

# G53KRR SEM Feedback and Revision 2017

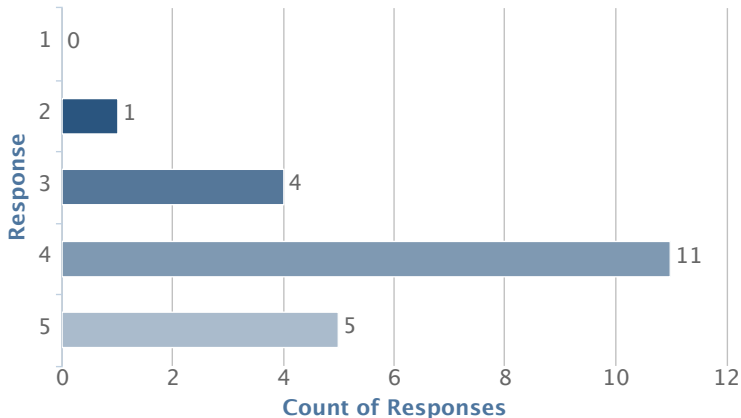
# SEM feedback

- No big issues raised
- I will go through SEM questions one by one

# Q1

1) The module has provided me with opportunities to explore ideas or concepts in depth.

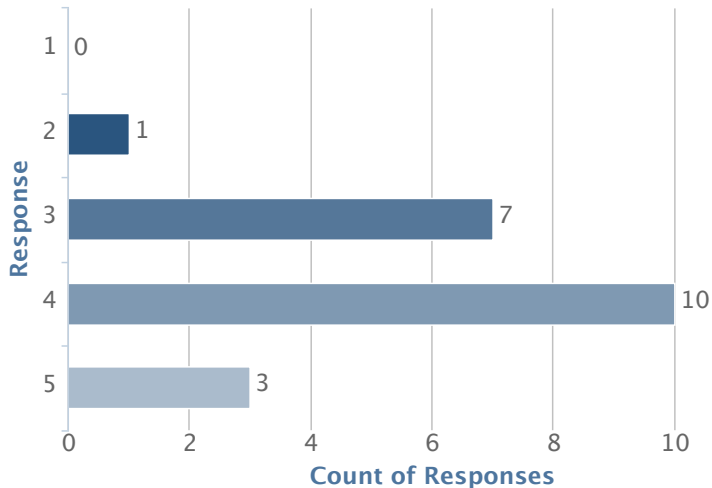
Average: 3.95



- I hope that you had an opportunity to study formal languages for knowledge representation in depth
- the fundamental concept of logical entailment
- the idea of logical reasoning/formal derivation

## Q2

2) The module has challenged me to deliver my best work.  
Average: 3.71



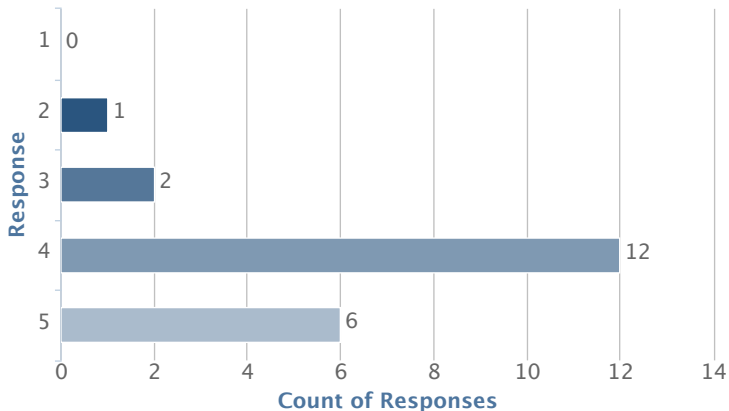
## Q2

- this is not easy to answer until the exam...

# Q3

3) The module has been well organised and has been running smoothly.

Average: 4.1



## Q3

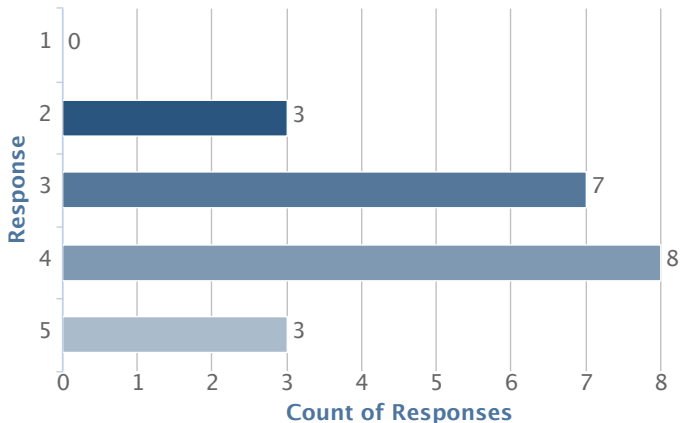
- did not get a text comment what was bad about organisation of the module
- would be grateful for feedback, anonymous or not



# Q4

4) The resources in Moodle for this module have helped me to complete my work.

