{tag} :: \textit{Event } a \rightarrow b \rightarrow \textit{Event } b$$
$$\textit{after} :: \textit{Time} \rightarrow b \rightarrow \textit{SF } a (\textit{Event } b)$$
$$\textit{edge} :: \textit{SF } \textit{Bool} (\textit{Event } ())$$

Switching

Q: How and when do signal functions “start”?

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Switchers thus allow systems with **varying structure** to be described.

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Switchers thus allow systems with **varying structure** to be described.

Generalised switches allow composition of **collections** of signal functions. Can be used to model e.g. varying number of objects in a game.

The Basic Switch

Idea:

- Allows one signal function to be replaced by another.
- Switching takes place on the first occurrence of the switching event source.

switch::

$SF\ a\ (b,\ Event\ c)$

$\rightarrow (c \rightarrow SF\ a\ b)$

$\rightarrow SF\ a\ b$

The Basic Switch

Idea:

- Allows one signal function to be replaced by another.
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switch::

Initial SF with event source

$SF\ a\ (b,\ Event\ c)$

$\rightarrow (c \rightarrow SF\ a\ b)$

$\rightarrow SF\ a\ b$

The Basic Switch

Idea:

- Allows one signal function to be replaced by another.
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switch::

Function yielding SF to switch into

$SF\ a\ (b,\ Event\ c)$

$\rightarrow (c \rightarrow SF\ a\ b)$

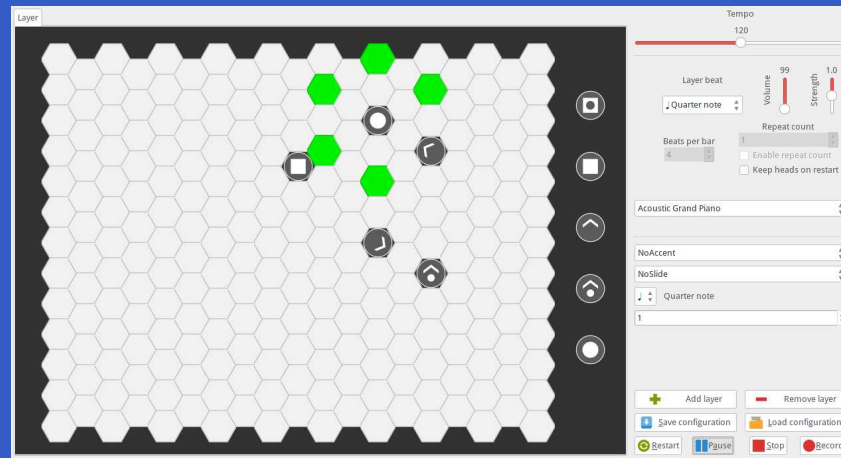
$\rightarrow SF\ a\ b$

Time in Music

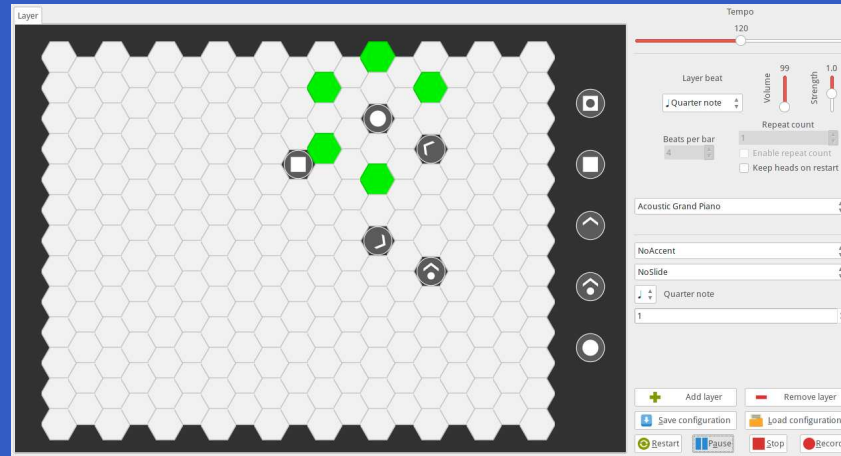
Time inherent to music. Both continuous-time and discrete-time aspects:

