# COMP2012/G52LAC Languages and Computation Lecture 5 Regular Expressions

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# **Regular Expressions**

- Automata describe languages in a somewhat indirect way: not always obvious what the defined language is.
- *Regular Expressions* offer a different, more direct way to describe languages.
- We will see (later) that the class of languages that can be described by regular expressions again is the same as those describable by DFAs and NFAs.
- This class is called the *regular* languages. Hence the name regular expressions.

# **Semantics of Regular Expressions**

1.  $L(\emptyset) = \emptyset$ 

- **2.**  $L(\epsilon) = \{\epsilon\}$
- 3. For all  $x \in \Sigma$ ,  $L(\mathbf{x}) = \{x\}$
- **4.**  $L(E + F) = L(E) \cup L(F)$
- **5.** L(EF) = L(E)L(F)
- 6.  $L(E^*) = L(E)^*$
- **7.** L((E)) = L(E)

### **Recap: DFAs and NFAs (1)**

We have so far encountered two ways of describing formal languages:

• Deterministic Finite Automata (DFA)

 $(Q, \Sigma, \delta, q_0, F)$ 

• Non-deterministic Finite Automata (NFA)

 $(Q, \Sigma, \delta, S, F)$ 

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# Syntax of Regular Expressions

1.  $\emptyset$  is an RE

2.  $\epsilon$  is an RE

3. For all  $x \in \Sigma$ , x is an RE (Handwriting convention: <u>x</u> is an RE)

- 4. If *E* and *F* are REs, so is E + F
- 5. If E and F are REs, so is EF
- 6. If E is an REs, so is  $E^*$
- 7. If E is an REs, so is (E)

#### These are *all* regular expressions.

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# **Recap: DFAs and NFAs (2)**

Key difference: the type of the transition function:

- **DFA**:  $\delta \in Q \times \Sigma \to Q$
- **NFA:**  $\delta \in Q \times \Sigma \to \mathcal{P}(Q)$

Language of an automaton: the set of all words it accepts.

As DFAs and NFAs are *interconvertible*, these two kinds of automata defines the same *class* of languages.

# Conventions

 The \*-operator has higher precedence than + and sequencing.
E.g.

$$\mathbf{ab}^* = \mathbf{a}(\mathbf{b}^*)$$
  
 $\mathbf{a} + \mathbf{b}^* = \mathbf{a} + (\mathbf{b}^*)$ 

- Sequencing has higher precedence than  $+. \ \mbox{E.g.}$ 

ab + cd = (ab) + (cd)

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