Average: 3.52

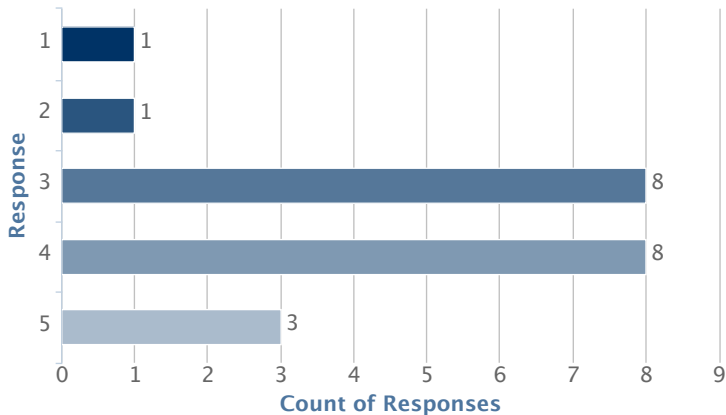


- there were clearly no resources on moodle apart from Logic in CS book
- there are however resources on the module web page, [www.cs.nott.ac.uk/~psznza/G53KRR](http://www.cs.nott.ac.uk/~psznza/G53KRR) which is linked from moodle
- hope everyone found it – it is essential for revision

# Q5

5) The criteria used in marking my work have been made clear to me.

Average: 3.52



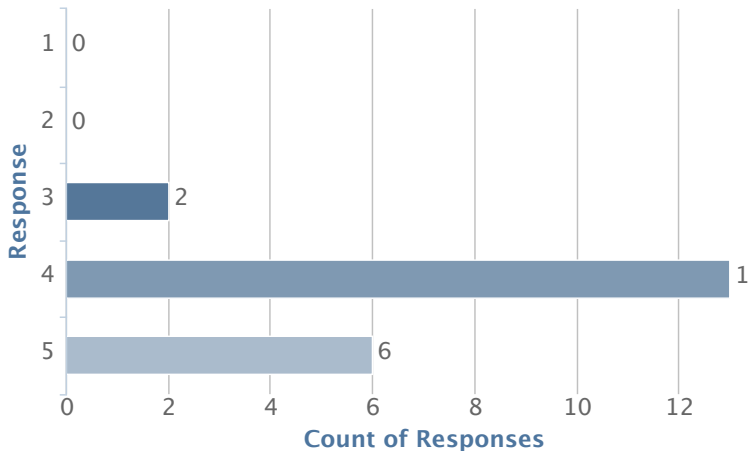
## Q5

- exam papers are on the web
- sample model answers and marking schemes are on the web
- any correct answer will get full marks
- small mistakes will get very small mark reductions or none at all, if there is evidence of clear understanding
- if you want to do a sample exam/informal coursework and get my feedback, please email it to me

# Q6

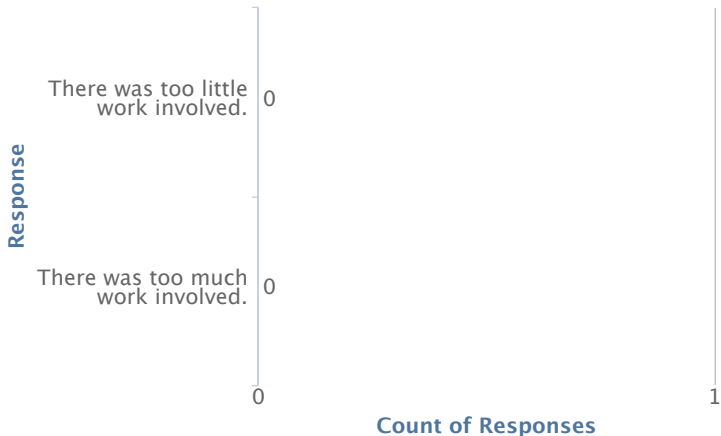
6) The workload on this module was reasonable for the number of credits