- Discrete or *striated* time:
 - Time signatures
 - Notes in a musical score
- Continuous or *smooth* time:
 - Crescendo
 - Ritardando
 - Portamento
 - Filter sweeps (cf. 50's SciFi)

Aspects of the Arpeggigon (1)

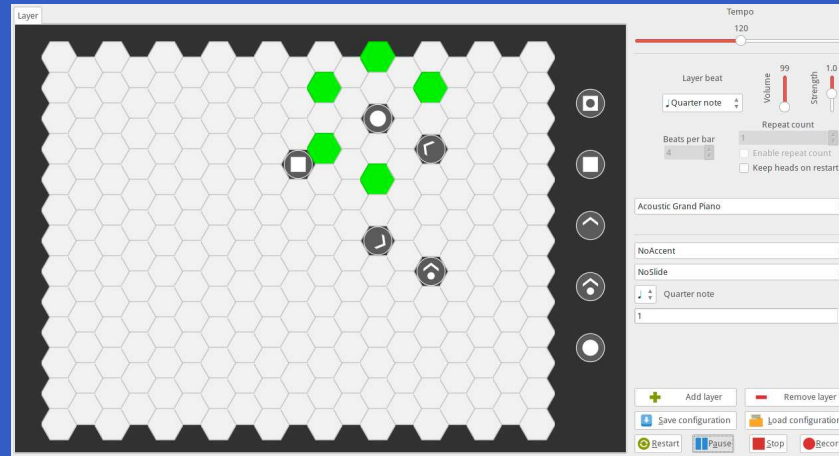


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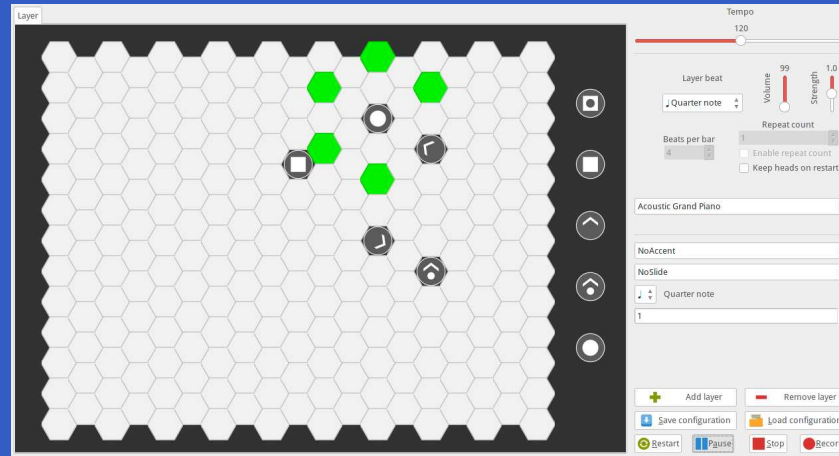
- *Interactive*

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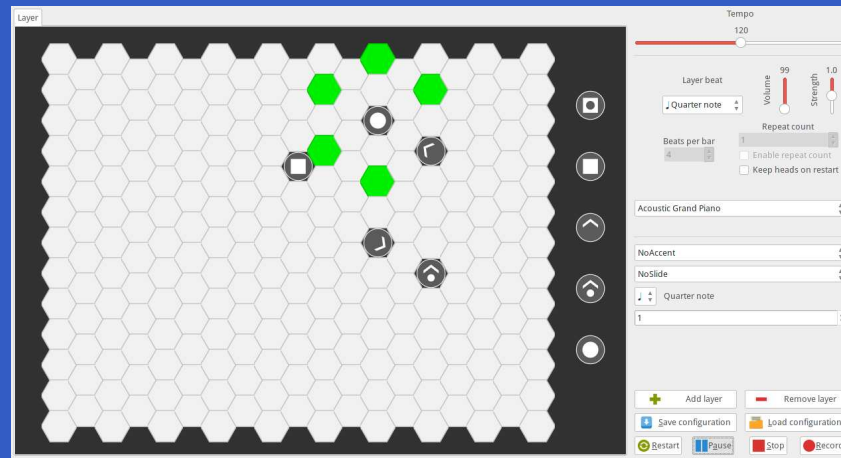
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- Layers can be added/removed: **dynamic structure**

