

Stacks and Queues

In this lecture:

- Variants on Lists
- Stacks
- Queues

Variants of Lists

- Previous lecture: double ended list (constant time access to front and end of list). Simpler variant: only access to the head of the list is constant time, to get to the tail need to traverse the list.
- Circular lists (ring buffers)
- Doubly linked lists

Circular lists

- Last link points back to first link.
- Terminating traversals of the list:
- Maintain separate count of list size, or:
- Sentinel element at end of list

- Usage: circular buffers

Doubly linked lists

- Each link points to its successor *and* predecessor in the list.

- Useful when the list should be traversible in both directions. Example of use: text processor where every line is an element in the list.

Stacks and Queues

- Not so much for data storage: more for organising programs

Stack: Last In, First Out

Stack : Last In, First Out

A

Stack : Last In, First Out

B
A

Stack : Last In, First Out

C
B
A

Stack : Last In, First Out

B
A

Stack : Last In, First Out

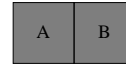
A

Queue: First In, First Out

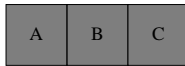
Queue: First In, First Out



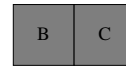
Queue: First In, First Out



Queue: First In, First Out



Queue: First In, First Out



Queue ADT

As for lists, need an ADT for items which are kept there. Let us call it **ItemType** (in Java, could be **Object**).

Methods

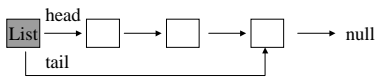
- **void enqueue(ItemType item)**
Postcondition: item added to end of queue.
- **boolean isEmpty()**
Postcondition: returns true if queue is empty

Methods contd.

- **ItemType dequeue()**
Precondition: queue is not empty
Postcondition: returns item at front of queue and deletes it from the queue.
- **ItemType peek()**
Precondition: queue is not empty
Postcondition: returns item at front of queue.

List implementation of queue

- Uses double ended list like the one from the previous lecture.
- enqueue(Object item): insert at tail
- dequeue(Object item): remove and return the head of the list.



Array implementation of queue

- Two indices: one for the front and one for the back of the queue.
- Deleting from front: increment front index
- Adding to back: increment back index.
- The queue wraps around, but front and back are not allowed to cross past each other.

Array implementation of Queue

Example:



↑
front = back = 0

size=0
capacity=4

Array implementation of Queue

Enqueue an item:

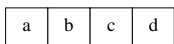


↑ ↑
front back
=0 =1

size=1
capacity=4

Array implementation contd.

- Make the queue full:



↑
front=back=0

size=capacity=4

Array implementation contd.

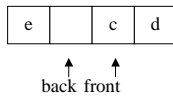
- Delete some things:



↑ ↑
back front

Array implementation contd.

- Insert more things:



Java for the array implementation

- Fields: `array arr; int front; int back; int size; int capacity`
- `isempty()`{
 `return (size == 0);`
}
- `peek()` { `if !isempty()`
 `return arr[front];`
 `else // throw exception`}

Array implementation contd.

- `enqueue(Object x){`
 `if (size == capacity) throw an`
 `exception: queue is full`
 `else {`
 `arr[back] = x;`
 `size++;`
 `if (back==capacity-1) back = 0;`
 `else back++;`
 `}}`

Array implementation contd.

- `dequeue(){`
 `if (size == 0) throw an exception:`
 `queue is empty`
 `else {`
 `value = arr[front];`
 `if(front==capacity-1) front=0;`
 `else front++;`
 `size--;`
 `return value;`
 `}}`

Stack ADT

- Logical domain: stacks of `ItemType`.
- Methods:
 - `boolean isempty()`
 Postcondition: returns true if stack is empty
 - `ItemType peek()`
 Precondition: stack is not empty
 Postcondition: item at top of stack returned.

Stack Methods contd.

- `void push (ItemType item)`
 Postcondition: item added to top of stack
- `ItemType pop()`
 Postcondition: item at top of stack returned and
 deleted from stack

Variations

- If we consider stacks of fixed maximal size, need the following variation:
- `boolean full()`
Postcondition: returns true if stack is full
- `void push(ItemType item)`
Precondition: stack is not full.
Postcondition: item added to top of stack.