Average: 4.19



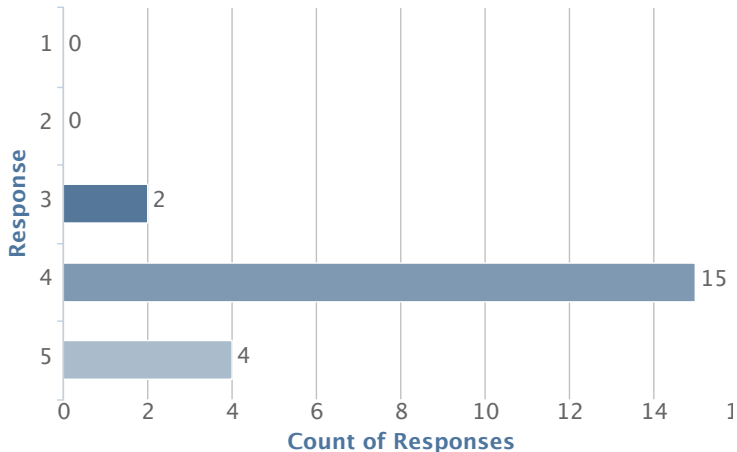
# Q6b

6b) Do you feel there was too much work involved or there was too little work involved?



# Q7

7) Overall, I am satisfied with this module.  
Average: 4.1



# Exam format

- same as in 2014 - 2016: 4 questions out of 4
- previous papers and answers on the G53KRR module web page



# Exam marking

- Answers to the exams published on the web are sample answers
- Often there are many different correct answers possible (for example, resolution derivations)
- Any correct answer will get full marks
- Answers which have minor mistakes will have minor marks reductions (or sometimes no reduction, if the answer shows clear understanding)
- Big mistakes which suggest poor understanding will lose more marks

# Exam topics = overview of the module

- First order logic
- Resolution
- Horn clauses, backward chaining, forward chaining
- Knowledge elicitation, lifecycle of a knowledge based system
- Description logic
- Non-monotonic reasoning
- Bayesian networks

# How to revise

- For each lecture, check recommended reading (on G53KRR web page)
- Do informal exercises (on G53KRR web page)
- Do exam questions from previous years (on G53KRR web page)
- Revision lecture in January?
- Send me topics for revision in advance
- Send me your exam attempts for feedback

## Some common mistakes

- Next I will go through some common mistakes, topic by topic

# Common mistakes 1

First order logic question: show that  $S1$ ,  $S2$  do not logically entail  $S3$

- Correct answer: describe an interpretation which makes  $S1$  and  $S2$  true and  $S3$  false
- Don't:
  - use truth tables for first order sentences
  - attempt a resolution derivation of  $\perp$  from  $S1$ ,  $S2$  and  $\neg S3$ , and then stop and say 'see, it does not work, so  $S3$  is not entailed'

## Common mistakes 2

### Resolution

- don't apply resolution to two literals at the same time:

$$\text{MISTAKE : } \frac{[A, B], [\neg A, \neg B]}{[]}$$

it is not sound!  $A \vee B$  and  $\neg A \vee \neg B$  should not derive false.

- only substitute for variables (not constants or functional terms)  
Don't do  $f(x)/a$  or  $a/f(x)$ .

$$\text{MISTAKE : } \frac{[(P(f(x))), [\neg P(a)]]}{[]}$$

# Bayesian networks

- Directed acyclic graph
- Nodes: propositional variables; a directed edge from  $p_i$  to  $p_j$  if the truth of  $p_i$  affects the truth of  $p_j$ .  $p_i$  parent of  $p_j$ .

$$J(\langle P_1, \dots, P_n \rangle) = Pr(P_1 \wedge \dots \wedge P_n)$$

- Chain rule

$$Pr(P_1 \wedge \dots \wedge P_n) = Pr(P_1) \cdot Pr(P_2|P_1) \cdot \dots \cdot Pr(P_n|P_1 \wedge \dots \wedge P_{n-1})$$

- Independence assumption *Each propositional variable in the belief network is conditionally independent from non-parent variables given its parent variables:*

$$Pr(P_i | P_1 \wedge \dots \wedge P_{i-1}) = Pr(P_i | \text{parents}(P_i))$$

where  $\text{parents}(P_i)$  is the conjunction of literals which correspond to parents of  $p_i$  in the network.

## Mistake 3

- Mistake: suppose a network consists of two variables,  $p_1$  and  $p_2$ , such that there is an edge from  $p_1$  to  $p_2$ . The mistake is to say that  $Pr(p_1 | p_2) = Pr(p_1)$  because  $p_2$  is not a parent of  $p_1$  (so apply the independence assumption 'in reverse order of indices')
- This is a much more subtle (and understandable given the way the independence assumption is stated) mistake.
- The independence assumption statement assumes that in the state description, the variables are listed in topological sort order (if there is an edge from  $p_i$  to  $p_j$ , then  $p_i$  appears before  $p_j$  in the order). This is always possible since the graph is acyclic. So we never check probability of parent conditioned on a child or a set of descendants.