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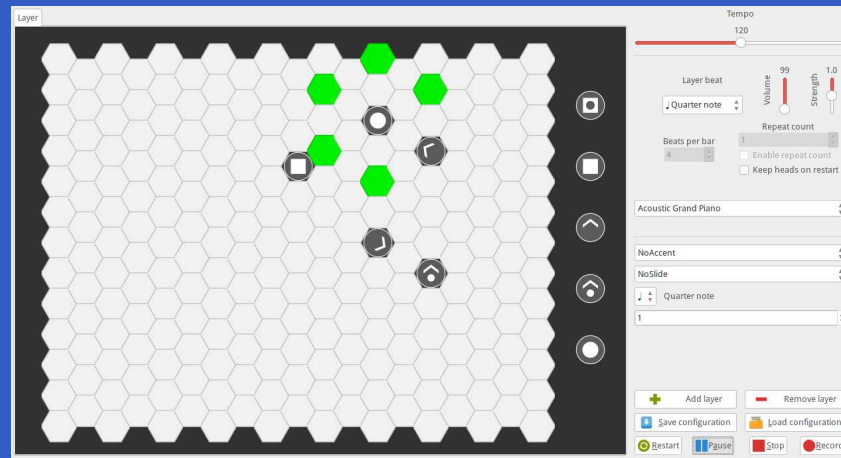
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Aspects of the Arpeggigon (1)



- **Interactive**
- Layers can be added/removed: **dynamic structure**
- Notes generated at **discrete** points in time
- Notes played **slightly shorter** than nominal length
- Configuration and performance parameters can be changed at **any** time

Aspects of the Arpeggigon (2)

Potential further enhancements, e.g.:

- Swing: alternately lengthening and shortening pulse divisions
- Staccato and legato playing
- Sliding notes
- Automated, smooth, performance parameter changes