Stack Implementations

- Vector implementation:
- Makes more sense when the size of stack is known in advance.
- No dynamic memory allocation or deallocation required once stack is created (unless we have to do dynamic re-sizing).
- Constant time access to top of stack

Stack implementations

- Linked list implementation:
- No limits on size of stack, and size need not be known in advance.
- Dynamic memory allocation and deallocation whenever items are popped onto or pushed off the stack
- Constant time access to top of stack.

Linked List Implementation

- Use a simple linked list
- `peek() { return the value at head;}`
- `push() {insert an item at the head;}`
- `pop() {return the value at head and reset the head to be the head.next link;}`

Vector Implementation

- Could have done an array implementation, but resizable array (vector) really makes more sense.
- Fields: resizable vector `vec` holding the stack and index of stack top (first free position in the stack), `top`. Stack grows to the right.

Vector Implementation

- Methods:
 - `boolean isempty() { return (top == 0) ; }`
 - `Object peek() { return vec.elementAt(top-1); }`
// will throw an exception if the stack is empty

Vector Implementation

```
• void push(Object item) {  
    vec.add(top++, item);  
}  
• Object pop() {  
    if (isempty) // throw exception  
    else {  
        return vec.elementAt(--top);  
    }  
}
```

Summary

- Stacks and queues are very important ADTs and have many uses.
- Stacks: LIFO (last in, first out).
- Queues: FIFO (first in first out).
- Can be implemented in different ways.
- For stacks, vector implementation is better if maximum size of stack can be predicted.
- Queues: array/vector or linked list implementation (list implementation is more straightforward).

Eliminating Recursion

- Recursion overheads
- Tail recursion elimination
- Elimination of recursion using a stack (don't try this at home)

Recursion is Expensive

- Recursive algorithms are elegant and usually easier to understand and implement, but recursive calls are expensive.
- Each recursive call is usually implemented by placing all the necessary information (return address, parameters, local variables) onto a stack. Each return pops the corresponding record of the stack.
- This uses both time (in setting up the record) and space on the stack.

Recursive factorial

```
recFactorial(n) { // assume n >=0  
    if (n <= 1) {  
        return 1;  
    } else {  
        return n*recFactorial(n-1);  
    }  
}
```

Iterative Factorial

```
itFactorial(n) {  
    result = 1;  
    while (n > 1) {  
        result = result * n;  
        n--;  
    }  
    return result;  
}
```

Tail recursion optimisation

- Even if you don't replace recursion by iteration in this case, it is likely that a decent compiler will.
- Instead of keeping all intermediate values on the stack, it will update the same variable (using constant space)
- In some cases this is not possible and explicit stack is used: does not save a lot of space but is still more efficient.

Just for illustration: factorial again

```
stackFactorial(n) {
    Stack stack = newStack();
    while (n>1) stack.push(n--);
    result = 1;
    while(! stack.isEmpty()) {
        result = result * stack.pop();
    }
    return result;
}
```

Real Example: Quicksort

```
public void recQuickSort(int[] arr,
    int left, int right){
    if (right - left) <= 0) return;
    else {
        int border = partition(arr, int
        left, int right);
        recQuickSort(arr, left, border-
        1);
        recQuickSort(arr, border+1,
        right);
    }
}
```

Quicksort using a stack

```
public void stackQuickSort(int[]
arr, int left, int right){
    Stack stack = new Stack(); //
    int border;
    // assume the stack can keep ints
    stack.push(left);
    stack.push(right);
```

Iterative Quicksort contd.

```
while(! stack.isEmpty()){
    int j = stack.pop();
    int i = stack.pop();
    border = partition(arr, i, j);
```

Iterative Quicksort contd.

```
if((border-1) - i > 1) {
    stack.push(i);
    stack.push(border-1);
}
if(j - (border+1) > 1) {
    stack.push(border+1);
    stack.push(j);
}
}
```


Example

Consider sorting the following array:

0	1	2	3	4
17	3	8	16	5

Stack: 4
0

Example

After the first iteration:

0	1	2	3	4
5	3	8	16	17

4
3
Stack: 1
0

Example

After the second iteration:

0	1	2	3	4
5	3	8	16	17

Stack: 1
0

Example

After the third iteration:

0	1	2	3	4
3	5	8	16	17

Stack:

Further reading

- Shaffer, chapter 4 (4.2 and 4.3).

Summary

- Recursion can always be eliminated using an explicit stack if you need a more efficient algorithm.
- However the resulting implementation maybe more difficult to understand and debug.