## Some revision slides

- Next I will go through some revision topics and previous exam answers

# Circumscription

- The main idea: formalise common sense rules which admit exceptions.
- Rules like 'Birds fly' formalised as

$$\forall x (Bird(x) \wedge \neg Ab(x) \supset Flies(x))$$

- To check whether something is entailed by a knowledge base which contains such rules, we only check if it is entailed under the assumption that the set of exceptions  $I(Ab)$  is as small as possible
- This is called circumscription or minimal entailment

## Example

$$KB = \{Bird(tweety), \forall x(Bird(x) \wedge \neg Ab(x) \supset Flies(x))\}$$

- Classically,  $KB \not\models Flies(tweety)$  because there are interpretations of  $KB$  where Tweety is an exceptional bird (it is in  $I(Ab)$ ) and it does not fly
- But such interpretations do not minimise the set of exceptions: nothing which is said in  $KB$  forces us to think that Tweety is exceptional, so it does not have to be in  $I(Ab)$
- If we only consider interpretation which satisfy  $KB$  and where the set of exceptions is as small as possible, Tweety is not in this set, so  $Bird(tweety) \wedge \neg Ab(tweety)$  holds and hence  $Flies(tweety)$  holds
- $KB$  entails  $Flies(tweety)$  on 'minimal' interpretations where  $I(Ab)$  is circumscribed (made as small as possible)

## Definition of minimal entailment

- Let  $M_1 = (D, I_1)$  and  $M_2 = (D, I_2)$  be two interpretations over the same domain such that every constant and function are interpreted the same way.
- $M_1 \leq M_2 \Leftrightarrow I_1(Ab) \subseteq I_2(Ab)$
- $M_1 < M_2$  if  $M_1 \leq M_2$  but not  $M_2 \leq M_1$ . (There are strictly fewer abnormal things in  $M_1$ ).
- *Minimal entailment*:  $KB \models_{\leq} \alpha$  iff for all interpretations  $M$  which make  $KB$  true, either  $M \models \alpha$  or  $M$  is not minimal (exists  $M'$  such that  $M' < M$  and  $M' \models KB$ ).

## Back to the example

- $KB = \{Bird(tweety), \forall x (Bird(x) \wedge \neg Ab(x) \supset Flies(x))\}$
- $KB \models_{\leq} Flies(tweety)$  because for every interpretation  $M$  which makes  $KB$  true and  $Flies(tweety)$  false, it has to be that  $I(tweety) \in I(Ab)$ .
- So for every such interpretation there is an interpretation  $M'$  which is just like  $M$ , but  $I'(tweety) \notin I'(Ab)$  and  $I'(tweety) \in I'(Flies)$ , and  $M'$  still makes  $KB$  true and  $M' < M$ .

# Defaults

- A *default rule* consists of a *prerequisite*  $\alpha$ , *justification*  $\beta$ , *conclusion*  $\gamma$  and says 'if  $\alpha$  holds and it is consistent to believe  $\beta$ , then believe  $\gamma$ ': 
$$\frac{\alpha : \beta}{\gamma}$$

- For example:

$$\frac{Bird(x) : Flies(x)}{Flies(x)}$$

- Default rules where justification and conclusion are the same are called *normal default rules* and are written  $Bird(x) \Rightarrow Flies(x)$ .

# Default theories and extensions

- A default theory  $KB$  consists of a normal first-order knowledge base  $F$  and a set of default rules  $D$
- A set of reasonable beliefs given a default theory  $KB = \{F, D\}$  is called an *extension* of  $KB$
- $E$  is an *extension* of  $(F, D)$  iff for every sentence  $\pi$ ,

$$\pi \in E \Leftrightarrow F \cup \left\{ \gamma \mid \frac{\alpha : \beta}{\gamma} \in D, \alpha \in E, \neg\beta \notin E \right\} \models \pi$$

# How one could construct an extension

$$\pi \in E \Leftrightarrow F \cup \{\gamma \mid \frac{\alpha : \beta}{\gamma} \in D, \alpha \in E, \neg\beta \notin E\} \models \pi$$