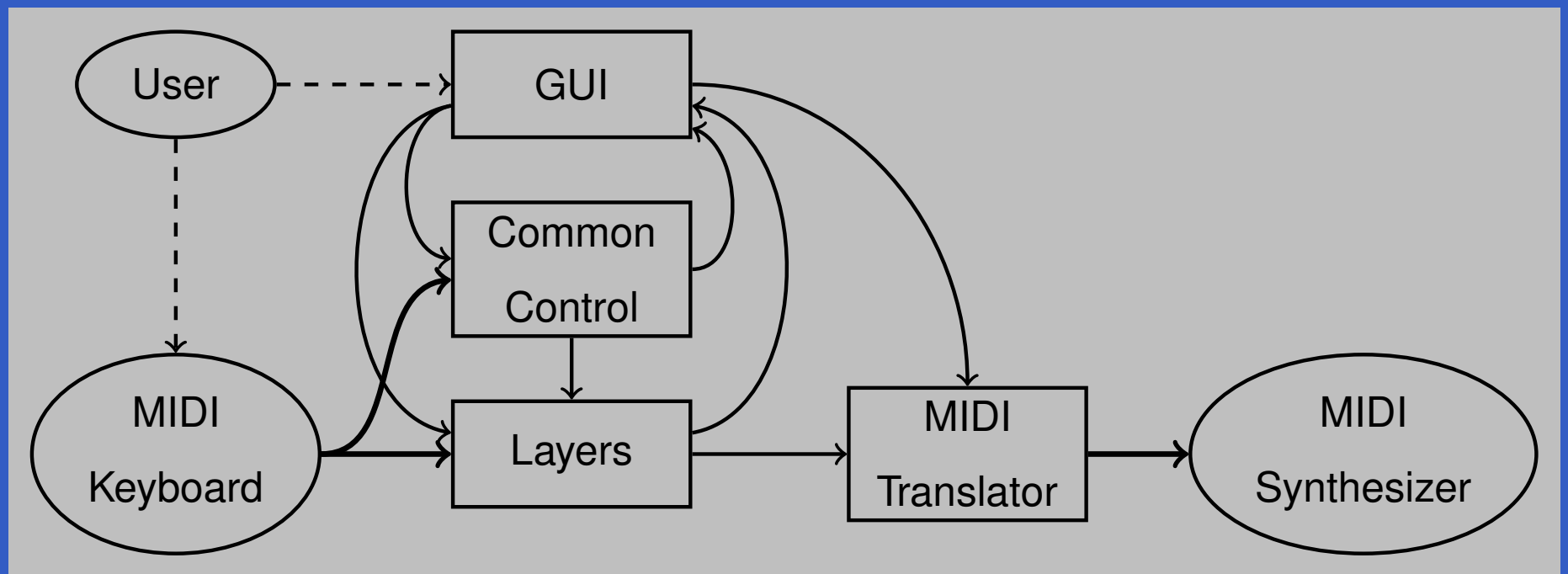
Aspects of the Arpeggigon (2)

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- Staccato and legato playing
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- Automated, smooth, performance parameter changes

Natural fit for an interactive framework supporting both discrete and continuous time. Like *Yampa*.

Arpeggigon Architecture



Some Basic Types

```
data PlayHead =  
  PlayHead {  
    phPos    :: Pos,  
    phBTM   :: Int,  
    phDir    :: Dir  
  }
```

```
data Note = Note {  
  notePch  :: Pitch,  
  noteStr  :: Strength,  
  noteDur  :: Duration,  
  noteOrn  :: Ornaments  
}
```

Cellular Automaton

State transition function for the cellular automaton:

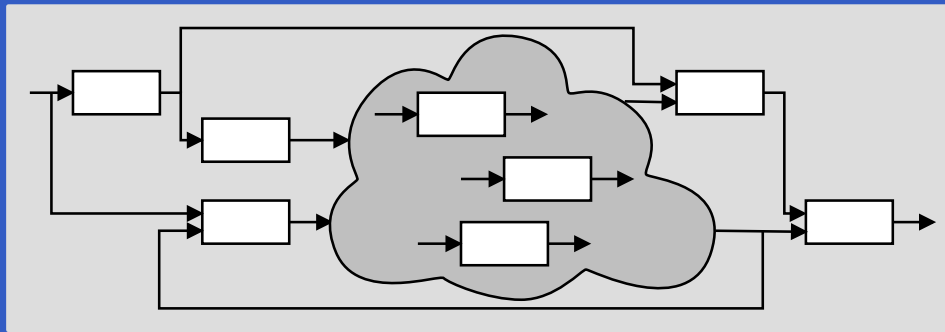
$$\begin{aligned} advanceHeads &:: Board \rightarrow BeatNo \rightarrow RelPitch \rightarrow Strength \\ &\rightarrow [PlayHead] \rightarrow ([PlayHead], [Note]) \end{aligned}$$

Lifted into a signal function primarily using *accumBy*:

$$accumBy :: (b \rightarrow a \rightarrow b) \rightarrow b \rightarrow SF (Event a) (Event b)$$
$$\begin{aligned} automaton &:: [PlayHead] \\ &\rightarrow SF (Board, DynamicLayerCtrl, Event BeatNo) \\ &\quad (Event [Note], [PlayHead]) \end{aligned}$$

Layers (1)

- A layer has two states: running and stopped
- Switching allows for:
 - Moving between states
 - Adding and removing layers dynamically



Layers (2)

A running layer is an instance of *automaton* along with a metronome:

$$\begin{aligned} \text{layerRunning} &:: \text{StaticLayerCtrl} \rightarrow [\text{PlayHead}] \\ &\rightarrow \text{SF} (\text{Event AbsBeat}, \text{Board}, \text{LayerCtrl}, \text{Event RunStatus}) \\ &\quad (\text{Event} [\text{Note}], [\text{PlayHead}]) \end{aligned}$$
$$\begin{aligned} \text{layerRunning islc iphs} &= \\ &\text{switch} (\text{lrAux islc iphs}) \$ \lambda(rs', \text{islc}', \text{iphs}') \rightarrow \\ &\quad \mathbf{case} \text{ } rs' \text{ of} \\ &\quad \text{Stopped} \rightarrow \text{layerStopped} \\ &\quad \text{Running} \rightarrow \text{layerRunning islc}' \text{ iphs}' \end{aligned}$$

Layers (3)

```
lrAux islc iphs = proc (clk, b, (slc, dlc, _), ers) → do  
  lbc ← layerMetronome islc ← (clk, dlc)  
  enphs ← automaton iphs ← (b, dlc, lbc)  
  e ← notYet ← fmap ( $\lambda rs \rightarrow (rs, slc, startHeads\ b)$ ) ers  
  returnA ← (enphs, e)
```

The static part of *LayerControl* are parameters can't usefully be changed while the automaton is running. *slc* is **sampled** at the point of switching, and becomes the new *islc*. The board *b* is sampled as well and used to compute the new *iphs*.

Automatic Restarting of a Layer

A useful feature is to allow optional automatic restart of a layer every n bars.

An additional static layer parameter *restart* :: *Maybe int* along with the following modification to *lrAux* achieves this:

$r \leftarrow \text{case } \textit{restart} \textit{ islc} \text{ of}$

$\quad \textit{Nothing} \rightarrow \textit{never}$

$\quad \textit{Just } n \rightarrow \textit{countTo} (n * \textit{barLength} + 1)$

$\quad \rightarrow \textit{lbc}$

$\textit{let } \textit{ers}' = \textit{ers} \textit{ 'lMerge' } (r \textit{ 'tag' } \textit{Running})$

$e \leftarrow \textit{notYet} \rightarrow \textit{fmap} (\lambda \textit{rs} \rightarrow (\textit{rs}, \textit{slc}, \textit{startHeads } b)) \textit{ers}'$

Automated Smooth Tempo Change

Smooth transition between two preset tempos:

$smoothTempo :: Tempo \rightarrow SF (Bool, Tempo, Tempo, Rate) \rightarrow Tempo$

$smoothTempo tpo0 = \mathbf{proc} (sel1, tpo1, tpo2, rate) \rightarrow \mathbf{do}$

\mathbf{rec}

$\mathbf{let} \ desTpo = \mathbf{if} \ sel1 \ \mathbf{then} \ tpo1 \ \mathbf{else} \ tpo2$

$\ \ diff \quad = \ desTpo - curTpo$

$\ \ rate' \quad = \mathbf{if} \quad diff > 0.1 \quad \mathbf{then} \ rate$

$\quad \quad \mathbf{else} \ \mathbf{if} \ diff < -0.1 \ \mathbf{then} \ -rate$

$\quad \quad \mathbf{else} \quad \quad \quad 0$

$\ \ curTpo \leftarrow arr (+tpo0) \lll integral \leftarrow rate'$

$\ \ \mathbf{return} A \leftarrow curTpo$

Reactive Values and Relations (1)

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 - GUI: GTK+
 - MIDI I/O: Jack

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- The Arpeggigon interacts with the outside world using two imperative toolkits:
 - GUI: GTK+
 - MIDI I/O: Jack
- Very imperative APIs: Hard or impossible to provide FRP wrappers.
- Instead, we use **Reactive Values and Relations** (RVR) to wrap the FRP core in a "shell" that acts as a bridge between the outside world and the pure FRP core.