- 1  $E := F$ ;
- 2 close  $E$  under classical entailment:  $E := \{\pi : E \models \pi\}$
- 3 choose some (substitution instance of)  $\frac{\alpha : \beta}{\gamma} \in D$
- 4 if  $\alpha \in E$ , and  $\neg\beta \notin E$  (meaning,  $\beta$  is consistent with  $E$ ),  
 $E := E \cup \{\gamma\}$
- 5 go back to 2



# Example

$$F = \{Bird(tweety)\}, D = \left\{ \frac{Bird(x) : Flies(x)}{Flies(x)} \right\}$$

- $E := \{Bird(tweety)\}$
- close  $E$  under classical entailment:  $E := \{\pi : Bird(tweety) \models \pi\}$
- $\frac{Bird(tweety):Flies(tweety)}{Flies(tweety)} \in D$
- $Bird(tweety) \in E$ , and  $\neg Flies(tweety) \notin E$   
 $E := E \cup \{Flies(tweety)\}$
- $E := \{\pi : Bird(tweety), Flies(tweety) \models \pi\}$
- there are no more rules to apply

## Example from 2008 exam, Q6e

$$F = \{Dutchman(peter), Dutchman(hans), Dutchman(johan),$$
$$peter \neq hans, hans \neq johan, peter \neq johan,$$
$$\neg Tall(peter) \vee \neg Tall(hans)\}$$
$$D = \left\{ \frac{Dutchman(x) : Tall(x)}{Tall(x)} \right\}$$

Three instances of the default rule:

$$\frac{Dutchman(peter) : Tall(peter)}{Tall(peter)} \quad \frac{Dutchman(hans) : Tall(hans)}{Tall(hans)}$$
$$\frac{Dutchman(johan) : Tall(johan)}{Tall(johan)}$$

## Exam 2008 example continued

- Suppose we start constructing  $E_1$  with the first rule, for Peter. Since  $\neg Tall(peter) \notin E_1$ , we can add  $Tall(peter)$  to  $E_1$ .
- After we close  $E_1$  under consequence, from  $Tall(peter)$  and  $\neg Tall(peter) \vee \neg Tall(hans)$  we get  $\neg Tall(hans) \in E_1$ .
- So now the second rule for Hans is not applicable.
- The third rule is applicable, since  $\neg Tall(johan) \notin E_1$ , we can add  $Tall(johan)$  to  $E_1$ .
- Another possible extension is  $E_2$ : we use the second rule first, and add  $Tall(hans)$  to  $E_2$ .
- Now the first rule is not applicable, because  $E_2$  contains  $\neg Tall(peter)$ .
- The third rule is applicable, since  $\neg Tall(johan) \notin E_2$ , we can add  $Tall(johan)$  to  $E_2$ .

## Another example with two extensions

- Facts:  $F = \{Republican(dick), Quaker(dick)\}$
- Default rules:  $Republican(x) \Rightarrow \neg Pacifist(x)$ ,  
 $Quaker(x) \Rightarrow Pacifist(x)$ .
- Extension  $E_1$  (pick the rule  $Republican(x) \Rightarrow \neg Pacifist(x)$  first) is all consequences of  
 $\{Republican(dick), Quaker(dick), \neg Pacifist(dick)\}$ . Because we start with  $E_1 = \{Republican(dick), Quaker(dick)\}$ ,  
 $\neg\neg Pacifist(dick) \notin E_1$ , so we can add  $\neg Pacifist(dick)$  to  $E_1$ .
- Extension  $E_2$  (pick the rule  $Quaker(x) \Rightarrow Pacifist(x)$  first) is all consequences of  
 $\{Republican(dick), Quaker(dick), Pacifist(dick)\}$ . Because we start with  $E_2 = \{Republican(dick), Quaker(dick)\}$ ,  
 $\neg Pacifist(dick) \notin E_2$ , so we can add  $Pacifist(dick)$  to  $E_2$ .

## Example with one extension

- Facts:  $F = \{Republican(dick), Quaker(dick), \forall x (Republican(x) \supset MemberOfPoliticalParty(x))\}$
- Default rules:  $Republican(x) \Rightarrow \neg Pacifist(x),$

$$\frac{Quaker(x) : Pacifist(x) \wedge \neg MemberOfPoliticalParty(x)}{Pacifist(x)}$$

- Closure of  $F$  under consequence includes:  
 $\{Republican(dick), Quaker(dick), \forall x (Republican(x) \supset MemberOfPoliticalParty(x)), MemberOfPoliticalParty(dick)\}$
- The second default rule is not applicable, because  $\neg\neg MemberOfPoliticalParty(dick) \in E$
- only the first rule is applicable, since  $\neg\neg Pacifist(dick) \notin E$ , so  $\neg Pacifist(dick)$  is added.

Any questions?