Reactive Values and Relations (2)

- A Reactive Value (RV) is a typed mutable value with access rights and subscribable change notification.

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- RVs provide a uniform interface to GUI widgets, files, network devices, ...

For example, the text field of a text input widget becomes an RV.

- Reactive Relations (RR) allow RVs to automatically be kept in synch by specifying the relations that should hold between them.

Reactive Values and Relations (3)

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- While the RVR programming takes place in the IO monad, the code reads fairly declaratively as it specifies an interconnected network of RVs.
- Of course, RVR bindings need to be written for libraries that we wish to use unless available. Inevitably imperative code.
- RVR bindings for GTK+ are available; Jack bindings were written from scratch.

System Tempo Slider

```
globalSettings :: IO (VBox, ReactiveFieldReadWrite IO Int)
globalSettings = do
  globalSettingsBox ← vBoxNew False 10
  tempoAdj          ← adjustmentNew 120 40 200 1 1 1
  tempoLabel       ← labelNew (Just "Tempo")
  boxPackStart globalSettingsBox tempoLabel PackNatural 0
  tempoScale      ← hScaleNew tempoAdj
  boxPackStart globalSettingsBox tempoScale PackNatural 0
  scaleSetDigits tempoScale 0
  let tempoRV =
        bijection (floor, fromIntegral)
        ‘liftRW‘ scaleValueReactive tempoScale
  return (globalSettingsBox, tempoRV)
```

Pause

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- Easy to implement by combining two RVs:

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$liftR2 (\lambda tempo\ paused \rightarrow \mathbf{if\ } paused \mathbf{\ then\ } 0 \mathbf{\ else\ } tempo)$

$tempoRV$

$pauseButtonRV$

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$$\begin{aligned} \text{tempoRV}' = & \\ & \text{liftR2 } (\lambda \text{tempo paused} \rightarrow \mathbf{if\ } \text{paused\ then\ } 0 \text{ else\ } \text{tempo}) \\ & \text{tempoRV} \\ & \text{pauseButtonRV} \end{aligned}$$

- This is an equation defining $\text{tempoRV}'$ once and for all.

Connecting the Core to the Shell

The following function makes a signal function available as RVs:

yampaReactiveDual ::

a

→ SF a b

→ IO (ReactiveFieldWrite IO a, ReactiveFieldRead IO b)

This creates two reactive values: one for the input and one for the output of the signal function. After writing a value to the input, the corresponding output at that point in time can be read.

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- Reactive Values and Relations proved very helpful for bridging the gap between the outside world and the FRP core in a fairly declarative way.
- Performance in terms of overall execution time and space perfectly fine.
- **Timing** is not as tight as it should be due to naive MIDI generation.

Reading (1)

- Henrik Nilsson and Gueric Chupin. Funky Grooves: Declarative Programming of Full-Fledged Musical Applications. In *9th International Symposium on Practical Aspects of Declarative Languages (PADL 2017)*, pp. 163–172, January 2017.
- Ivan Perez and Henrik Nilsson. Bridging the GUI Gap with Reactive Values and Relations. In *Proceedings of the 8th ACM SIGPLAN Symposium on Haskell (Haskell'15)*, pp. 47–58, September 2015.

Reading (2)

- Henrik Nilsson, Antony Courtney, and John Peterson. Functional reactive programming, continued. In *Proceedings of the 2002 Haskell Workshop*, pp. 51–64, October 2002.
- Antony Courtney and Henrik Nilsson and John Peterson. The Yampa Arcade. In *Proceedings of the 2003 Haskell Workshop*, pp. 7–18, August 2003.